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The Impact of Two Coupled Cirrus Microphysics-Radiation Parameterizations on the Temperature and Specific Humidity Biases in the Tropical Tropopause Layer in a Climate Model

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1   ABSTRACT

2   The impact of two different coupled cirrus microphysics-radiation parameterizations

3   on the zonally averaged temperature and humidity biases in the tropical tropopause layer

4   (TTL) of a Met Office climate model configuration is assessed. One parameterization is

5   based on a linear coupling between a model prognostic variable, the ice mass mixing

6   ratio, q_i, and the integral optical properties. The second is based on the integral optical

7   properties being parameterized as functions of q_i and temperature, T_c, where the mass

8   coefficients (i.e. scattering and extinction) are parameterized as nonlinear functions of the

9   ratio between q_i and T_c. The cirrus microphysics parameterization is based on a moment

10 estimation parameterization of the particle size distribution (PSD), which relates the mass

11 moment (i.e. second moment if mass is proportional to size raised to the power of 2) of

12 the PSD to all other PSD moments through the magnitude of the second moment and T_c.

13 This same microphysics PSD parameterization is applied to calculate the integral optical

14 properties used in both radiation parameterizations and, thus, ensures PSD and mass

15 consistency between the cirrus microphysics and radiation schemes.

16   In this paper, the temperature-non-dependent and temperature-dependent

17 parameterizations are shown to increase and decrease the zonally averaged temperature

18 biases in the TTL by about 1 K, respectively. The temperature-dependent radiation

19 parameterization is further demonstrated to have a positive impact on the specific

20 humidity biases in the TTL, as well as decreasing the shortwave and longwave biases in

21 the cloudy radiative effect. The temperature-dependent radiation parameterization is

22 shown to be more consistent with TTL and global radiation observations.

23

1. Introduction

It is well known that cirrus makes an important contribution to the radiative balance of the tropical tropopause layer (TTL) through its temperature, spatial distributions, opacity, and composition. Moreover, it influences the water vapor concentration in the stratosphere (Heymsfield 1986; Sassen et al. 1989; McFarquhar et al. 2000; Corti et al. 2006; Wang and Dessler 2006; Stubenrauch et al. 2007; Jensen et al. 2008; Mace et al. 2009; Yang et al. 2010; Schwartz and Mace 2010; Taylor et al. 2011; Zhou et al. 2014; Hong and Liu 2015; Hardiman et al. 2015, and references therein).

Typical TTL cirrus will efficiently trap outgoing longwave radiation from the surface and atmosphere, generally leading to a warming of the surface, and absorb incoming shortwave radiation at near-infrared wavelengths, generally leading to a local heating of the upper troposphere (Liou 1986; Liou 2005; Edwards et al. 2007; Baran 2009; Taylor et al. 2011; Baran 2012; Yi et al. 2013; Zhou et al. 2014; Hong and Liu 2015; Yang et al., 2015; Hardiman et al. 2015). The balance between cirrus warming or cooling the upper troposphere depends on its visible optical depth, as shown by Hong and Liu (2015), who demonstrated that cirrus with visible optical depths less than unity leads to a net heating of the upper troposphere, whilst optically thicker cirrus results in a net cooling of the upper troposphere. Moreover, subvisual cirrus occurs in the TTL, as found by Lawson et al. (2008), and Lee et al. (2009) showed that these clouds may exert a net radiative effect on the order of about 1.1 Wm^{-2}.

In general, the role of cirrus in either heating or cooling the TTL depends not only

on the visible optical depth but also on the microphysics and the scattering and

absorption properties of atmospheric ice (Baran et al. 2014a; Yang et al. 2015, and

references therein). There have been aircraft campaigns which have examined the ice

microphysics composition of the TTL. In the study by Heymsfield (1986), the

common occurrence of trigonal particles was reported but more recent studies by

Lawson et al. (2008) have found few occurrences of trigonal ice particles. In the study

by McFarquhar et al. (2000), they found habit mixtures comprising 50% of hexagonal

columns and trigonal ice crystals in the subvisual TTL cirrus they studied.

Meanwhile, Lawson et al. (2008) found the occurrence of quasi-spherical ice particles

to be the most common particle type for all crystal sizes. However, it is uncertain as

to whether these particles are actually quasi-spherical due to the limiting resolving

power of the microphysics instrumentation used at the time; therefore, the appearance

of quasi-sphericity could be due to diffractive and optical effects, as noted by Cotton

et al. (2010) and references therein. On the other hand, these particles could be quasi-

spherical, but instruments are required that can adequately resolve these ice crystals

of an uncertain shape, such as the small ice detector described in Ulanowski et al.

(2006). For crystal sizes greater than 65 μm, Lawson et al. (2008) found habit

mixtures comprising mostly hexagonal plates and irregular ice crystals. In the study

by Jensen et al. (2008) they noted the occurrence of hexagonal plate aspect ratios of

6:1 of nearly 100 μm in size near the TTL, which were reported to be unassociated

with deep tropical convection. The more recent Airborne Tropical TRopopause

Experiment (ATTREX) reported by Jensen et al. (2015) found bullet rosettes to be

commonly occurring with little evidence of aggregated ice crystals in the cirrus cases

they sampled. The two particle size distributions shown in Jensen et al. (2015) extend

to maximum dimensions of about 50 μm and almost 200 μm, at temperatures of <

195 K and between about 195 and less than 210 K, respectively. Meanwhile, Lawson

et al. (2008) report particle distributions extending to 165 μm in the subvisual TTL

cirrus they sampled, which contrasts with the study of McFarquhar et al. (2000), who

found that particle maximum dimensions did not extend to beyond 50 μm.

Determining the habit mixtures and particle distributions in TTL cirrus is important,

as the choice of assumed particle distributions in climate models will influence their

predicted radiative effect of cirrus. For instance, in the study of Mitchell et al. (2008)

they show that by assuming two different parameterizations of the small ice mode,

the shortwave radiative effect differences in the annual zonally averaged fluxes at

top-of-atmosphere in the tropics can be up to about -25 Wm^{-2}. They also show that

the longwave differences in the tropics can be up to 20 Wm^{-2}. Clearly, from the

studies cited above, there is uncertainty as to the most general ice microphysics

composition in the TTL to assume in models, in turn, this will affect climate model

simulations of the TTL, as differing climate models assume dissimilar microphysics

properties, which may lead to an excess in TTL warming or cooling (Hardiman et al.

2015). Further campaigns in the TTL are necessary if such uncertainties reported by

Hardiman et al. (2015) are to be reduced in climate models. However, recent TTL

process studies by Hardiman et al. (2015) have shown that physically improved

climate model parameterizations do not necessarily improve simulations of the TTL.

For example, recent parameterizations of cirrus microphysics and bulk optical

properties by Furtado et al. (2015) and Baran et al. (2014a), respectively, were shown

to increase the temperature and specific humidity biases in the TTL in recent global configurations of the Met Office Unified Model (MetUM). In this paper, the physical reasons are explored as to why the Baran et al. (2014b) parameterizations, hereinafter referred to as B014b, increased the TTL temperature bias in the climate model. This paper also presents a new bulk optical property parameterization of cirrus that is demonstrated to provide a more accurate simulation of the TTL in the MetUM as well as an improved representation of MetUM simulations of the cloudy shortwave and longwave radiative effects. The paper is organised as follows: Section 2 describes the bulk optical property parameterization and its accuracy, and includes comparisons between the new and the B014b parameterizations. Section 3 briefly describes a baseline MetUM configuration and compares the impact of the new and B014b parameterizations on this configuration against both observations and analyses. Section 4 discusses the results.

2. The parameterization

The parameterization presented in this paper is based on the ensemble model of cirrus ice crystals fully described in Baran and Labonnote (2007), whereby the bulk optical properties are derived by averaging habit-dependent, single-scattering properties over an assumed PSD; a figure of the model is shown in Fig. 2 in B014b. A brief description of the model is given here. The ensemble model consists of six shapes, and these are a hexagonal ice column of an assumed aspect ratio (AR) of unity, the six-branched bullet rosette, and then hexagonal monomers are randomly attached to build four ice aggregate models, which consist of three-, five-, eight- and, finally, ten-branched hexagonal ice aggregates. The latter aggregate models can cover the largest ice crystal sizes found in the

PSD, whilst the former members can populate the smaller end of the ice crystal PSD.

Alternatively, weights can be assigned to each member of the ensemble model at each

PSD bin size to compute the bulk optical properties. Here, use is also made of the same

bulk ice optical property database that was used to develop the B014b parameterization.

The database is composed of the following bulk optical properties: the extinction and

scattering coefficients, the single-scattering albedo, ω_0, and the asymmetry parameter, g.

These bulk optical properties are defined by Eqs. (1–3) in B014b, and the same

definitions are used in this paper. A full description of that database can be found in

B014b and in Baran et al. (2014a), hereinafter referred to as B014a. However, brief

descriptions of the bulk optical property database and its experimental validation are

given here. The database described in B014a consists of 20662 values of ice water

content (IWC) and T_c, which were compiled from a number of cirrus field campaigns

described in Baran et al. (2011a), and these in-situ campaigns were predominantly

located between northern Europe and the tropics. However, most of the in-situ IWC

values that were compiled by Baran et al. (2011a) were not obtained at temperatures

colder than -60°C. Due to this lack of in-situ ice microphysics measurements down to

temperatures as low as -80°C, in B014a, IWC values were randomly selected from

temperatures warmer than -60°C and placed at temperatures between -60 and -80°C. In

this way, the IWC and T_c space was built up to 20662 values, which ranged between

about 3.0×10^{-3} and about 10^{-9} kg m^{-3}, and between about -80 and 0°C, respectively. This

range in IWC and T_c is sufficient to cover the range in IWC and T_c values that are likely

to be predicted in the MetUM.

   In B014a and B014b, the IWC and T_c values were related to the PSD through a

moment estimation parameterization of the PSD due to Field et al. (2007), and this

parameterization is further described below. The IWC–T_c generated PSDs were

previously applied to the ensemble model single-scattering properties described in B014a

to obtain the cirrus bulk optical properties used in B014b at 145 wavelengths between

0.20 and 120 µm. The same bulk ice optical properties utilized in B014b are used in this

paper.

The coupled IWC–T_c bulk ice optical properties used in this paper have been validated

using a variety of aircraft and space-based solar and infrared radiometric measurements.

For instance, in B014a the ensemble model bulk ice optical properties were applied to a

fast radiative transfer model to simulate very high-resolution solar (between about 3.4

and 4.1 µm) and infrared (between about 8.0 and 12.0 µm) aircraft-based brightness

temperature measurements obtained from directly above midlatitude cirrus of visible

optical depth varying between about 0.03 and 0.06. It is shown in the paper that the solar

and infrared brightness temperature measurements were mostly simulated to within $\pm$ 2

and $\pm$ 1 K, respectively. Note also that the lower visible optical depth of 0.03 is generally

taken as the upper limit for "subvisual" cirrus, as defined by Sassen and Cho (1992).

Moreover, B014a also showed that the same ensemble microphysical model could

forward model deep frontal cirrus effective radar reflectivity at 35 GHz and microwave

brightness temperatures at 190 GHz to generally within ± 2 dBZ$_e$ and $\pm$ 2K, respectively.

Thus, B014a showed that in the case of the solar and infrared measurements, the same

microphysical model can be consistently applied across the spectrum using a full set of

optical properties (i.e. the scattering phase function and integral optical properties) to

simulate those observations. Meanwhile, Sourdeval et al. (2015) demonstrated that the

same ensemble model bulk ice optical properties used in B014a could also replicate

Cloud-Aerosol Lidar with Orthogonal Polarization (CALIOP) and in-situ polar

nephelometer measurements of the volume extinction coefficient of midlatitude cirrus to

generally within the standard deviation of both CALIOP and polar nephelometer

measurements. The in-situ and CALIOP volume extinction coefficients varied between

less than about 0.2 and 1.4 km^{-1}, at the wavelengths of 0.532 and 0.80 μm, respectively.

The ensemble model's predicted bulk optical properties have also been globally validated

by Vidot et al. (2015) and Letu et al. (2015).

   In Vidot et al. (2015) it is shown that an equivalent weighting of 0.30, 0.30, 0.10, 0.20,

and 0.10 applied to each of the ensemble habit extinction and scattering coefficients at

each bin size of the Field et al. (2007) PSD parameterization best simulated cirrus

infrared brightness temperature measurements from the Imaging Infrared Radiometer

(IIR) instrument at wavelengths of 8.65, 10.60 and 12.05 μm. The combined mean

brightness temperature bias using the weighted model optical properties was found to be

only 0.43 K with a standard deviation of 6.85 K for visible optical depths between 0.03

and 4.0. The IIR brightness temperature simulations were based on more than 26000

profiles of IWC from the 2C-ICE and DARDAR products (Deng et al. 2010; Delanöe and

Hogan 2010). The IWC product profiles and atmospheric profiles (the latter profiles came

from the European Centre for Medium Range Weather Forecasts and were colocated with

CALIOP) were located between the latitudes of about ±60° and at altitudes between about

440 and 50 hPa, thus covering the region of the TTL, and most of the profiles were

located in the tropics. Meanwhile, Letu et al. (2015) used global observations from the

Polarization and Directionality of the Earth's Reflectances-3 (POLDER-3) measurements

1 on board the Polarization and Anisotropy of Reflectances for Atmospheric Sciences

2 coupled with Observations from a Lidar (PARASOL) to show that the ensemble model's

3 predicted ice cloud solar optical depths at a wavelength of 0.865 μm best minimized

4 differences between observations, with all ice crystal models considered. The POLDER-3

5 analysis of Letu et al. (2015) is based on 589246 pixels, with each pixel size being

6 approximately 6 km × 6 km. In most pixels the scattering angle range covered is between

7 60° and 160°, and in some pixels the scattering angle range covered is between 160° and

8 180°. The pixels were located between the latitudes of about $\pm 90^{o}$, but the vast majority

9 of pixels were located at latitudes between about $\pm 60^{o}$. The data covers the period

10 between the 20th to 22nd of March, June, September and December 2008. Therefore, all

11 meteorological seasons are covered in the time period studied by Letu et al. (2015), and

12 the study is, thus far, the most comprehensive and consistent analysis of POLDER-3

13 global data. Given the preceding evidence, the ensemble model bulk ice optical properties

14 have been sufficiently validated globally to apply to a parameterization of cirrus optical

15 properties in a climate model. Such validation exercises described above are necessary to

16 carry out to show that the full set of optical properties are consistent with measurements

17 from across the spectrum in order to provide confidence in their applicability to climate

18 models. As a further example of this validation approach, see for example, the paper by

19 Holz et al. (2015).

20   The PSDs applied to the ensemble model single-scattering properties in the

21 preceding literature assumed the Field et al. (2007) moment estimation

22 parameterization of the PSD, hereinafter referred to as F07. A full derivation of the

23 PSD parameterization is given in F07, but a brief description is given here. The Field

1   et al. (2007) parameterization is based on 10000 in-situ measurements of the PSD and

2   IWC, which were measured between the temperatures of $0\,^{\circ}C$ and $-60\,^{\circ}C$ during a

3   number of cirrus field campaigns located in the midlatitudes and tropics. The

4   parameterization is based on the moments of the PSD, given by the integral product

5   of D^n and f(D), where D is the maximum dimension of the ice crystal and f(D) is the

6   PSD, which gives the particle number concentration at each D, and $n \geq 0$. Therefore,

7   the zeroth moment (i.e. n=0) is the total number concentration of particles per unit

8   volume of cloudy air. The PSD parameterization is related to the total IWC through

9   some assumed relationship between mass and D, where in the case of aggregating ice

10   crystals the mass of ice $\propto D^2$ (Westbrook et al. 2004; Cotton et al. 2013, and

11   references therein). The other moments of the PSD are related to the 2nd moment (M_2)

12   through a relationship of the form $M_n = \sigma_n M_2{}^{\beta_n}$, where σ_n and β_n are functions of T_c.

13   Therefore, given all M_n, the full PSD can be estimated from the IWC and T_c values

14   via an assumed mass–dimensional relationship. It should be noted here that to reduce

15   the impact of ice crystal shattering on the PSD parameterization, the in-situ PSDs in

16   F07 were filtered by using the measured inter-arrival times of the ice crystals as

17   described in F07 and in Field et al. (2006), and ice crystals with $D < 100$ µm were

18   ignored. However, the PSD parameterization does not ignore the shape of the ice

19   crystal PSD at $D < 100$ µm, but instead assumes an exponential PSD (Field and

20   Heymsfield 2003) that is added to a modified gamma distribution at an ice crystal size

21   of about 100 µm. The degree to which in-situ PSDs are skewed due to ice crystal

22   shattering has more recently been studied by Korolev et al. (2013). In that paper, they

23   found that if filtering alone is applied without any modifications to the in-situ

microphysics probes on board aircraft, such as the use of anti-shatter tips, the PSD

becomes significantly skewed from the best measured PSD at D ≤ 200–175 μm,

where the best measured PSDs were determined using both anti-shatter tips and

filtering. Korolev et al. (2013) state that the precise ice crystal size at which

significant divergence from the best-estimated PSD occurs cannot as yet be

determined due to insufficient statistical sampling of ice clouds. In other words, there

are too few cirrus field campaigns on which to base firm conclusions. Therefore, it is

currently unknown as to the degree to which the F07 parameterization has been

affected by the shattering of ice. However, this parameterization is more

representative of cirrus PSDs than the Houze et al. (1979) PSD parameterization,

which is the current assumption in the MetUM operational model. The Houze et al.

(1979) parameterization is based on 37 in-situ PSDs, 90% of which were measured at

temperatures warmer than -30°C. Currently, within the operational MetUM, the

Houze et al. (1979) estimated PSD is kept constant at temperatures colder than -35°C.

This assumption means that at much colder temperatures, such as those that occur

within the TTL region, there will be orders of magnitude more frequently occurring

large ice crystals than there should be. This has clear implications for the assumed fall

speed of ice crystals within the MetUM model, which must be artificially increased to

several ms^{-1} to accommodate space-based radiometric shortwave and outgoing

longwave measurements of flux at top-of-atmosphere (TOA).

The F07 parameterization has been experimentally validated by Baran et al.

(2011b) and Furtado et al. (2015). In Baran et al. (2011b) the moment estimated PSD

was found to fit well to several cases of averaged in-situ measured tropical PSDs. For

several cases of midlatitude cirrus Furtado et al. (2015) compared the F07 moments to

in-situ measured moments, whilst ignoring particles less than 100 μm in size, due to

the current uncertainties in measuring the size of small ice at D < 100 μm, and found

good correlations between the parameterization and measurements for all cases

considered. However, poor correlations emerged in that study when the moments

predicted by the Houze et al. (1979) parameterization were compared against the in-

situ derived moments. The study of Furtado et al. (2015) emphasizes that the F07

parameterization is a better representation of the ice PSD to apply to climate models

in general than the Houze et al. (1979) parameterization. This last statement is

especially true in the TTL, given the above description of the Houze et al. (1979)

parameterization.

Given that the F07 PSDs are related to a model prognostic variable (i.e. the mass

carrying moment M_2) and this varies as a function of T_c, given that the ensemble model

single-scattering properties have been integrated over these PSDs, the bulk ice optical

properties can also be directly related to the climate model prognostic variable IWC (i.e.

$m(D)=$constant $\times D^2$, where m is the mass in units of kg) and T_c or just IWC (as is the

case in B014b). The behavior of the 20662 bulk ice optical properties, ω_0 and g, in M_2–T_c

space, is shown in Figs. 1a and 1b, respectively, at a wavelength of 1.575 μm. This

wavelength is chosen as an example to show the variation of the bulk ice optical

properties in the full space used for the later parameterizations. In Fig. 1a, it is shown that

ω_0 varies between the values of 0.7 and 1.0, at the coldest temperature values, down to

about -80°C and $M_2\sim10^{-5}$ m^{-1}, and ω_0 is near unity. At these values of M_2 and T_c, the PSD

is very narrow and will be largely composed of small ice crystals with much fewer

1 occurring large ice crystals; therefore at this wavelength the smaller ice crystals will

2 efficiently scatter incident radiation. At much larger values of M_2 and at much warmer

3 temperatures, at 0.01 m^{-1} and -15°C, respectively, the value of ω_0 decreases to a value of

4 about 0.8. At such M_2 and T_c values, the PSD becomes much broader than previously,

5 with much more frequently occurring large ice crystals, which at this wavelength will

6 absorb incident radiation, thereby decreasing ω_0. The converse behavior is shown, at the

7 same values of M_2 and T_c, for g in Fig. 1b, where g has the corresponding values of about

8 0.78 and 0.88. The reasons for these values are the same as those given for the behavior

9 of ω_0. Figures 1a–1b show that the spatial distribution of ω_0 and g is physically to

10 expectation and would be a similar distribution if the optical properties were plotted as a

11 function of some characteristic size. Here, we demonstrate this using the characteristic

12 size usually assumed in radiation schemes in climate models, which is the mean effective

13 dimension, D_{eff}, defined after Foot (1988) as:

14
$$D_{eff} = \frac{mass_t}{\rho A_t} \qquad (1)$$

15 where in Eq. (1) $mass_t$ and A_t are the total mass and orientation-averaged projected area

16 of the PSD, respectively, and ρ is the density of solid ice. Here, we assume that ρ=1000

17 kg m^{-3} to keep units in Eq. (1) consistent, hence the units of $mass_t$ and A_t being in SI.

18 Firstly, we show that the moment M_2 can easily be related to D_{eff}, as shown in Fig. 2,

19 where in Fig. 2, as an example, we assume that the $mass_t$ and A_t are computed from the

20 first member of the ensemble model, which is the hexagonal ice column of AR=1.0. As

21 can be seen from Fig. 2, the 2nd moment or, equivalently, IWC (by assuming some mass–

22 D relationship) could easily be related to D_{eff} as a function of T_c or just by relating IWC

1 directly to D_{eff} by using some fitting procedure. Indeed, this latter approach was used by

2 McFarquhar et al. (2003), who parameterized IWC explicitly as a function of an effective

3 radius (D_{eff} can be related to the effective radius, r_{eff}, by $r_{eff}=(3/4)\times D_{eff}$). Therefore, the

4 bulk ice optical properties can also be easily parameterized as a function of M_2 or IWC

5 and T_c, as is done in B014b (i.e. IWC alone) and in this paper (i.e. IWC and T_C). We

6 note that, for aggregating ice crystals both mass and diameter are proportional to D^2, so

7 D_{eff} becomes independent of IWC. A further characteristic size could also be defined,

8 such as the ratio between the 3rd and 2nd moments of the PSD. If the 2nd moment is the

9 mass carrying moment M_2, this characteristic size is the mean mass-weighted size, D_{mmw}.

10 The relationship between D_{eff} and D_{mmw} is characterized by Figs. 3a–3b, respectively,

11 which show the variation of ω_0 at a wavelength of 1.575 µm as a function of the

12 characteristic sizes and T_c for all 20662 F07 PSDs. In the case of D_{eff}, in the figures, the

13 same definitions are used as above. The figure shows that D_{eff} is simply some multiple of

14 D_{mmw} and the spatial distribution of ω_0 in the spaces of characteristic size—T_c is exactly

15 the same. Furthermore, the distribution of ω_0 shown in Figs. 3a–3b is relatable to Fig.

16 1a. That is, at the same T_c values of -80ºC and -15ºC, small and large characteristic

17 sizes can be chosen to give the same values of ω_0 for the same values of M_2 assumed

18 above. The above figures illustrate that there is a choice to be made as to how the bulk

19 ice optical properties are parameterized in climate models.

20   As is done in B014b and in this paper, we avoid relating the bulk ice optical

21 properties to D_{eff} as is traditionally done. Instead, our choice is to relate the optical

22 properties directly to climate model prognostic variables such as M_2/IWC. This is because

23 in climate models, D_{eff} is generally diagnosed in the radiation scheme and the D_{eff} in the

radiation scheme is different from the D_{eff} in the cloud physics scheme of a climate model

because different PSDs are usually assumed. In the approach adopted by B014b and in

this paper, we ensure that the PSDs generated through the F07 parameterization in the

cloud physics scheme in the climate model are the *same* as those used in the radiation

scheme, thus providing internal physical consistency within the climate model. In the

traditional approach, this physical internal consistency is generally currently lost. Internal

physical consistency could be satisfied using the traditional approach if D_{eff} were

determined from the PSDs within the cloud physics scheme of the climate model and

these values passed to the radiation scheme. In this way, the effective size then becomes

consistent between the two schemes. However, this recovery of physical consistency

requires an extra step within the climate model. Here, we prefer to avoid such an

unnecessary step. It should also be noted that from Eq. (1), the integral over the mass

requires some mass–D relationship to be applied. However, this mass–D relationship will

obviously change depending on the choice of habit models; as a consequence, this has the

potential to change the spatial distribution of ω_0 shown in Fig. 3a. However, in the

approach adopted here, the mass of ice predicted by the climate model cannot change

and, thus, will always be the same mass of ice between the cloud physics and radiation

schemes.

In this paper, to generate the PSDs, the F07 moments are generated while assuming

the recommended Furtado et al. (2015) mass–dimensional pre-factor and exponent values

of 0.0257 and 2.0, respectively, which were derived by Cotton et al. (2013), and by using

the 20662 IWC estimates and in-cloud temperature measurements compiled by B014a.

Note that this mass–dimensional relationship is the same as that assumed by Hardiman et

al. (2015), and was used by Vidot et al. (2015) to find the optimal ensemble model optical

property parameterization that best simulated globally measured infrared radiometric

brightness temperatures. Furthermore, in this paper, the weights assigned to each of the

ensemble members at each F07 PSD bin size are the same as those assumed in

experiment 4 of B014b (i.e. Eq. (9) in that paper), which were 0.50, 0.20 and 0.30,

respectively. This assignment of weights to the ensemble model is different from that

found by Vidot et al. (2015) to achieve radiometric equivalence between the model and

measurements. However, experiment 4 of B014b gave the best comparisons between the

climate model runs and space-based shortwave and longwave radiation measurements. In

contrast, the Vidot et al. (2015) analysis is based on measurements obtained at three

wavelengths in the infrared. It is yet to be seen whether the weightings found in that

paper would remain the same if more solar and infrared wavelengths were to be utilized.

This will be the subject of a future paper; thus, we assume the same weightings as thosed

used in experiment 4 of B014b.

In the MetUM configuration of models, atmospheric particulates such as aerosol, ice

and water clouds are represented by vertical profiles of their mixing ratios with respect to

air. In this paper and in B014b, the IWC becomes the ice mass mixing ratio, q_i, that is, the

ratio between ice mass per unit volume and the mass of cloudy air per unit volume, and is

in units of kg kg^{-1}. Likewise, the bulk optical properties, the volume extinction, and

scattering coefficients become the mass extinction, K_{ext}, and mass scattering coefficients,

K_{sca}, and both are in units of m^2 kg^{-1} (i.e. the extinction and scattering coefficients per

unit mass of cloudy air).

In this paper, the bulk optical property database is first divided into the six shortwave

1 and nine longwave Edwards–Slingo (1996, hereafter referred to as ES96) bands; these

2 bands are defined in Table 1. In each of the ES96 bands, a total of about 10000 q_i and T_c

3 values were randomly selected from the bulk optical property database of B014a.

4 Selected values of q_i and T_c were between 1.0×10^{-8} and 0.004 kg kg^{-1} and -80°C and

5 0°C, respectively. This randomly selected range in q_i–T_c space is sufficient to capture the

6 full range that might be generated in an atmospheric model. In each of the ES96 bands,

7 the bulk optical properties were parameterized as nonlinear and linear functions,

8 dependent on q_i and T_c, by an iterative minimization procedure. That is, the forms of the

9 parameterizations were first assumed and then the coefficients, for each of the

10 parameterizations, were estimated by iterating through possible coefficient values. This

11 was done until differences between the parameterizations and randomly selected 10000

12 bulk optical properties were within acceptable experimental limits (i.e. estimated K_{ext} and

13 K_{sca} values must be within ±50% of their true values for > 90% of all possible q_i–T_c

14 values). The error of ±50% in the mass coefficients is based on likely in-situ errors in

15 extinction estimates previously discussed in Baran et al. (2009). The errors resulting from

16 this fitting procedure are discussed further below. The above fitting procedure resulted in

17 the following best-fit bulk optical property parameterizations of cirrus:

18 $$K_{ext}(\lambda,q_i,T_c) = a_\lambda (q_i/T_c^4) \qquad (2)$$

19 $$\omega_0(\lambda,q_i,T_c) = b_\lambda + c_\lambda q_i T_c \qquad (3)$$

20 $$g(\lambda,q_i,T_c) = d_\lambda + e_\lambda q_i T_c \qquad (4)$$

21 where the temperature, T_c, is in units of Kelvin. The ES96 estimated band-dependent

22 coefficients a_λ, b_λ, c_λ, d_λ and e_λ are listed in Table 1. It should be noted that to obtain

23 the correct asymptotic behavior for $\omega_0(\lambda,q_i,T_c)$ and $g(\lambda,q_i,T_c)$, for the cases where $q_i >$

1 10^{-3} kg kg^{-1}, the values of ω_0 and g should assume the same values as ω_0 and g when

2 $q_i = 10^{-3}$ kg kg^{-1}. If this condition is applied, ω_0 and g should never attain unphysical

3 values. In B014b the above bulk optical properties are expressed as functions of q_i

4 only (i.e. Eqs. 4–7 in that paper). This is possible to do, as shown by Fig. 2, and is

5 equivalent to the parameterization proposed by McFarquhar et al. (2003). In that

6 paper, as previously stated, the IWC is explicitly derived as a function of r_{eff}; in turn,

7 the bulk optical properties are derived as a function of r_{eff}. Thus, r_{eff} can be eliminated

8 between relationships to leave the bulk optical properties expressed as a function of

9 IWC only, which is equivalent to B014b.

10 The difference between the above parameterization and that of B014b is

11 highlighted by the following example. If we assume that $T_c = 190$ K and $q_i = 1.0 \times 10^{-}$

12 ^{3} kg kg^{-1}, Eq. (3) at ES96 shortwave band 5 (1.19–2.38 µm) gives $\omega_0 = 0.9015$, whilst

13 Eq. (6) from B014b gives $\omega_0 = 0.8663$. The former calculation is about 5% greater

14 than the latter calculation, which means that in the former case the cirrus is about

15 27% less absorbing (i.e., $\sim 1 - \omega_0$) than in the latter case. With such a difference in

16 shortwave absorption between the two parameterizations, the B014b parameterization

17 is clearly more likely to result in an increase in TTL temperature than Eq. (3).

18 In the introduction to this paper, it was noted that trigonal ice crystals were

19 observed by a number of studies in the TTL. Single-scattering calculations based on

20 trigonal ice crystals using the anomalous diffraction approximation (ADT) have been

21 reported by Murray et al. (2015). These calculations show that ω_0, computed

22 assuming trigonal columns can be as much as 20% higher than their equivalent

23 hexagonal column counterparts for a range of crystal sizes they considered at an

absorbing wavelength. If the TTL were composed mostly of trigonal columns, then

this would imply less solar absorption and, as a consequence, less in-cloud heating,

due to generally larger ω_0 values, relative to Eq. (3). However, ADT is a soft particle

approximation (i.e. assumes real refractive indices near unity), originally due to van

de Hulst (1957), and so by using this approximation, ω_0 values presented in Murray et

al. (2015) may be overestimated (due to the neglect of reflection; refraction and

particle edge effects, which all tend to increase absorption, see for instance, Mitchell

et al. 2006). The latter limitations of ADT were noted by Murray et al. (2015), who

also called for more accurate computations of the single-scattering properties of

trigonal particles. On the other hand, if the TTL were composed of quasi-spherical

particles as reported in some studies cited in the introduction to this paper, the

calculated ω_0 values of these particles would tend to be lower (due to geometrical

considerations and edge effects, see Baran and Havemann 1999; Mitchell et al. 2006;

Bi and Yang, 2014) than that calculated for the equivalent trigonal particles. This

implies more absorption, and so, greater in-cloud heating in the TTL, assuming equal

microphysics assumptions. This range in potential TTL in-cloud heating is indicative

of the current uncertainties in the microphysics composition within the TTL.

Reducing uncertainty in calculated ω_0 values requires observations of PSDs, ice

particle shapes, and application of electromagnetic methods and not gross

approximations such as ADT to observed TTL microphysics measurements.

The accuracy of the new parameterizations was tested by selecting an independent

set of about 10000 q_i and T_c values taken from the ice optical property database of

B014a. As before, the bulk optical properties, as a function of q_i and T_c, are grouped

1   into their ES96 bands. The test of accuracy of the new parameterizations is based on

2   the relative percent error, ε(λ), which given by:

3    $$\varepsilon_\lambda = \frac{\text{true}_\lambda - \text{estimated}_\lambda}{\text{true}_\lambda} \times 100\%$$ (5)

4   where in Eq. (5) true$_\lambda$ and estimated$_\lambda$ are the actual bulk optical properties in the

5   B014b database consisting of 2.986×10^6 values (i.e. 20662 q_i–T_c values $\times$ 145

6   wavelengths – 10000 randomly selected values) and the estimated values using Eqs.

7   (2–4), respectively. Here, the accuracy of the parameterizations is illustrated using

8   only ES96 shortwave band 5 (1.19–2.38 μm), as all other bands have similar

9   accuracies, and this band is important for the shortwave heating of cirrus in the TTL.

10   The calculated normalized PDFs of ε(λ) are shown for $K_{ext}(\lambda,q_i,T_c)$, $K_{sca}(\lambda,q_i,T_c)$ and

11   g in Figs. 4a–c, respectively. Figs. 4a and b show that ε(λ) in the mass

12   parameterizations is within ±50% for about 90% and 94% of the independently

13   selected database, respectively. Typically, the in-situ measurement error in

14   $K_{ext}(\lambda,q_i,T_c)$ is usually ±50% (Baran et al. 2009), so the relative error distribution

15   shown in Figs. 4a–b is acceptable. Fig. 4c shows ε(λ) for g and, as can be seen from

16   the figure, ε(λ) is within ±2.5% for about 83% of the database, which is also

17   acceptable. Theoretical and in-situ uncertainty in the asymmetry parameter value is

18   far greater than the error in the g parameterization (Ulanowski et al. 2006; Fu 2007;

19   Garrett 2008; Baran 2012; van Diedenhoven et al. 2014). We compare our

20   parameterization of g to the g parameterization developed by Fu (2007) by assuming

21   q_i and T_c values of 1.0×10^{-4} kg kg^{-1} and 190 K, respectively. In Fu (2007), g is

22   parameterized in the shortwave by assuming hexagonal columns and hexagonal plates

1 as a function of an effective AR by using either rough or smooth collections of

2 particles. The range in the effective aspect ratio given by Fu (2007) represents the

3 aspect ratios of monomer ice crystals that make up more complex ice crystals. Indeed,

4 the effective AR of the ensemble model members assumed in this paper are 1.0, 0.42

5 and 0.42 (the first being the hexagonal ice column of AR=1.0, and the latter two

6 being the AR and averaged AR values found for the six-branched bullet rosette and

7 the three monomer hexagonal ice aggregate, respectively), and the following weights

8 of 0.50, 0.20 and 0.30 are assigned to the three ensemble members, respectively. The

9 comparison is made by using the coefficients d_λ and e_λ tabulated in Table 1 at ES96

10 shortwave band 1 (i.e. 0.20–0.32 µm) and at ES96 shortwave band 3 (0.32–0.69 µm).

11 These two shortwave bands cover the wavelength range given in Fu (2007), for

12 shortwave band 1 (i.e. 0.25–0.70 µm) given in that paper. Although the comparison is

13 not exact in terms of the wavelength range and assumed ice microphysics, it is

14 considered sufficiently accurate for the purposes of this paper. Applying the above

15 three effective AR ratios for each of the ensemble models to Eqs. (3.2 and 2.2) given

16 in Fu (2007), and weighting the calculated asymmetry parameter values by the three

17 weights given above, we find a weighted value of 0.765 for g (i.e.

18 0.5×0.73+0.20×0.80+0.3×0.80). This Fu (2007) asymmetry parameter value

19 compares to the values of 0.757 and 0.787 found for ES96 shortwave bands 1 and 3,

20 respectively, and the average of these two values is 0.772. The averaged value is

21 within about 1% of the Fu (2007) calculation, and the values calculated at the two

22 ES96 shortwave bands are within about ±2% of Fu (2007). If we take g=0.765 and

23 g=0.787 (i.e. the most extreme difference) and assume that the cirrus is located over a

1   dark ocean and conservative scattering, then the backward solar reflection is about

2   23.5 and 21.3%, respectively, where backward reflection ~ (1.-g). The difference in

3   reflected shortwave flux is at most about 7 Wm^{-2}, assuming an area-averaged incident

4   solar flux of 330 Wm^{-2}, at least for the case considered here. These differences found

5   for the g parameterizations are far less than the range in g found by the following

6   studies (Ulanowski et al. 2006; Fu 2007; Garrett 2008; Baran 2012; van Diedenhoven

7   et al. 2014, Yang et al. 2015). Indeed, in the case of Ulanowski et al. (2006),

8   experimentally derived g values were found to vary between 0.80±0.04 and 0.63±0.05

9   for smooth and rough ice analog rosettes, respectively, and this difference results in a

10   shortwave flux uncertainty of about -56 Wm^{-2}. Furthermore, the calculated

11   asymmetry parameter values using the two parameterizations compare well against

12   radiometrically derived asymmetry parameter values using POLDER observations

13   from van Diedenhoven et al. (2014). The observations from POLDER were located

14   over the north coast of Australia. In that paper, at a T_c value of about -85°C, the

15   asymmetry parameter values are shown to vary between about 0.74±0.02 and

16   0.79±0.04, which encompass the values of g, derived using the two completely

17   different parameterizations. These experimental results obtained at 0.865 μm, were

18   roughly coincident with the three assumed shortwave bands used in the comparisons,

19   and the imaginary index of ice is very weakly absorbing at all of the chosen

20   shortwave bands as shown in B014b. At least at TTL temperatures, the parameterized

21   g values derived in this paper appear representative of other independent derivations

22   of g. However, g is one of the bulk ice optical properties that is important to constrain

23   in climate models, as noted by Stephens et al. (1990). In this paper, we are concerned

1   about TTL heating and specific humidity errors in a climate model, and these errors

2   are more associated with the parameterizations found for $K_{ext}(\lambda,q_i,T_c)$ and $\omega_0(\lambda,q_i,T_c)$.

3   Eqs. (2) and (3) are now compared against the equivalent parameterizations

4   developed by B014b. The parameterizations of g are not compared here as the results are

5   not sufficiently different. In comparing the parameterizations a constant value of q_i is

6   assumed, with its value being 1.0×10^{-5} kg kg^{-1}, whilst the temperature is allowed to vary

7   between -80°C and 0°C. The comparisons are shown in Figs. 5a–c at ES96 shortwave

8   band 5 for $K_{ext}(\lambda,q_i,T_c)$, the co-albedo (i.e., 1.- $\omega_0(\lambda,q_i,T_c)$), and (c) $K_{abs}(\lambda,q_i,T_c)$ (i.e.,

9   $K_{abs}(\lambda,q_i,T_c)= K_{ext}(\lambda,q_i,T_c)- K_{sca}(\lambda,q_i,T_c)$), respectively. Other bands show generally

10 similar results to Figs. 5a–c and are not shown here for reasons of brevity. Fig. 5a shows

11 that at T_c values of about -80°C, the nonlinear parameterization of $K_{ext}(\lambda,q_i,T_c)$ is about a

12 factor of 2.5 greater than that predicted by B014b. This means that at typical TTL

13 temperatures, the new parameterization, relative to B014b, will transmit less longwave

14 terrestrial radiation to space through the cirrus, which will result in less longwave

15 absorption by trace gases above the TTL cirrus, consequently lowering TTL temperatures

16 through emission at cold temperatures. Also critical to the TTL temperature is the co-

17 albedo. The co-albedo comparisons are shown in Fig. 5b; again, the figure shows that at

18 T_c = -80°C, the new parameterization co-albedo is less than B014b by almost a factor of

19 7. This change in absorption between the parameterizations is shown clearly in Fig. 5c,

20 which shows $K_{abs}(\lambda,q_i,T_c)$, and at T_c = -80°C, the new parameterization is almost a factor

21 3 times less absorbing than B014b. The comparisons show that the temperature-

22 dependent parameterization in the TTL should result in less cirrus heating relative to

23 B014b. The next section presents the impact of these different heating profiles on the

1 simulation of the TTL in an atmosphere-only climate integration using the MetUM.

2 **3. The impact of the parameterizations on the simulation of the TTL**

3 To assess the fidelity of the TTL simulation in models using the B014b parametrization

4 and the parametrization described in section 2, we perform a pair of 20-year atmosphere-

5 only climate simulations using each parametrisation. Apart from the formulation of the

6 ice cloud optical properties, these simulations each use an identical baseline of the Global

7 Atmosphere 6.0 (GA6.0) configuration of the MetUM. GA6.0 is described by Walters et

8 al. (2015), so a description is not repeated here. The simulations are performed at a

9 horizontal resolution of N96 (~135 km in the mid-latitudes) and use a vertical level set

10 with spacings of between 500 and 700 m in the TTL region with a model "lid" at 85 km

11 from the surface. The simulations run from December 1988 to November 2008 and use

12 prescribed (but time-varying) sea-surface temperatures, greenhouse gas concentrations,

13 and aerosol emissions while roughly following the protocol of the Atmospheric Model

14 Intercomparison Project (AMIP, Taylor et al. 2012). Results are presented for the

15 meteorological season December–January–February (DJF), as this season represents the

16 period during which cirrus occurrence in the tropics is at a maximum (Sassen et al. 2008).

17 The climate model predictions are compared against the ERA-Interim reanalysis

18 temperature product (Dee et al. 2011) and the Modern-ERA Retrospective analysis for

19 Research and Applications (MERRA) specific humidity product (Rienecker et al. 2011).

20 The impacts of the parameterizations on the 20-year averaged DJF cloudy shortwave and

21 longwave radiative effects at TOA are compared against the Loeb et al. (2009) reanalysis

22 of the Clouds and the Earth's Radiant Energy System (CERES) product.

1   Firstly, the DJF zonally averaged temperature differences between the B014b

2   parameterization and the ERA-Interim reanalysis are shown in Fig. 6a, whilst the same

3   differences are shown in Fig. 6b but for the new parameterizations. It is clear from Fig.

4   6b, relative to Fig. 6a, that the new parameterizations have reduced the TTL temperature

5   by about 1 K, and generally throughout the tropics, which is consistent with the

6   discussion surrounding Figs. 5a and b. In addition, the new parameterization has also

7   removed the warming in the southern sub-tropical troposphere region by about 1–2 K,

8   and reduced cooling and warming over the South and North Poles, respectively. On the

9   negative side, the new parameterizations lead to a cooling of the tropical troposphere by

10   about 1 K, and to a similar cooling at altitudes between about 15 and 30 hPa, which

11   occurs near the equator.

12   The impact of the new parameterizations on the model bias of zonally averaged

13   $\log_{10}$ (specific humidity), relative to MERRA, is shown in Fig. 6d. The figures show that

14   the impact of the new parameterizations on the $\log_{10}$ (specific humidity) model bias in the

15   TTL is to reduce it, and its distribution throughout the TTL, especially around the

16   equatorial region. Relative to the B014b parameterization, shown in Fig. 6c, the new

17   parameterization reduces the $\log_{10}$ (specific humidity) model bias in the TTL by about 0.1

18   $\log_{10}$ (kg kg^{-1}) and generally reduces the extent of this bias in the sub-tropics. For each

19   panel shown in Figs. 6a–d, the grid point root mean square errors (RMS) were calculated

20   over the region between 20°S and 20°N, and between 150 and 70 hPa. The resulting RMS

21   errors were found to be 2.52, 1.90 K, and 0.13 and 0.12 $\log_{10}$ (kg kg^{-1}), respectively.

22   Therefore, in the TTL region, the new parameterization reduces the zonally averaged

23   temperature and specific humidity biases in the model.

Finally, to show that the new parameterizations do not result in any detriment to the

climate model, in terms of the cloud radiative effect at TOA and global means. Results

are presented for the model's predicted radiative effects in Figs. 7a–d and global means

in Table 2. The figures show that the new parameterization improves the shortwave and

longwave cloud radiative effects in the climate model, relative to B014b. The extent of

the shortwave bias in the model is significantly reduced, as shown by the reduction in the

area-weighted RMS error by 1.08 Wm^{-2}, and this improvement is especially evident in the

tropics. Note also the reduction in bias brought about by the new parameterization

throughout the Southern Ocean. The longwave biases in the climate model are also

reduced by the new parameterizations as shown in Figs. 7c and 7d, where it can be seen

that the area-averaged RMS error is reduced by 0.41 Wm^{-2}. The significant longwave

negative biases around the warm pool shown in Fig. 7c have been reduced by the new

parameterizations by up to about 20 Wm^{-2}, as demonstrated by Fig. 7d.

Table 2 shows a comparison between the Stephens et al. (2012) estimated CERES

global means for seven variables together with their estimated standard deviation $\pm\sigma$, and

the B014b and temperature-dependent parameterizations. The table shows that the

temperature-dependent parameterization is within the estimated uncertainty for six out of

seven of the global mean variables shown in table 2. This improves on the B014b

parameterization, which has four out of seven variables within the estimated uncertainty.

In particular, the B014b parameterization significantly underestimates the reflected

shortwave flux at TOA. As a result of this underestimation, the predicted shortwave

radiative effect is too low relative to the CERES estimated mean. The temperature-

dependent parameterization does predict adequate reflected shortwave flux at TOA, but

the prediction of the shortwave radiative effect is just over 1σ from the CERES estimated

mean. This compares to about $1\frac{3}{4}\sigma$ from the estimated mean found for the B014b

parameterization. The reason for this discrepancy between the parameterizations and the

CERES observations for this variable is probably due to, in the case of B014b; the mass

extinction coefficient being underestimated at about temperatures $< -40^{\circ}C$, as can be seen

from Fig. 5a, relative to the temperature-dependent parameterization. In the case of the

temperature-dependent parameterization, the physical reasons for this underestimation

could be due to: (i) There is too little ice mass being predicted by the model cloud scheme

and/or (ii) the model asymmetry parameter is too large. It is yet to be seen which of these

reasons might account for the discrepancy in the shortwave radiative effect. However, in

general, the new parameterization presented within this paper improves the model

performance, relative to B014b, in terms of the shortwave and longwave cloudy radiative

effect as can be seen from Figs. 7b–d, but also the predictions of model global mean

fluxes.

4. Conclusions

A cirrus bulk optical property parameterization has been presented, and it has been

demonstrated that the parameterization reduces zonally averaged temperature biases in

the TTL of GA 6.0 by about 1–2 K relative to the B014b parameterizations. The

parameterization of the asymmetry parameter was compared against an independent

parameterization and was shown to be within about 1% and ±2% of the latter

parameterization at ES96 short wavebands 1 and 2, respectively. Moreover, the

asymmetry parameters predicted by both parameterizations were shown to encompass

space-based estimations of g from observations from around the north coast of Australia

1. at TTL cirrus temperatures of -85°C. The reason for this improvement in climate model

2. performance is through coupling the bulk optical properties to q_i and T_c. At the low

3. temperatures in the TTL, the B014b parameterization will under-predict the single-

4. scattering albedo, resulting in TTL warming due, in part, to the absorption of shortwave

5. radiation, highlighting the importance of wavelengths in the near-infrared. The new

6. temperature-dependent parameterization also improves, relative to B014b, on

7. representing the model's prediction of the shortwave and longwave cloudy radiative

8. effect as well as global flux means. To improve climate model representations of the

9. TTL, more careful consideration should be given to the calculation of ice optical

10. properties, especially the mass extinction coefficients and single-scattering albedo, which

11. are the bulk ice optical properties that principally determine the temperature and specific

12. humidity distributions in our simulations of TTL cirrus. Further observations of cirrus

13. PSDs, IWCs, habits (in addition to humidity and temperature measurements), and solar

14. and infrared radiative properties in the TTL should be considered a priority.

15. **Acknowledgements**

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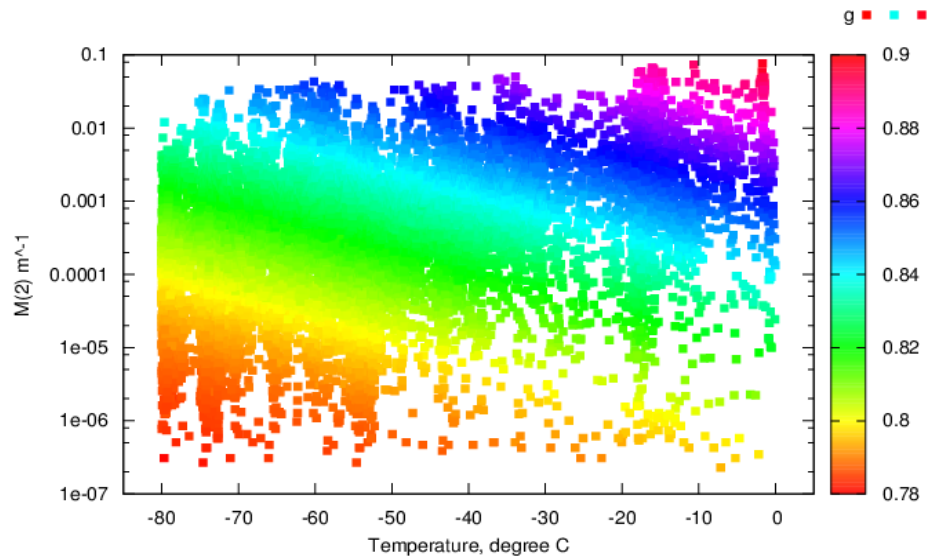
1   Fig. 1. The bulk optical properties (a) ω_0 and (b) g as a function of the mass carrying

2   moment M(2) and temperature at the wavelength of 1.575 µm for all 20662

3   values. The calculated values for ω_0 and g are shown as the color bar on the right-

4   hand side of the figures.

5   Fig. 2. The mass carrying moment M(2) as a function of the mean effective dimension,

6   D_{eff}, and temperature, T_c, for all 20662 values. The key on the right-hand side of

7   the figure is T_c in units of ^oC.

8   Fig. 3. The 20662 calculated values of ω_0 as a function of (a) D_{eff} and (b) M3/M2, the

9   mean mass-weighted size, D_{mmw}, of the PSD. The key on the right-hand side of

10   the figures is the calculated values of ω_0 at the wavelength of 1.575 µm.

11   Fig. 4. The normalized PDFs of the relative percent error in the parameterization of (a)

12        $K_{ext}(\lambda, q_i, T_c)$, (b) $K_{sca}(\lambda, q_i, T_c)$, and (c) $g(\lambda, q_i, T_c)$. Relative percent error results

13   are shown for Edwards and Slingo (1996) shortwave band 5 (1.19–2.38 µm).

14   Fig. 5. Comparing the new parameterization (full line) to the B014b parameterization

15   (dashed line) at Edwards and Slingo (1996) shortwave band 5 (1.19–2.38 µm).

16   Comparisons are shown for (a) $K_{ext}(\lambda, q_i, T_c)$, (b) the co-albedo, and (c) $K_{abs}(\lambda, q_i,$

17        $T_c)$.

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1 Fig. 6. The 20-year DJF zonally averaged temperature and log10 (specific humidity)

2 differences, shown in the top and bottom panels, respectively. The differences are

3 between the MetUM configuration 6.0 run, the ERA-Interim and MERRA

4 products, respectively. In the left column, panels (a) and (c), results are shown

5 while assuming the B014b parameterization. In the right column, panels (b) and

6 (d), results are shown while assuming the new parameterization. The units of

7 temperature difference and log (specific humidity) are K and log10 (kg kg-1),

8 respectively.

9 Fig. 7. The annual 20-year TOA cloud radiative effect differences between MetUM

10 configuration 6.0 and the CERES products. Results are shown for the shortwave

11 while assuming the (a) B014b parameterization and (b) the new parameterization.

12 The longwave results are shown while assuming the (c) B014b parameterization

13 and (d) the new parameterization. The area-averaged root mean square difference

14 is shown in each of the panels, and differences are in units of Wm^{-2}.

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1   (a)
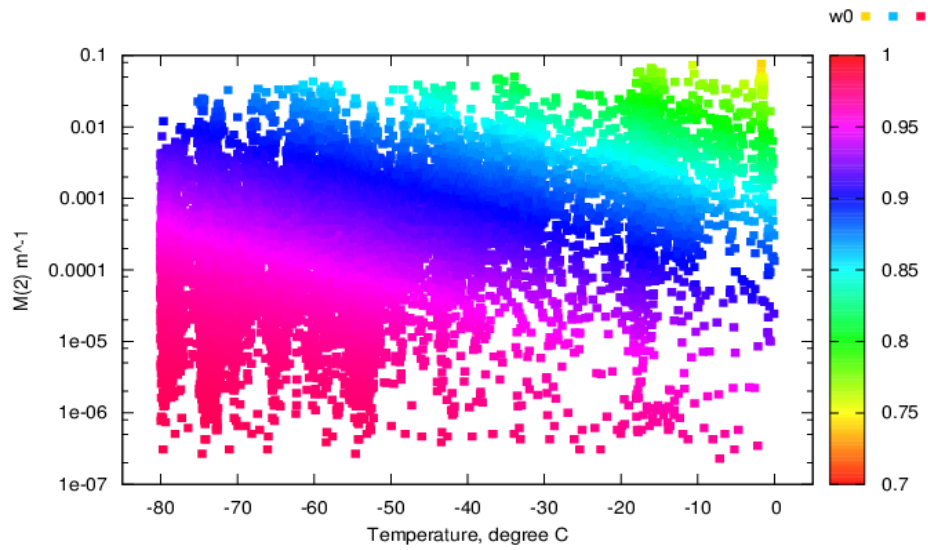
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3   (b)

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5   Fig. 1. The bulk optical properties (a) ω_0 and (b) g as a function of the mass carrying

6   moment M(2) and temperature at the wavelength of 1.575 μm for all 20662

7   values. The calculated values for ω_0 and g are shown as the color bar on the right-

8   hand side of the figures.

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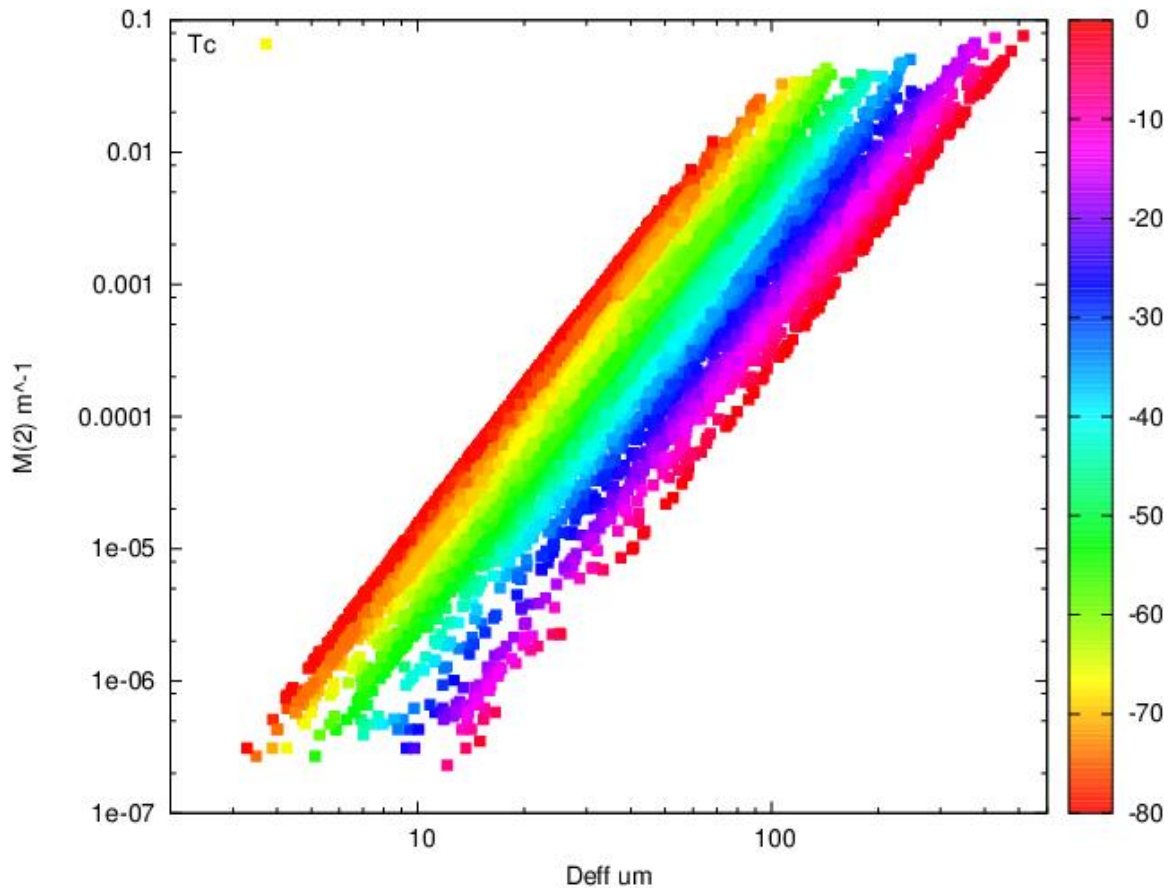
Fig. 2. The mass carrying moment M(2) as a function of the mean effective dimension, D_{eff}, and temperature, T_c, for all 20662 values. The key on the right-hand side of the figure is T_c in units of $^{\circ}C$.

1   (a)
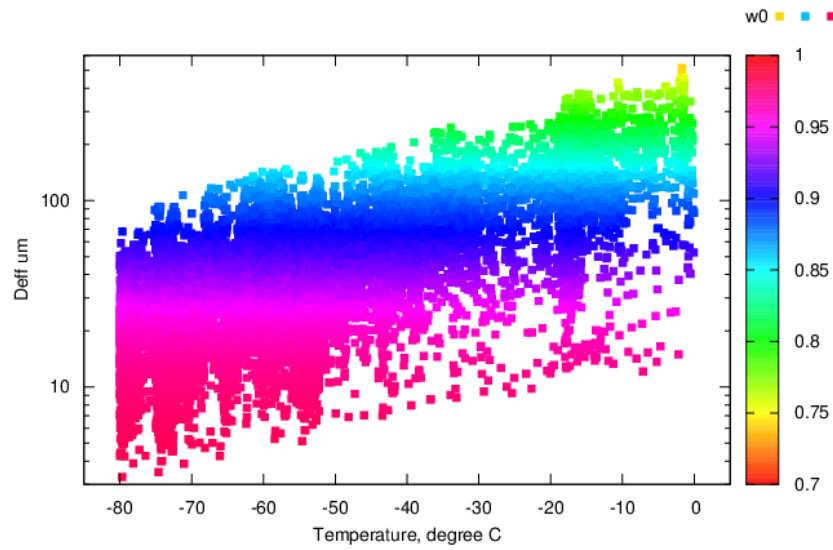
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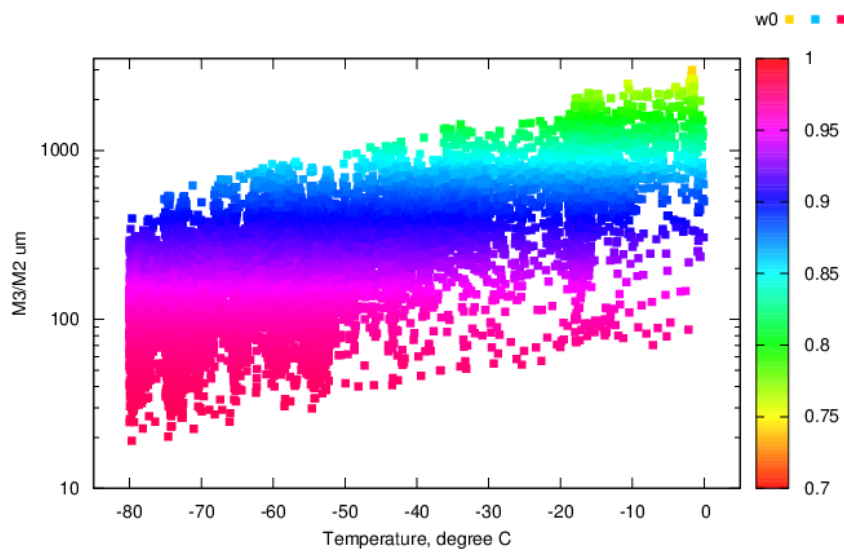
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5   Fig. 3. The 20662 calculated values of ω_0 as a function of (a) D_{eff} and (b) M3/M2, the

6   mean mass-weighted size, D_{mmw}, of the PSD. The key on the right-hand side of

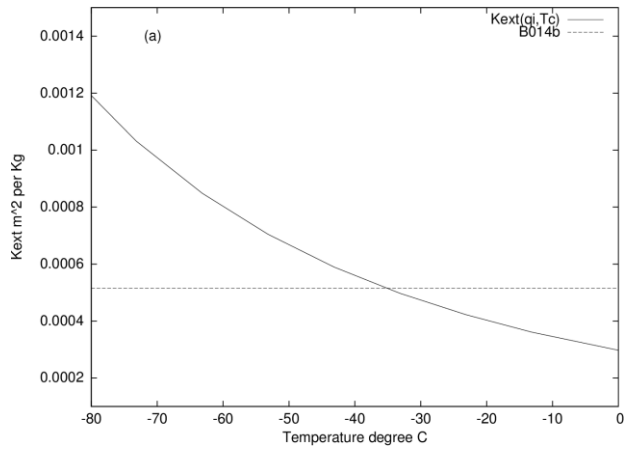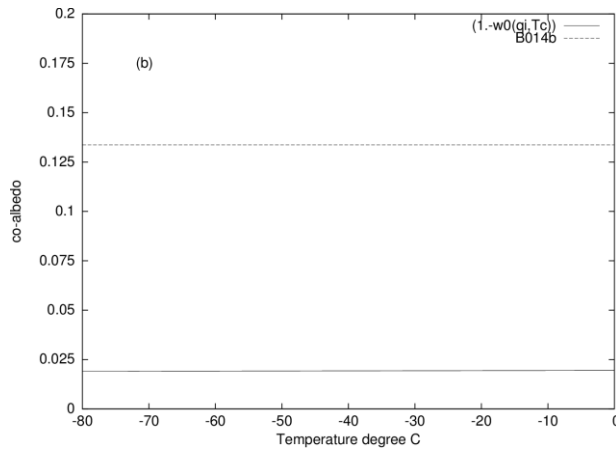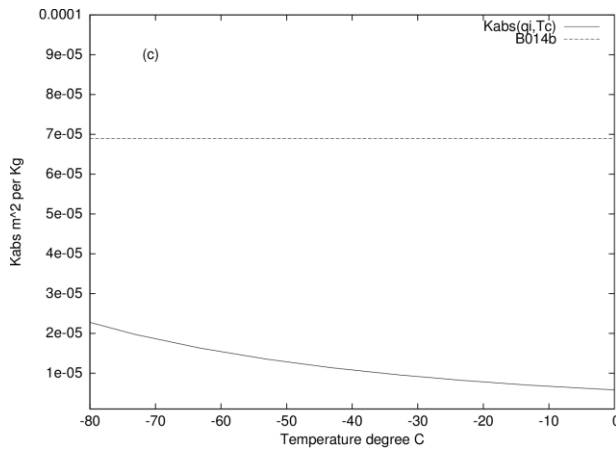7   the figures is the calculated values of ω_0 at the wavelength of 1.575 µm.
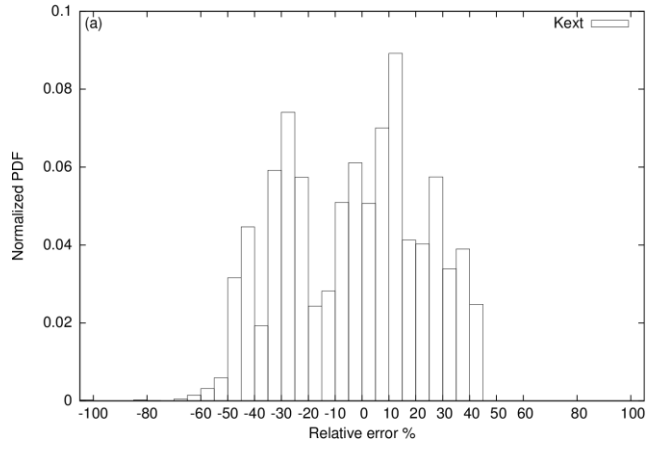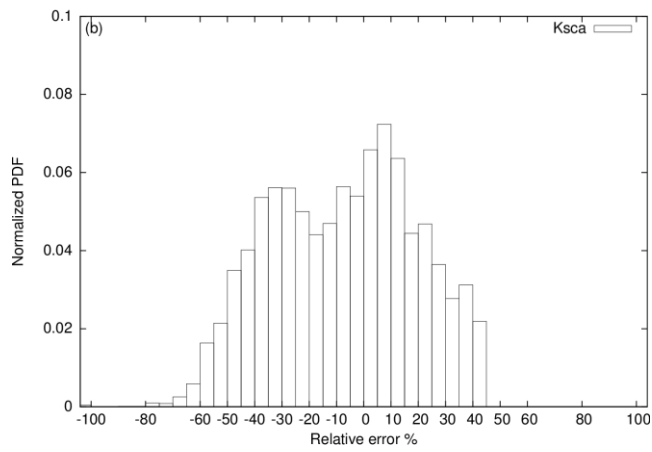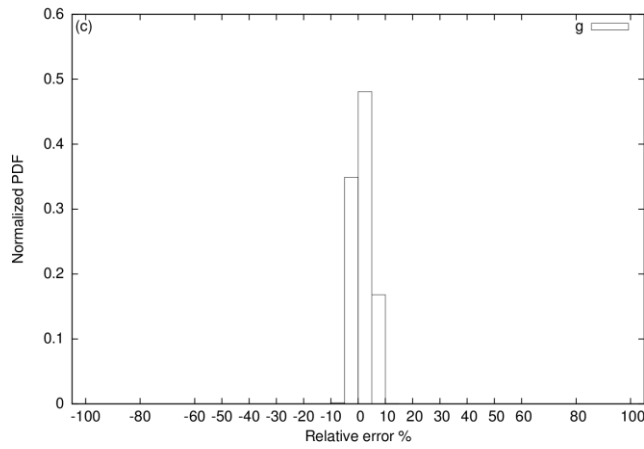
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Fig. 4. The normalized PDFs of the relative percent error in the parameterization of (a) $K_{ext}(\lambda, q_i, T_c)$, (b) $K_{sca}(\lambda, q_i, T_c)$, and (c) $g(\lambda, q_i, T_c)$. Relative percent error results are shown for Edwards and Slingo (1996) shortwave band 5 (1.19–2.38 μm).

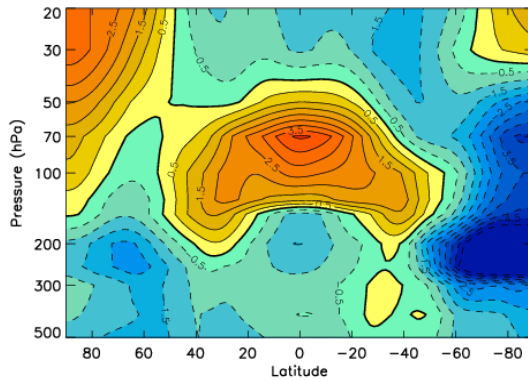Fig. 5. Comparing the new parameterization (full line) to the B014b parameterization

(dashed line) at Edwards and Slingo (1996) shortwave band 5 (1.19–2.38 µm).

Comparisons are shown for (a) $K_{ext}(\lambda, q_i, T_c)$, (b) the co-albedo, $(1.-\omega_0(\lambda, q_i, T_c))$,

and (c) $K_{abs}(\lambda, q_i, T_c)$.

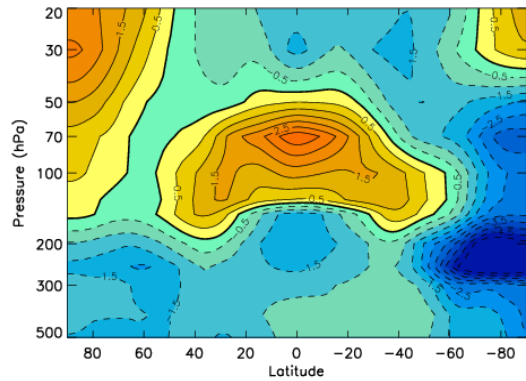1   (a)   (b)

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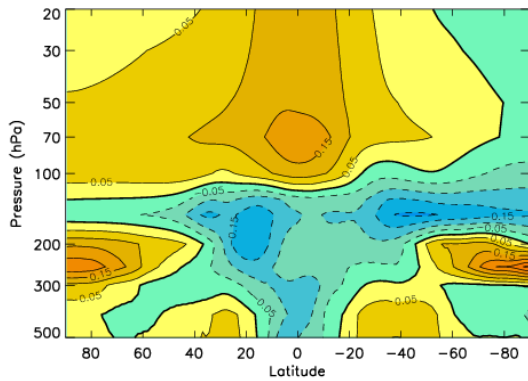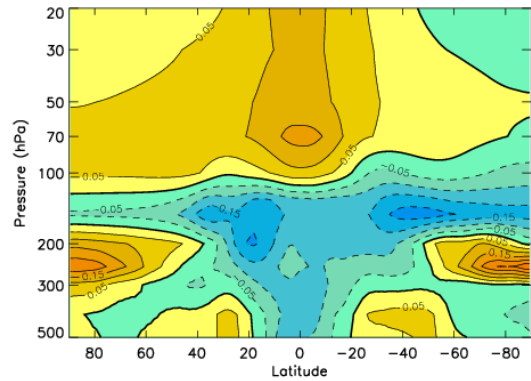3   (c)   (d)

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5   Fig. 6. The 20-year DJF zonally averaged temperature and log10 (specific humidity)

6   differences, shown in the top and bottom panels, respectively. The differences are

7   between the MetUM configuration 6.0 run, the ERA-Interim and MERRA

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9   while assuming the B014b parameterization. In the right column, panels (b) and

10   (d), results are shown while assuming the new parameterization. The units of
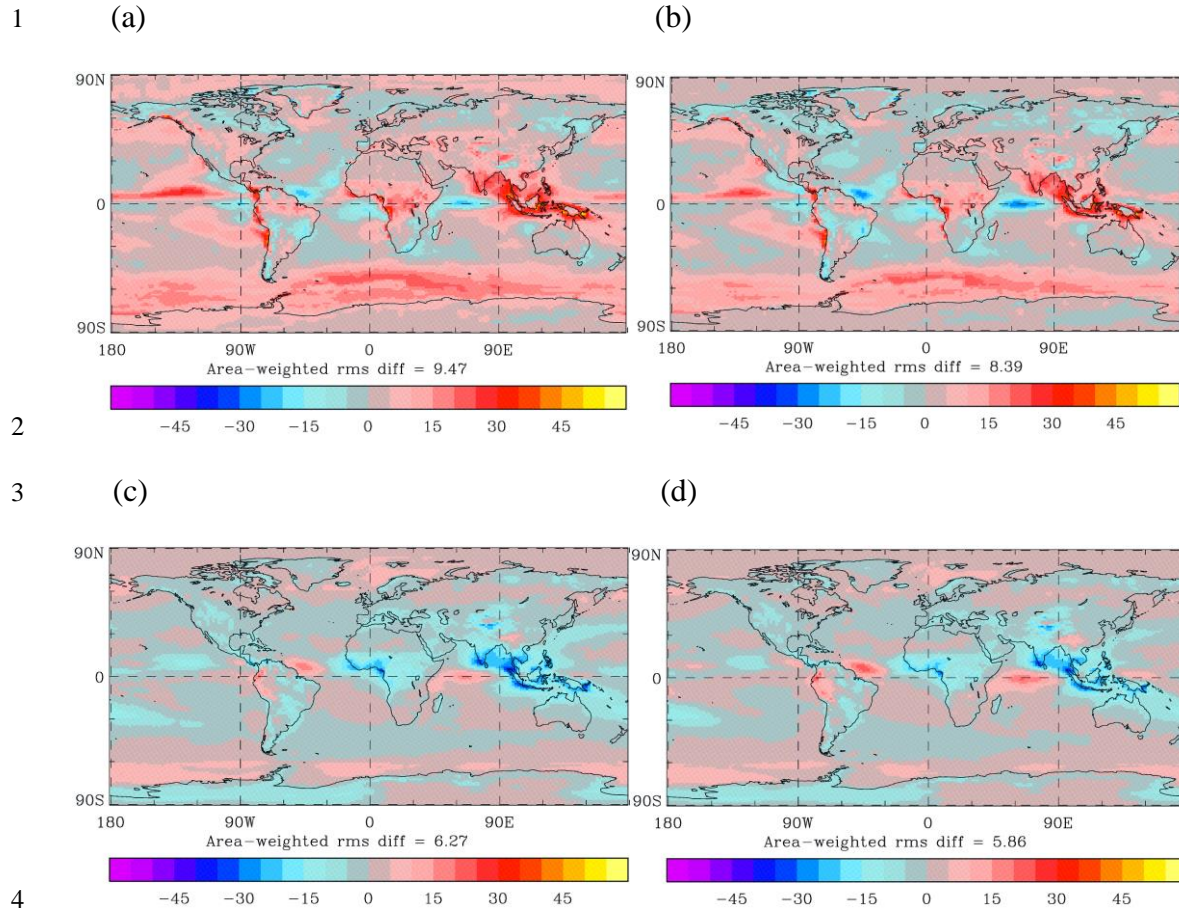
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12   respectively.

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1   (a)   (b)

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5   Fig. 7. The annual 20-year TOA cloud radiative effect differences between MetUM

6   configuration 6.0 and the CERES products. Results are shown for the shortwave

7   while assuming the (a) B014b parameterization and (b) the new parameterization.

8   The longwave results are shown while assuming the (c) B014b parameterization

9   and (d) the new parameterization. The area-averaged root mean square difference

10   is shown in each of the panels, and differences are in units of Wm^{-2}.

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Table 1. The derived values of the band-dependent coefficients for each of the

Edwards and Slingo (1996) shortwave and longwave bands. The first six entries in the

table are the shortwave bands and the following nine entries are the longwave bands.

Band μm	a_λ	b_λ	c_λ	d_λ	e_λ
0.20–0.32	1.64×10^{11}	1.0000	6.5×10^{-15}	0.7560	0.0378
0.32–0.69	1.66×10^{11}	1.0000	-1.4×10^{-6}	0.7804	0.0419
0.32–0.69	1.64×10^{11}	0.9999	-6.4×10^{-5}	0.7860	0.0434
0.69–1.19	1.64×10^{11}	0.9996	-0.0031	0.7897	0.0468
1.19–2.38	1.65×10^{11}	0.9817	-0.4218	0.8208	0.1351
2.38–10.0	1.60×10^{11}	0.7500	-0.2353	0.9130	0.1240
25.0–10^4	1.50×10^{11}	0.6300	-0.2500	0.7129	0.6568
18.18–25.0	1.75×10^{11}	0.7700	-0.2866	0.8356	0.3085
12.50–18.18	1.73×10^{11}	0.5480	0.0108	0.8843	0.1833
13.33–16.95	1.74×10^{11}	0.5469	0.0146	0.8845	0.1730
8.33–12.50	1.44×10^{11}	0.5346	0.0106	0.9338	0.1013
8.93–10.10	1.54×10^{11}	0.6500	-0.1420	0.9401	0.1144
7.52–8.33	1.70×10^{11}	0.6000	-0.1781	0.9264	0.1513
6.67–7.52	1.72×10^{11}	0.6000	-0.1781	0.9331	0.1287
3.34–6.67	1.71×10^{11}	0.6009	-0.1304	0.9080	0.1762

1 Table 2. CERES means obtained from Stephens et al. (2012) compared against the

2 MetUM configuration 6.0 means predicted using the B014b parameterization and the

3 temperature-dependent parameterization. All flux units (SW and LW) are in Wm^{-2}.

4 Asterisks denote that the predicted variable is within the current CERES measurement

5 uncertainty.

6

Variable	Observation	B014b	Temperature-dependent
Outgoing SW	100±2	97.58	99.66*
Outgoing LW	239.7±3.3	240.53*	239.52*
Absorbed SW	240.2±2	242.80	240.73*
Albedo TOA	29.41±1	28.67*	29.28*
SW CF	-47.5±3	-42.18	-44.23
LW CF	26.7±4	23.88*	24.74*
Net surf SW	165±6	168.64*	170.92*

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