

*Are current dynamic water quality models too complex? A comparison of a new parsimonious phosphorus model, SimplyP, and INCA-P*

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1 Are our dynamic water quality models too complex? A comparison of a new parsimonious  
2 phosphorus model, SimplyP, and INCA-P

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8 **Key Points:**

- 9 • We developed a new parsimonious dynamic catchment phosphorus model, SimplyP
- 10 • SimplyP performed as well in calibration, validation and scenarios as a well-established,  
11 substantially more complex model
- 12 • Results support the hypothesis that water quality models are too complex and suggest wider  
13 simplification exercises may be warranted

## 14 Abstract

15 Catchment-scale water quality models are increasingly popular tools for exploring the potential  
16 effects of land management, land use change and climate change on water quality. However, the  
17 dynamic, catchment-scale nutrient models in common usage are complex, with many uncertain  
18 parameters requiring calibration, limiting their usability and robustness. A key question is  
19 whether this complexity is justified. To explore this, we developed a parsimonious phosphorus  
20 model, *SimplyP*, incorporating a rainfall-runoff model and a biogeochemical model able to  
21 simulate daily streamflow, suspended sediment, and particulate and dissolved phosphorus  
22 dynamics. The model's complexity was compared to one popular nutrient model, INCA-P, and  
23 the performance of the two models was compared in a small rural catchment in northeast  
24 Scotland. For three land use classes, less than six *SimplyP* parameters must be determined  
25 through calibration, the rest may be based on measurements, whilst INCA-P has around 40  
26 unmeasurable parameters. Despite substantially simpler process-representation, *SimplyP*  
27 performed comparably to INCA-P in both calibration and validation and produced similar long-  
28 term projections in response to changes in land management. Results support the hypothesis that  
29 INCA-P is overly complex for the study catchment. We hope our findings will help prompt  
30 wider model comparison exercises, as well as debate amongst the water quality modelling  
31 community as to whether today's models are fit for purpose. Simpler models such as *SimplyP*  
32 have the potential to be useful management and research tools, building blocks for future model  
33 development (prototype code is freely available), or benchmarks against which more complex  
34 models could be evaluated.

## 35 1. Introduction

36 Dynamic, process-based integrated catchment models are designed to represent the  
37 processes governing catchment hydrology and water quality, and may therefore be useful tools  
38 for catchment management. Models can be used, for example, to interpolate sparse monitoring  
39 data, to highlight knowledge and data gaps and help design monitoring strategies, as well as to  
40 provide evidence to support decision making. Integrated catchment models are increasingly  
41 called upon, for example, to explore potential future water quality under scenarios of changing  
42 management, land use and climate, often as part of wider integrated modelling frameworks  
43 (Jakeman & Letcher, 2003, Martin-Ortega *et al.*, 2015). As a result, many catchment-scale  
44 nutrient and sediment models have been developed during the last few decades.

45 In a recent review, Wellen *et al.* (2015) found that the majority of recent nutrient  
46 modelling studies used just five models: SWAT (Arnold & Fohrer, 2005, Arnold *et al.*, 1998),  
47 INCA (Wade *et al.*, 1999, Wade *et al.*, 2002, Whitehead *et al.*, 1998), AnnAGNPS (Binger &  
48 Theurer, 2005, Young *et al.*, 1989), HSPF (Bicknell *et al.*, 2001, Donigian Jr *et al.*, 1995) and  
49 HBV, now superseded by HYPE (Lindström *et al.*, 2010). These models are semi-distributed,  
50 mass balance models, which simulate the daily dynamics of nutrient transport in catchments.  
51 Although the models differ in their structures, each requires on the order of >50 to 100s of user-  
52 supplied parameters for hydrology, sediment and phosphorus (P) simulations to be performed.  
53 Many of these cannot be measured directly and are highly uncertain, and their values must  
54 therefore be determined by calibrating the model to observations. In most catchments, calibration  
55 is carried out using end-of-pipe measurements of discharge and water chemistry, the latter often  
56 only sampled infrequently. Previous analyses have suggested that there is only enough  
57 information in discharge data to constrain a small number (<6) of hydrology model parameters

58 during calibration (Jakeman & Hornberger, 1993), and it seems unlikely that in-stream  
59 concentration data will provide enough additional information for tens or even hundreds of  
60 additional parameters to be constrained (Kirchner, 2006). Overall, there is a growing awareness  
61 that, given data and process knowledge limitations, current catchment water quality models are  
62 overly-complex and there is a need for more parsimonious models that capture the dominant  
63 modes of behavior at the scale of interest (Jackson-Blake & Starrfelt, 2015, Jakeman *et al.*,  
64 2006, Kirchner, 2006, Krueger *et al.*, 2007, Radcliffe *et al.*, 2009). Examples of some of the new  
65 simpler dynamic nutrient models being developed include the Rainfall-Runoff Phosphorus model  
66 (Hahn *et al.*, 2013, Van Meter & Basu, 2015), which focuses on identifying critical source areas  
67 and simulating discharge and soluble reactive phosphorus (SRP) concentration in grassland  
68 catchments, and an analytical model for quantifying time lags between implementing measures  
69 and seeing reductions in surface water nitrate concentrations (Van Meter & Basu, 2015). These  
70 models are relatively limited in their aims and scope, and there is a need to assess to what extent  
71 the aims of more complex models like INCA and SWAT, which attempt to simulate a wider  
72 range of nutrient species and processes, could be achieved using simpler modelling approaches.

73 There are sound theoretical reasons for why simpler models should be chosen over more  
74 complex ones (see e.g. MacKay, 2003, Chapter 28). With over-parameterized models, different  
75 parameter sets will give almost identical fits to the calibration data (e.g. Beven & Binley, 1992),  
76 and yet may yield very different predictions of how the system will behave as conditions change,  
77 and can therefore perform poorly in validation (Seibert, 2003). Model complexity often therefore  
78 turns out to be unjustified in practice (e.g. Perrin *et al.*, 2001). There are related practical reasons  
79 for choosing simpler models. Firstly, over-complexity leads to difficulties in using the model to  
80 test hypotheses about the dominant processes operating within a catchment, as the real processes  
81 may be masked by too much flexibility introduced by unnecessary parameters (Jakeman *et al.*,  
82 2006, Kirchner, 2006). Secondly, large parameter spaces lead to difficulties in model calibration  
83 because of parameter non-identifiability, whether due to structural or practical non-identifiability  
84 (as defined in Raue *et al.*, 2009). There are then related problems with auto-calibration,  
85 sensitivity and uncertainty analyses, as the parameter space increases exponentially with the  
86 number of parameters, eventually becoming too large to be searched within realistic time frames.  
87 Uncertainty analyses are becoming a pre-requisite for model applications, yet as only subsets of  
88 the parameter space of more complex models can be searched, these analyses become somewhat  
89 subjective and incomplete (Jackson-Blake & Starrfelt, 2015, Pappenberger *et al.*, 2007), and the  
90 meaningfulness of estimated uncertainty intervals is often questionable. Finally, as models  
91 become more complex they become more time-consuming to set up and require larger  
92 calibration and evaluation datasets, increasing the financial burden associated with model  
93 applications and limiting the size of the user group. Ultimately, over-complexity therefore  
94 reduces a model's usefulness for supporting research and real world decision-making.

95 Simplicity should not be a goal in itself – the ultimate test of a model is how well it can  
96 simulate the system of interest, usually assessed through validation. The relative performance of  
97 different model structures in validation depends to some extent on data availability – more  
98 detailed data permit more rigorous testing, potentially allowing identification of more complex  
99 model structures. However, in applications where the data available for calibration and validation  
100 are “sparse” (usually the case for catchment simulations, even in well-studied catchments),  
101 simpler models may be expected to perform just as well as complex ones.

102 The hypothesis driving this study is therefore that the most popular catchment-scale  
103 dynamic water quality models are unnecessarily complex. Testing this hypothesis will require a  
104 concerted effort from many modelling groups, with comparative studies of a range of different  
105 model structures in a wide variety of catchments. In this study, we begin this model evaluation  
106 process with the comparison of one popular and representative water quality model, INCA-P,  
107 and a newly-developed parsimonious catchment phosphorus model, SimplyP. The comparison is  
108 carried out in a rural Scottish catchment which contains the majority of land uses and P-related  
109 processes found in temperate rural regions, so results are likely to be applicable more widely.  
110 Our hypothesis is that INCA-P is overly-complex for the catchment, in which case we would  
111 expect similar model performance skill metrics from INCA-P and SimplyP.

## 112 2. Study area

113 Model applications were carried out in the Tarland Burn catchment, upstream of the  
114 James Hutton Institute monitoring point at Coull (51 km<sup>2</sup>). The Tarland is a rural sub-catchment  
115 of the River Dee in northeast Scotland. Land use is a mixture of agriculture (primarily spring  
116 barley, improved grassland and rough grazing), upland heath and forestry. Humus iron podzols  
117 and brown forest soils tend to be associated with agricultural land, with peaty podzols under  
118 semi-natural land on the hills fringing the catchment. The main settlement is the village of  
119 Tarland, which has a small wastewater treatment works (around 600 people); septic tanks serve  
120 the remainder of the catchment (several hundred people). Water quality is of concern, primarily  
121 due to inputs of nutrients and sediments from agriculture. The Tarland Burn is the most upstream  
122 tributary of the ecologically-sensitive River Dee to have impaired water quality, and works have  
123 therefore been underway during the last decade to reduce sediment and nutrient inputs to the  
124 water course (Bergfur *et al.*, 2012). During the 2000-2010 period, the catchment had a mean  
125 annual rainfall of 966 mm, a mean annual runoff of 451 mm yr<sup>-1</sup>, and median total dissolved P  
126 (TDP) and total P (TP) concentrations of 25 and 40 µg l<sup>-1</sup>, respectively.

## 127 3. Modelling approach

### 128 3.1 INCA-P

129 INCA-P is a process-based, semi-distributed catchment model for simulating the daily  
130 transport of sediment, dissolved and particulate P from catchments to streams, as well as  
131 subsequent in-stream transport and processing. It is similar to other popular water quality models  
132 in terms of its structure and the number of processes and parameters it includes, and is therefore  
133 representative of the current dynamic phosphorus models in popular usage. During the last  
134 decade, INCA-P has been applied to a variety of catchments throughout Europe (e.g. Couture *et al.*,  
135 2014, Martin-Ortega *et al.*, 2015, Wade *et al.*, 2007, Whitehead *et al.*, 2013), Canada (e.g.  
136 Crossman *et al.*, 2013) and India (Jin *et al.*, 2015), to explore how P dynamics may respond to  
137 changes in land management and climate. The model was originally developed in the early 2000s  
138 (Wade *et al.*, 2002) and has since undergone several phases of re-development. The most recent  
139 model description is given in Jackson-Blake *et al.* (2016), and only a brief description is given  
140 here. In this study, we used INCA-P version 1.4.4.

141 INCA-P requires input time series of air temperature, precipitation, hydrologically  
142 effective rainfall (HER; the water from precipitation and snowmelt which contributes to runoff),  
143 and soil moisture deficit (SMD, the difference between the soil moisture content and field  
144 capacity). HER and SMD are derived from an external hydrology model.

145           Within INCA-P, water is delivered to the water course via three flow paths: quick flow,  
146 which accounts for overland flow and other rapid flow pathways, soil water flow and  
147 groundwater flow. Quick flow is generated through infiltration and saturation excess overland  
148 flow, soil water flow is generated by HER, and groundwater flow is derived from soil water flow  
149 via percolation. All flows transport dissolved P (as TDP), whilst sediment and particulate P (PP)  
150 are only transported via quick flow. Within the terrestrial compartment, P is present in the soil as  
151 solid labile or inactive soil P, or as dissolved P in soil water. Within the soil water and  
152 groundwater, TDP concentrations are controlled by sorption equilibria. Terrestrial P inputs  
153 include solid and liquid fertilizer, manure and atmospheric deposition; the major terrestrial sinks  
154 are plant uptake and adsorption. The rates of plant uptake, weathering and immobilization are  
155 dependent on temperature, whilst plant uptake is also dependent on soil moisture and season.  
156 Sediment delivery to the stream uses equations from INCA-sed (Jarritt & Lawrence, 2007, Lazar  
157 *et al.*, 2010), including process representations for splash detachment, flow erosion and the  
158 transport capacity of quick flow. PP is associated with sediment, and therefore affected by the  
159 same processes. Instream, the model includes effluent inputs, water abstractions, sediment  
160 settling and resuspension, bank erosion, P sorption reactions in the water column and in the  
161 stream bed and biological uptake of P from the water column and the stream bed. To simulate  
162 biological uptake, the model also simulates the dynamics of epiphyte and macrophyte biomass  
163 within stream reaches.

164           The rate of change in volume or mass of model state variables with respect to time is  
165 described by a series of ordinary differential equations (ODEs), solved within each time step  
166 using an adaptive 4<sup>th</sup> order Runge-Kutte-Merson method.

### 167 **3.2   SimplyP**

168           A new simple hydrology, sediment and phosphorus model, SimplyP, was developed for  
169 comparison to INCA-P. A full description of SimplyP model structure, equations, numerical  
170 methods and priorities for future model development is given in the supplementary information  
171 (SI, Text 1), and only a brief description is provided below.

172           A full description of model aims and scope is given in SI Section 3.1. Briefly, the  
173 development of SimplyP was motivated by results of several studies evaluating INCA-P  
174 (Jackson-Blake *et al.*, 2015, Jackson-Blake & Starrfelt, 2015, Jackson-Blake *et al.*, 2016). These  
175 provided recommendations for model improvements, some of which were incorporated into  
176 INCA-P (version 1.4 onwards). However, one of the main recommendations was for model  
177 simplification. Whilst a certain amount of simplification can be achieved through  
178 parameterization, this requires a high level of familiarity with the model, is time-consuming and  
179 prone to errors, and there are limits to the amount of simplification that can be achieved. The aim  
180 here was therefore to carry out a more substantial process of simplification, whilst maintaining  
181 sufficient complexity for the model to be useful in hypothesis and scenario testing. SimplyP  
182 retains a number of similarities with INCA-P (Section 4.1). Other areas of the model were  
183 inspired by experiences in applying INCA-P, by assumptions used in other water quality models,  
184 or by well-established process understanding. A particular design aim was for the process  
185 representation to be simple enough to allow parameter values to be constrained using available  
186 data, by both keeping the number of parameters requiring calibration to a minimum, and aiming  
187 for as many parameters as possible to be in principle measurable.

188 Like INCA-P and other popular mechanistic water quality models, SimplyP is dynamic  
 189 with a daily time step and is spatially semi-distributed, so the catchment may be split into sub-  
 190 catchments and associated reaches. The model is run for each sub-catchment in turn, and outputs  
 191 from each reach are fed into the main stem sequentially down-stream. Land may be further sub-  
 192 divided based on simple ‘land classes’: for dissolved P processes, two classes are considered, a  
 193 ‘high P’ and a ‘low P’ class. Land within a given class should have a similar gross annual P  
 194 balance, soil P content and hydrological characteristics; in a typical rural catchment the high P  
 195 class could include fertilized grassland and arable land, with everything else assigned to the low  
 196 P class. For sediment and particulate P processes, the high P class may be sub-divided to account  
 197 for differences in erodibility (e.g. improved grassland versus arable land). Finally, if arable land  
 198 is present, the proportion of spring versus autumn-sown crops may be taken into account, along  
 199 with the variation in soil erodibility through time. For convenience, there is also the possibility of  
 200 a ‘newly-converted’ land class, to take into account legacy soil P when agricultural land becomes  
 201 disused, or the lack of legacy soil P in new agricultural land (see SI Section 3.2).

202 A full description of SimplyP model processes is given in SI Section 4. In brief, the  
 203 following sets of processes are included: snow accumulation and melt (SI Section 4.1.1);  
 204 rainfall-runoff (SI Section 4.1.2); in-stream hydrology (SI Section 4.1.3); sediment delivery to  
 205 the watercourse and in-stream transport (SI Section 4.2); and terrestrial and in-stream P  
 206 processes (SI Section 4.3). A summary of the main stores and fluxes of water, sediment and P is  
 207 provided in Figure 1. Three terrestrial flow paths are taken into account: (1) Quick flow, to  
 208 simulate inputs to the watercourse during larger rainfall events and when soils are dry and little  
 209 soil water flow occurs. This was simply calculated by assuming quick flow is proportional to  
 210 incoming precipitation and is routed instantaneously to the stream; (2) Soil water flow,  
 211 responsible for TDP leaching from soils and groundwater recharge. Inputs to the soil water are  
 212 from rainfall and snowmelt; outputs are through evapotranspiration and soil water flow, and soil  
 213 water flow is assumed to only occur once the soil water content is above field capacity; (3)  
 214 Groundwater flow, important for controlling baseflow TDP concentrations. Groundwater  
 215 recharge occurs through percolation from the soil water. In-stream reach volume and discharge  
 216 are then estimated.

217 Sediment processes are represented in a highly simplified manner (see SI Section 4.2 for  
 218 details). Briefly, in-stream suspended sediment (SS) concentration has long been known to be  
 219 well-explained by a simple power law with in-stream discharge (Bagnold, 1966), as:

$$SS = E_{sus} Q_r^k \quad [1]$$

220 where  $Q_r$  is in-stream discharge and  $E_{sus}$  and  $k$  are constants (Colby, 1956). This simple  
 221 power law is taken as the basis for predicting the combined sediment inputs to the stream reach  
 222 from both the land phase and in-stream entrainment. The  $E_{sus}$  parameter is divided into a  
 223 calibrated scaling factor and a number of factors which are known to affect terrestrial sediment  
 224 delivery and in-stream entrainment rates, such as sub-catchment and channel slope and land  
 225 cover. The land cover factor may be varied throughout the year to take into account periods of  
 226 higher soil erodibility (Watson & Evans, 2007).

227 P is represented in the soil in three forms: TDP in the soil water, labile soil P and inactive  
 228 soil P. The masses of dissolved and labile soil P change through time, whilst the mass of inactive  
 229 soil P is constant. Labile soil P and TDP are assumed to be in equilibrium, related via a linear  
 230 relationship (McCray *et al.*, 2005). A number of assumptions are made to help parameterize this



231 relationship, e.g. it is assumed that the inactive soil P content is the same in the high and low P  
232 classes, and that the low P class does not contain labile soil P and has soil water TDP  
233 concentrations around zero. The difference in total soil P content between the two classes is  
234 therefore all potentially labile P in the high P class, built up during fertilizer and manure  
235 additions (for a discussion of the issues relating to incorporating agronomic soil test P  
236 measurements into the model, see SI Section 4.3.1e). Initial soil water TDP concentration is  
237 calibrated within plausible ranges, and used to calculate a gradient for the labile P versus TDP  
238 relationship, which can then be used to relate soil labile P and TDP concentration outside the  
239 calibration period (see SI Section 4.3.1). Fertilizer, manure and plant uptake fluxes are grouped  
240 together into a single gross annual P balance parameter, which is then evenly applied or  
241 subtracted over the course of the year. This representation of soil P processes is highly  
242 simplified. In reality, soil P is present in a continuum of interlinked states of varying  
243 extractability, and hysteresis effects are common in P transfers between states. However, the  
244 understanding of how detailed soil chemical processes upscale to the catchment-scale is arguably  
245 not yet advanced enough to be usefully incorporated into a catchment-scale model.

246 Quick flow TDP concentration is assumed to be the same as soil water TDP  
247 concentration. Groundwater TDP concentration is set as a constant, given generally high P  
248 sorption capacities in and below mineral soil horizons. TDP is then transported to the reach via  
249 all three terrestrial flow pathways, whilst PP dynamics are linked to SS dynamics, taking into  
250 account enrichment of PP relative to parent material due to the selective transport of finer-  
251 grained, more P-rich material (Sharpley, 1980). Incidental P losses, potentially large P fluxes  
252 washed into watercourses when rainfall events coincide with fresh fertilizer and manure  
253 applications, are not yet included, due to difficulties in capturing the high spatial and temporal  
254 variability of these events and the relatively detailed management knowledge required.

255 In-stream, the model only includes the dilution of diffuse and point source P inputs and  
256 down-stream transport. This simple formulation assumes that in-stream processing is in a state of  
257 dynamic equilibrium, i.e. in-stream sinks and sources are balanced. Whilst there is insufficient  
258 data to suggest otherwise in the study catchment, it would be straightforward to add a simple  
259 retention or loss factor to the model for catchments where in-stream retention is thought to be  
260 important, informed, for example, by results of large-scale empirical studies (e.g. Alexander *et*  
261 *al.*, 2004).

262 The rate of change in volume or mass of model state variables with respect to time is  
263 described by a series of ODEs. To reduce errors introduced by numerical approximations, model  
264 ODEs were formulated as continuous functions, avoiding thresholds, and were solved within  
265 each time step using the LSODA solver (Hindmarsh, 1983) (see SI Section 4.5).

266 SimplyP requires input time series of daily precipitation, air temperature and potential  
267 evapotranspiration (PET). Model outputs include time series of daily fluxes and flow-weighted  
268 daily mean concentrations of TDP, PP and SS and daily mean flow. The state of the internal  
269 stores may also be output (e.g. snow depth, volumes and flows from the two water stores, and P  
270 masses in the different stores).

271 SimplyP v1.0 model code is open source and freely-available for download  
272 (<https://github.com/LeahJB/SimplyP>). See SI Section 2 for details and instructions.

### 273 3.3 Data for model calibration and testing

274 Data from the catchment outflow from 2000 to 2010 were used for model calibration and  
275 testing. Weekly chemistry sampling took place between 2000 and the end of 2003, with some  
276 daily sampling during rainfall events. Daily samples were collected between February 2004 and  
277 June 2005, providing 15 months of daily data. After June 2005, infrequent irregular sampling  
278 continued for the rest of the period. Measured parameters included SS, TDP and soluble reactive  
279 P (SRP) concentrations; daily 2004-2005 samples were also analyzed for total P (TP), allowing  
280 PP to be calculated (as  $TP - TDP$ ). Daily discharge data is also available (daily means calculated  
281 from 15-minute data). For further details of monitoring and analytical methods, see Stutter *et al.*  
282 (2008).

283 A comprehensive set of additional data were compiled to help parameterize both models,  
284 including land use data, estimates of sewage effluent inputs from septic tanks and the sewage  
285 treatment works, soil solution and groundwater TDP concentrations, and soils data, including  
286 soil total P content and bulk density. See Jackson-Blake *et al.* (2015) for a full description of  
287 these data.

### 288 3.4 Model setups in the study catchment

289 The INCA-P application used in this study is described in Jackson-Blake *et al.* (2016).  
290 Briefly, the catchment was split into four reaches and associated sub-catchments (Figure 2). Four  
291 parameters were varied by reach: reach width and slope, initial bed sediment silt mass and  
292 effluent inputs. Three land classes were considered: arable, improved grassland and semi-natural,  
293 although when calculating fertilizer and manure inputs to agricultural land, area-weighted inputs  
294 from a finer-representation of the land use were used. Semi-natural land incorporated rough  
295 grazing, heather moorland, deciduous and coniferous woodland. For more details, including  
296 percent land use per sub-catchment, see Jackson-Blake *et al.* (2016).

297 For SimplyP, the catchment was considered as a single unit, rather than being separated  
298 into sub-catchments and reaches. Only one partially unconstrained SimplyP parameter may vary  
299 by reach, the effluent input, and for this first test of the model sewage effluent inputs from the  
300 sewage treatment works and septic tanks were summed and added at the top of the single  
301 simulated reach. The catchment area was then grouped similarly to the INCA-P setup: the high P  
302 class (50% of the catchment area) included arable land (20%) and improved grassland (30%).  
303 Upland heath, forestry and rough grazing were grouped into the low P class as semi-natural land  
304 (50%).

305 Input data to drive both models included air temperature and precipitation, derived from  
306 the UK Met Office 5 km gridded dataset, and PET, estimated using the FAO56 Penman  
307 Monteith method (Allen *et al.*, 1998). HER and SMD time series for INCA-P were calculated  
308 using a water balance model (described in Jackson-Blake *et al.*, 2015), which in turn required  
309 inputs of daily precipitation and PET. This water balance model has 8 parameters, the majority  
310 based on soil properties.

### 311 3.5 Model calibration, validation and scenario analysis

312 Ideally, a single auto-calibration procedure would be used to calibrate both INCA-P and  
313 SimplyP, rather than relying on manual calibration which could introduce modeler bias.  
314 However, the complexity of INCA-P means that full auto-calibration of all uncertain parameters

315 is not possible – the parameter space is too large to be explored within reasonable time scales  
316 (e.g. Jackson-Blake & Starrfelt, 2015), and the choice of which subset of parameters to include  
317 in the analysis is subjective. Auto-calibration often does not lead to improved model  
318 performance compared to manual calibration (Boyle *et al.*, 2000), particularly for dynamic  
319 variables such as phosphorus – previous auto-calibration of INCA-P in the study catchment  
320 resulted in less realistic simulated TDP dynamics than manual calibration (Jackson-Blake &  
321 Starrfelt, 2015). For this study, both models were therefore calibrated manually. The INCA-P  
322 calibration does however represent what we feel is the best possible setup for the Tarland  
323 catchment: much time has been spent calibrating INCA-P in the study catchment, initially  
324 through manual calibration and an investigation of different model structures (Jackson-Blake *et*  
325 *al.*, 2015), then through auto-calibration using a sophisticated MCMC algorithm (Jackson-Blake  
326 & Starrfelt, 2015), and finally through manual calibration informed by the results of previous  
327 calibrations (Jackson-Blake *et al.*, 2016). By contrast, the SimplyP calibration was done within a  
328 few hours, and therefore represents a first test of the model’s potential.

329 The calibration period was 2004-2005, encompassing the 15 months when daily  
330 discharge and surface water chemistry data are available. Daily discharge and sparser water  
331 chemistry data for the period 2000-2010 (excluding 2004-2005) were then used for model  
332 validation.

333 Manual calibration was done in a step-wise manner: hydrology-related parameters were  
334 adjusted until an acceptable discharge calibration was obtained, then sediment-related parameters  
335 and finally P-related parameters, with several iterations. Additional data taken into account in  
336 calibration included one-off measurements of soil solution TDP concentrations from agricultural  
337 soils in the catchment. Model performance was evaluated using the procedure recommended in  
338 Jackson-Blake *et al.* (2015), using a combination of: (1) visual assessment of time series, (2)  
339 comparison of distributions of observed and simulated data using quantile-quantile (QQ) plots,  
340 and (3) model performance statistics, including Spearman’s Rank correlation coefficient and  
341 model bias. Nash Sutcliffe efficiency (NS) and NS on logged data were used to assess the  
342 discharge simulation. NS was not used for water chemistry parameters as previous work has  
343 shown it to be poor at discriminating between realistic and unrealistic P simulations (Jackson-  
344 Blake *et al.*, 2015). In addition, the INCA-P calibration included checking for plausible changes  
345 in masses of soil P and stream bed sediment and PP during the model run.

346 For both models, the calibration procedure also involved adjusting the initial soil P store  
347 so that simulated agricultural soil water TDP concentration changed at an appropriate rate over  
348 longer model runs: long-term monitoring experiments suggest that, in the absence of fertilizer  
349 inputs, soil P in agricultural land should drop to near semi-natural values with a half-life of 7 to 9  
350 years (McCollum, 1991, Syers *et al.*, 2008), i.e. within around 35 years in the study catchment.  
351 In INCA-P, this involved adjusting the soil depth parameter. In SimplyP, the soil areal mass  
352 parameter was adjusted (combining soil depth and bulk density; SI Table 7). Soil depths in the  
353 range 7 to 10 cm were obtained, 14 to 20 cm taking soil porosity into account. This is plausible,  
354 given that soil P decreases with depth and is highest in the top 20 cm in agricultural soils (Syers  
355 *et al.*, 2008). Calibrated parameter values for SimplyP are given in Table 1.

356 Several sensitivity tests were then carried out with SimplyP to test the model’s ability to  
357 explore future scenarios of change. The model was run for a 30-year period with a number of  
358 reductions in net P inputs relative to the 2000 – 2010 baseline, corresponding to reductions in  
359 fertilizer and manure applications of 25%, 50% and 100%. Agricultural land in the catchment

360 has an estimated P balance (inputs from fertilizer and manure minus outputs via harvesting) of  
361 around  $10 \text{ kg ha}^{-1} \text{ yr}^{-1}$  (Messiga *et al.*, 2010) and fertilizer and manure inputs are estimated at  
362 around  $24 \text{ kg ha}^{-1} \text{ yr}^{-1}$ . The 25% and 50% reduction scenarios are therefore economically-  
363 feasible, corresponding to annual P balances of around 4 and  $-2 \text{ kg ha}^{-1} \text{ yr}^{-1}$ , which should have  
364 little impact on crop yields for a number of years. The 100% reduction scenario is included as a  
365 sensitivity test. Results were compared to previous results for the same set of scenarios derived  
366 using INCA-P (Jackson-Blake *et al.*, 2016).

## 367 **4. Results**

### 368 **4.1 Comparison of model process-representation and complexity**

369 SimplyP has a number of features in common with INCA-P, such as three terrestrial flow  
370 paths, a simple split of P into TDP and PP, and a split of soil P into labile and inactive stores.  
371 Many processes included in INCA-P have however been omitted from SimplyP, the most  
372 important P-related ones being: (1) the removal of seasonal variability in soil water TDP  
373 concentrations; (2) simplification of quick flow generation, by removing the process-  
374 representation of infiltration excess and saturation excess; (3) extensive simplification of the  
375 sediment-related equations, including removing the process-representation of splash detachment,  
376 flow erosion, the transport capacity of quick flow and in-stream entrainment and deposition; (4)  
377 controls on groundwater TDP concentration, which in SimplyP is considered to be constant; (5)  
378 simplification of the in-stream P processes, including removal of the macrophyte and epiphyte  
379 biomass equations and of the simulation of separate P processes in the water column and the  
380 stream bed.

381 Another difference is the incorporation of a hydrology model into SimplyP. We see this  
382 as a great improvement, removing the need for an external hydrology model and simplifying the  
383 calibration procedure, as water quality simulations are extremely dependent on the hydrology  
384 simulation, so time-consuming iterative calibration of separate hydrology and water quality  
385 models is often required for good model performance.

386 Model complexity is in part reflected by the number of state variables included in the  
387 model. For each sub-catchment/reach, SimplyP has 13 ODEs (Table SI-9), plus four for  
388 calculating daily in-stream fluxes from instantaneous fluxes (not present in INCA-P to our  
389 knowledge, but required to calculate volume-weighted daily mean concentrations). This is  
390 substantially fewer than INCA-P, despite the fact that SimplyP includes a hydrology model:  
391 INCA-P has 28 ODEs before land use variability is taken into account and 52 in an equivalent  
392 setup to SimplyP with 3 land use classes.

393 Model complexity is also in part reflected by the number of model parameters. SimplyP  
394 parameters are described in Table 1 and INCA-P parameters in Jackson-Blake *et al.* (2016). Both  
395 models require a number of well-constrained parameters which are generally not included in the  
396 calibration procedure (e.g. catchment area, areas of land classes, slopes and reach lengths;  
397 described in Table SI-10 for SimplyP). Excluding these, the total number of parameters in both  
398 models, split by process or type, is summarized in Table 2. SimplyP has 23 parameters that are to  
399 some extent unconstrained, 24 – 27 when spatial variability between land classes is taken into  
400 account. At least 8 of these are optional (before taking spatial variability into account),  
401 depending on the level of process-representation desired. By comparison, INCA-P has 146  
402 parameters (assuming one reach and sub-catchment, varying three parameters by two land

403 classes for dissolved P processes and by three classes for soil erodibility for comparability with  
404 SimplyP). The version of INCA-P described in the tests performed here (4 reaches with 3 land  
405 classes) involves around 48 calibrating parameters, which we believe is simple compared to  
406 previous applications (e.g. Crossman *et al.*, 2013, Jin *et al.*, 2015). A further ~45 parameters  
407 were carefully assigned values to help simplify the model structure and turn certain processes  
408 off, leaving around 53 unused parameters.

409 Only one SimplyP parameter varies by sub-catchment or reach, the effluent TDP input,  
410 so model complexity will not increase substantially in larger systems. For INCA-P, 64  
411 parameters may be varied by sub-catchment or reach, resulting in the potential for highly  
412 parameterized model setups.

413 Another important issue is the extent to which model parameters may be informed by  
414 data (Table 2). Around 43 INCA-P parameters are not measurable and must be determined  
415 purely through calibration, and 14 are not measurable and yet are thought to exert a key  
416 influence on model output (Jackson-Blake *et al.*, 2016). This can be problematic for model  
417 calibration. Meanwhile, the majority of SimplyP parameters may be based on measured data or  
418 data derived from literature reviews, and only 4 or 5 must be determined purely through  
419 calibration (Table 1). One of these relates to the sediment simulation, the rest are hydrology  
420 parameters. This is promising, as water quality models are particularly sensitive to hydrology  
421 parameters (Dean *et al.*, 2009, Jackson-Blake & Starrfelt, 2015, van Griensven *et al.*, 2006), so  
422 there is a good chance of these parameters being identifiable. Even in the most complex setup in  
423 which all 27 SimplyP parameters are used, it should therefore be feasible to search the entire  
424 parameter space as part of an auto-calibration or uncertainty analysis, provided the user has data  
425 to inform the parameter values (Table 1) and sufficient discharge and water quality observations  
426 (including SS, TDP and PP concentrations under the full range of flow conditions).

## 427 **4.2 Model performance in the Tarland Burn**

### 428 **4.2.1 Model calibration and validation results**

429 During the calibration period, discharge performance statistics were slightly better for  
430 SimplyP than for INCA-P (Table 3). This is in part because a snow accumulation and melt  
431 routine was included in SimplyP and not in the simple model used to generate HER input for  
432 INCA-P, although this only affects a few winter flow peaks (Figure 4). Small discharge peaks  
433 were also often slightly better simulated by SimplyP, particularly during baseflow, which may  
434 not have been the case had a more complex hydrology model been used to generate input for  
435 INCA-P. The models performed similarly for SS, which is noteworthy given the dramatically  
436 simpler process-representation in SimplyP. Slightly improved SS performance statistics for  
437 SimplyP are likely to be due to the slightly better discharge simulation. The TP and PP  
438 simulations are also similar: output from SimplyP is less biased than output from INCA-P and  
439 the distribution of the simulated PP data in particular is closer to that of the observations (Figure  
440 3). Both variables however have a lower correlation coefficient than INCA-P output. The story is  
441 clearer for the TDP simulation, with SimplyP scoring higher in all model performance statistics  
442 during the calibration period (Table 3), and also producing distributions of simulated data that  
443 were more comparable to the observations (Figure 3). The slightly improved TDP dynamics may  
444 be related to the better discharge simulation. However, an improvement in simulated TDP is  
445 apparent even during flow events when SimplyP and INCA-P produced comparable discharge

446 simulations (Figure 4): SimplyP TDP peaks tend to be less broad and more responsive to  
447 hydrological inputs, something which could not be achieved with INCA-P even when the soil  
448 water time constants were reduced to below the values used in SimplyP. The reasons for this are  
449 not clear, but could relate to the formulation or solving of the ODEs in INCA-P (although this  
450 could not be checked as the code is closed source).

451 The story is similar during the validation period, when model performance statistics for  
452 SimplyP were slightly better than those for INCA-P for discharge and TDP (aside from a slightly  
453 larger bias in TDP), whilst SS had lower bias but a smaller correlation coefficient (Table 3).  
454 There has been a shift in baseflow discharge over time during the validation period (Figure 5),  
455 likely due to a change in channel cross section. Both models therefore over-estimate summer  
456 discharge during the first half of the period and under-estimate it later on. Although TDP  
457 performance statistics are slightly better for SimplyP, TDP is somewhat under-estimated during  
458 baseflow, something which is less of an issue in INCA-P during the validation period (Figure 5),  
459 and which leads to the slightly larger difference in distributions of observed and simulated data  
460 for SimplyP (Figure 3). This is likely due to differences in the discharge simulation, as SimplyP  
461 tends to simulate slightly higher discharge during baseflow, and even small differences in  
462 simulated baseflow discharge lead to large differences in simulated concentration.

463 Note that NS coefficients are only reported for water quality variables in Table 3 for  
464 comparability with other studies, and were not used when assessing model performance.  
465 Although NS coefficients might suggest simulations from both models are inadequate, various  
466 authors have pointed out problems with using NS as a measure of model performance (e.g. Jain  
467 & Sudheer, 2008, Schaepli & Gupta, 2007) and we have argued elsewhere that NS is  
468 particularly poor for measuring the performance of P models in agricultural catchments, where  
469 NS values above 0.2 are rare unless point sources dominate (Jackson-Blake *et al.*, 2015).

470 The results presented here constitute a small fraction of the behavior that could be  
471 compared between the two models. However, the indications are that, at least during calibration  
472 and testing within similar conditions to the calibration period, SimplyP appears to perform  
473 comparably for PP, SS and TP, and perhaps slightly outperform INCA-P in terms of discharge  
474 and TDP. The two models therefore appear to be as capable, at least in this catchment, of  
475 simulating daily concentrations and discharge. The broader question of whether either model  
476 performs well enough for model output to be useful is a valid one, the answer depending largely  
477 on what the output will be used for and how it is presented. This is discussed further in Jackson-  
478 Blake *et al.* (2015).

479

#### 480 **4.2.2 Scenario analysis**

481 Results from the fertilizer and manure reduction scenarios are shown in Figure 6 in terms  
482 of the change in agricultural soil water  $EPC_0$  (the equilibrium TDP concentration of zero  
483 sorption) and in-stream mean annual TDP concentration over the 30-year period. Results from  
484 the two models tell the same story: under the baseline and 25% reduction scenario P is still being  
485 added surplus to crop requirements, and so  $EPC_0$  continues to rise, resulting in an increase over  
486 time in in-stream TDP concentration during rainfall events and a higher annual mean.  
487 Meanwhile, the 50% and 100% reduction scenarios result in net plant uptake of P from the soil,  
488 gradually depleting the labile P store and causing reductions in simulated  $EPC_0$ , soil water TDP  
489 inputs to the stream and therefore lower mean annual in-stream TDP concentration. However,

490 there is an important lag in the time for improvements to be seen, with only small decreases in  
491 in-stream TDP concentrations during the first 5 years of the simulation (less than a 15%  
492 reduction compared to the baseline even for the 100% reduction scenario; data not shown). The  
493 full benefits of the measures are only realized by the end of the 30-year period, the time taken for  
494 near full depletion of the labile soil P store.

495 Whilst terrestrial compartment results were similar for the two models, in-stream TDP  
496 results differed slightly, with a larger effect simulated by INCA-P. This may be because the in-  
497 stream TDP peaks simulated by INCA-P are slightly too broad (Section 4.2.1), resulting in over-  
498 estimation of the influence of agricultural inputs on mean in-stream TDP concentrations.

499 The similarity in results does not mean either model is right, but it does show that  
500 SimplyP is as capable of predicting the dynamics of legacy soil P as INCA-P. For both models to  
501 produce more robust output, more long term soil P data is needed to help constrain the  
502 parameterization as well as improved understanding of how soil P extractability changes at the  
503 catchment scale as soil P stores become depleted. Furthermore, a potentially important process  
504 currently missing from both models is the link between soil P content and crop uptake of P, as it  
505 is probably unrealistic to expect uptake to be unchanged as soil P stocks become depleted.

506 SimplyP has been run with just one kind of future scenario here – the effect of changing  
507 terrestrial P balances. However, like INCA, the model can be used to simulate a number of other  
508 broad-scale measures. Being a catchment-scale model, it is particularly suited to looking at the  
509 potential impacts of changes in land use, climate and effluent inputs. The effectiveness of  
510 measures aimed at reducing sediment inputs to the stream may also be simulated through  
511 changing the terrestrial erodibility parameters (informed for example by literature on the  
512 Universal Soil Loss Equation (Kinnell, 2010)) or through the use of a delivery reduction factor.

## 513 **5. Discussion and conclusions**

514 We set out to test the hypothesis that INCA-P is overly-complex when applied in a  
515 Scottish agricultural catchment. To do this, a new simple catchment phosphorus model was  
516 developed, SimplyP, and model structure and performance were compared to INCA-P. SimplyP  
517 is substantially more streamlined than INCA-P, with up to 28 parameters, whilst INCA-P has  
518 around 148. Only 4 or 5 SimplyP parameters are ‘free’, i.e. cannot be informed by observations,  
519 compared to around 45 for INCA-P. This reduction in complexity is despite the fact that SimplyP  
520 includes a rainfall-runoff module, whilst INCA-P relies on output from an external hydrology  
521 model (not included in this comparison of complexity). In the study catchment, both models  
522 performed similarly during calibration and validation. Both models also produced similar results  
523 in a scenario assessment, with identical implications for diffuse pollution mitigation and decision  
524 support. Results therefore support the hypothesis that INCA-P is overly-complex in the study  
525 catchment.

526 Although limited to just one study site, P dynamics in the study catchment are controlled  
527 by similar processes to those operating in the majority of temperate regions, with a mixture of  
528 land uses, hydrological flow paths and P inputs from both agriculture and sewage. This result is  
529 therefore likely to be transferable to other study areas. In addition, INCA-P is similar in  
530 complexity and structure to other popular catchment water quality models, so this conclusion is  
531 likely to apply to other models and water quality variables. Results are consistent with long-  
532 established theory and recent thinking in catchment science (e.g. Kirchner, 2006, Sivapalan,

533 2006), and provide further support for the idea that a more parsimonious approach to simulating  
534 catchment water quality is warranted.

535 Overall, there are strong arguments, backed up by the findings presented here, that the  
536 current generation of catchment-scale, dynamic water quality models are too complex. This  
537 complexity has likely been driven by two factors. Firstly, there has been a desire to include  
538 process-understanding and data derived from plot-scale studies. However, non-linearities  
539 between small-scale and catchment-scale processes mean up-scaling is often inappropriate (e.g.  
540 Kirchner, 2006, Oreskes & Belitz, 2001); catchment-scale responses are often simpler than  
541 might be anticipated from detailed process knowledge (Sivapalan, 2005). We therefore need a  
542 better understanding of catchment-scale behavior, requiring more comprehensive spatially-  
543 distributed data collection across catchments as well as high frequency monitoring of  
544 watercourses. Technological improvements in remote sensing and in-stream sensors are  
545 beginning to yield exciting new data, but more effort is needed to constrain soil water,  
546 groundwater and effluent chemistry, and to determine longer-term trends in soil and groundwater  
547 chemistry, especially in response to changes in e.g. land management and climate. Secondly,  
548 there has been a desire to make models versatile and widely applicable, i.e. to produce ‘one-size-  
549 fits-all’ models. This has helped us think about the variety of processes that could operate in  
550 different areas, but for any given study area is likely to result in overly complex models.  
551 Balancing the demands of model realism and parsimony remains a significant challenge, and  
552 resolving the tension between the two can only be achieved by assessing the performance of  
553 models with different structures (e.g. Fenicia *et al.*, 2006), preferably within statistical model  
554 comparison frameworks (e.g. Spiegelhalter *et al.*, 2002). For this, community-based modular  
555 model frameworks offer perhaps the best hope for the future (e.g. Mooij *et al.*, 2010, Robson,  
556 2014).

557 The initial aim in developing SimplyP was a proof-of-concept that simple can be as good  
558 as complex. However, we believe that SimplyP also has the potential to fill an important gap,  
559 attempting to be both process-based and dynamic, maintaining a spatially semi-distributed setup,  
560 differentiating between soluble and particulate P phases, incorporating hydrology and a variety  
561 of flow paths, and yet having far fewer parameters than other popular water quality models.  
562 SimplyP also retains sufficient complexity to be used to investigate scenarios relevant for  
563 research, policy and land management. It was markedly quicker (and therefore cheaper) to set up  
564 and calibrate than INCA-P, and it should be feasible to include all parameters in an auto-  
565 calibration/uncertainty analysis procedure, and therefore in a formal model comparison  
566 framework. The fact that most parameters are physically-meaningful is also likely to help with  
567 generalization and transferability to other (perhaps more data-poor) areas (Sivapalan, 2005). At a  
568 more fundamental level, the reduction in the number of parameters should make validation  
569 exercises more effective for diagnosing structural problems with the model, as model behavior  
570 becomes less dependent on parameter tuning and more on model structure. This in turn means  
571 that the simpler model should be more useful for testing hypotheses about system behavior  
572 (Kirchner, 2006). The hope is therefore that SimplyP could provide a benchmark when choosing  
573 between different models, a building block for future model development, or, given its  
574 advantages over more complex models, be a useful tool in its own right (prototype code is freely  
575 available, see Section 3.2).

576 For SimplyP to become a robust tool in its own right, a number of further developments  
577 are recommended. The first priority is for more testing in a range of contrasting study sites, to



578 establish whether any of the extra processes available in more complex models are required in  
 579 certain areas. Additional potential model improvements are summarized in SI Section 5 and  
 580 Table SI 12. Many of these suggestions involve an increase in complexity, and would need to be  
 581 justified by demonstrating improved model performance in validation.

582 Overall, we hope that the model development and simple comparison exercise presented  
 583 here will help prompt wider model comparison and simplification, and more generally  
 584 encourage debate amongst the water quality modelling community as to whether today's models  
 585 are appropriate and fit for purpose.

## 586 **Supplementary references**

587 The description of SimplyP in the supplementary information cites many additional  
 588 studies, reproduced here in the main text to ensure they are indexed, included in citation records  
 589 and given appropriate credit (Bowes *et al.*, 2005, Chapra, 2008, Clark & Kavetski, 2010, Croke  
 590 *et al.*, 2006, Dari *et al.*, 2015, Domagalski & Johnson, 2011, Fenicia *et al.*, 2011, Gan & Luo,  
 591 2013, Hindmarsh, 1983, Holman *et al.*, 2008, House, 2003, Jarvie *et al.*, 2013a, Jarvie *et al.*,  
 592 2013b, Jordan-Meille *et al.*, 2012, Kavetski & Clark, 2011, Kavetski *et al.*, 2006a, Kavetski *et al.*,  
 593 2006b, Kleinman *et al.*, 2011, Lefrançois *et al.*, 2007, Leopold & Maddock Jr, 1953, Luo *et al.*,  
 594 2012, Menzel, 1980, Merritt *et al.*, 2003, Neal & Jarvie, 2005, Oeurng *et al.*, 2010, Radcliffe  
 595 & Cabrera, 2006, Ratliff *et al.*, 1983, Renard *et al.*, 1991, Sample, 2015, Sharpley *et al.*, 2013,  
 596 Stollenwerk, 1996, Stutter *et al.*, 2010, Stutter *et al.*, 2009, Trimble, 2010, Twarakavi *et al.*,  
 597 2009, Wischmeier & Smith, 1965, Wischmeier & Smith, 1978, Wittenberg, 1999, Wolman *et al.*,  
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 604 Infrastructure for river-basin modelling. Data to reproduce the conclusions reported here are  
 605 available for download, including parameter values, input data and observed data  
 606 ([https://github.com/LeahJB/SimplyP/tree/Hydrology\\_Model/Tarland\\_Data\\_WRR2016](https://github.com/LeahJB/SimplyP/tree/Hydrology_Model/Tarland_Data_WRR2016)).  
 607 SimplyP parameter values for scenario analysis are described in Section 3.5. SimplyP model  
 608 code may be downloaded from <https://github.com/LeahJB/SimplyP>, see SI Section 2 for more  
 609 details. To obtain an INCA-P executable, email [rmc@niva.no](mailto:rmc@niva.no).

## 610 **References**

- 611 Alexander R, Smith R, Schwarz G (2004) Estimates of diffuse phosphorus sources in surface  
 612 waters of the United States using a spatially referenced watershed model. *Water Science  
 613 and Technology*, **49**, 1-10.
- 614 Allen R, Pereira L, Raes D, Smith M (1998) *Crop evapotranspiration – guidelines for computing  
 615 crop water requirements. FAO irrigation and drainage paper 56.*
- 616 Arnold JG, Fohrer N (2005) SWAT2000: current capabilities and research opportunities in  
 617 applied watershed modelling. *Hydrological Processes*, **19**, 563-572.

- 618 Arnold JG, Srinivasan R, Muttiah RS, Williams JR (1998) Large area hydrologic modeling and  
619 assessment part I: Model development1. *JAWRA Journal of the American Water*  
620 *Resources Association*, **34**, 73-89.
- 621 Asselman NEM (2000) Fitting and interpretation of sediment rating curves. *Journal of*  
622 *Hydrology*, **234**, 228-248.
- 623 Bagnold R (1966) An approach to the sediment transport problem. *General Physics Geological*  
624 *Survey, Prof. paper*.
- 625 Beck HE, Dijk AI, Miralles DG, Jeu RA, Mcvicar TR, Schellekens J (2013) Global patterns in  
626 base flow index and recession based on streamflow observations from 3394 catchments.  
627 *Water Resources Research*, **49**, 7843-7863.
- 628 Bergfur J, Demars BOL, Stutter MI, Langan SJ, Friberg N (2012) The Tarland Catchment  
629 Initiative and Its Effect on Stream Water Quality and Macroinvertebrate Indices. *J.*  
630 *Environ. Qual.*, **41**, 314-321.
- 631 Beven K, Binley A (1992) The future of distributed models: Model calibration and uncertainty  
632 prediction. *Hydrological Processes*, **6**, 279-298.
- 633 Bicknell BR, Imhoff JC, Kittle Jr JL, Jobes T, Donigian Jr A, Johanson R (2001) Hydrological  
634 simulation program-Fortran: HSPF version 12 user's manual. *AQUA TERRA*  
635 *Consultants, Mountain View, California*.
- 636 Binger R, Theurer F (2005) AnnAGNPS Technical Processes documentation, version 3.2. In:  
637 *USDA-ARS, National Sedimentation Laboratory*. pp Page.
- 638 Bowes MJ, House WA, Hodgkinson RA, Leach DV (2005) Phosphorus–discharge hysteresis  
639 during storm events along a river catchment: the River Swale, UK. *Water Research*, **39**,  
640 751-762.
- 641 Boyle DP, Gupta HV, Sorooshian S (2000) Toward improved calibration of hydrologic models:  
642 Combining the strengths of manual and automatic methods. *Water Resources Research*,  
643 **36**, 3663-3674.
- 644 Chapra SC (2008) *Surface water-quality modeling*, Waveland press.
- 645 Clark MP, Kavetski D (2010) Ancient numerical daemons of conceptual hydrological modeling:  
646 1. Fidelity and efficiency of time stepping schemes. *Water Resources Research*, **46**,  
647 W10510.
- 648 Colby B (1956) Relationship of sediment discharge to streamflow. pp Page, US Dept. of the  
649 Interior, Geological Survey, Water Resources Division.
- 650 Couture R-M, Tominaga K, Starrfelt J, Moe SJ, Kaste Ø, Wright RF (2014) Modelling  
651 phosphorus loading and algal blooms in a Nordic agricultural catchment-lake system  
652 under changing land-use and climate. *Environmental Science: Processes & Impacts*, **16**,  
653 1588-1599.
- 654 Croke BF, Andrews F, Jakeman AJ, Cuddy SM, Luddy A (2006) IHACRES Classic Plus: a  
655 redesign of the IHACRES rainfall-runoff model. *Environmental Modelling & Software*,  
656 **21**, 426-427.
- 657 Crossman J, Futter MN, Oni SK *et al.* (2013) Impacts of climate change on hydrology and water  
658 quality: Future proofing management strategies in the Lake Simcoe watershed, Canada.  
659 *Journal of Great Lakes Research*, **39**, 19-32.
- 660 Dari B, Nair V, Colee J, Harris W, Mylavarapu R (2015) Estimation of Isotherm Parameters: A  
661 Simple and Cost-effective Procedure. *Frontiers in Environmental Science*, **3**.

- 662 Dean S, Freer J, Beven K, Wade AJ, Butterfield D (2009) Uncertainty assessment of a process-  
 663 based integrated catchment model of phosphorus. *Stochastic environmental research and*  
 664 *risk assessment*, **23**, 991-1010.
- 665 Domagalski JL, Johnson HM (2011) Subsurface transport of orthophosphate in five agricultural  
 666 watersheds, USA. *Journal of Hydrology*, **409**, 157-171.
- 667 Donigian Jr A, Bicknell B, Imhoff J, Singh V (1995) Hydrological Simulation Program-Fortran  
 668 (HSPF). *Computer models of watershed hydrology.*, 395-442.
- 669 Eurostat (2013) Agri-environmental indicator fact sheet - risk of pollution by phosphorus. In:  
 670 *European Union (EU) agri-environmental indicator fact sheets*. pp Page.
- 671 Fenicia F, Kavetski D, Savenije HHG (2011) Elements of a flexible approach for conceptual  
 672 hydrological modeling: 1. Motivation and theoretical development. *Water Resources*  
 673 *Research*, **47**, n/a-n/a.
- 674 Fenicia F, Savenije HHG, Matgen P, Pfister L (2006) Is the groundwater reservoir linear?  
 675 Learning from data in hydrological modelling. *Hydrol. Earth Syst. Sci.*, **10**, 139-150.
- 676 Gan R, Luo Y (2013) Using the nonlinear aquifer storage–discharge relationship to simulate the  
 677 base flow of glacier- and snowmelt-dominated basins in northwest China. *Hydrol. Earth*  
 678 *Syst. Sci.*, **17**, 3577-3586.
- 679 Hahn C, Prasuhn V, Stamm C, Lazzarotto P, Evangelou M, Schulin R (2013) Prediction of  
 680 dissolved reactive phosphorus losses from small agricultural catchments: calibration and  
 681 validation of a parsimonious model. *Hydrology and Earth System Sciences*, **17**, 3679.
- 682 Hindmarsh AC (1983) ODEPACK, A Systematized Collection of ODE Solvers, RS Stepleman et  
 683 al.(eds.), North-Holland, Amsterdam,(vol. 1 of), pp. 55-64. *IMACS transactions on*  
 684 *scientific computation*, **1**, 55-64.
- 685 Holman IP, Whelan MJ, Howden NJK, Bellamy PH, Willby NJ, Rivas-Casado M, Mcconvey P  
 686 (2008) Phosphorus in groundwater—an overlooked contributor to eutrophication?  
 687 *Hydrological Processes*, **22**, 5121-5127.
- 688 House WA (2003) Geochemical cycling of phosphorus in rivers. *Applied Geochemistry*, **18**, 739-  
 689 748.
- 690 Jackson-Blake LA, Dunn SM, Helliwell RC, Skeffington RA, Stutter MI, Wade AJ (2015) How  
 691 well can we model stream phosphorus concentrations in agricultural catchments?  
 692 *Environmental Modelling & Software*, **64**, 31-46.
- 693 Jackson-Blake LA, Starrfelt J (2015) Do higher data frequency and Bayesian auto-calibration  
 694 lead to better model calibration? Insights from an application of INCA-P, a process-based  
 695 river phosphorus model. *Journal of Hydrology*, **527**, 641-655.
- 696 Jackson-Blake LA, Wade AJ, Futter MN *et al.* (2016) The INtegrated Catchment model of  
 697 Phosphorus dynamics (INCA-P): description and demonstration of new model structure  
 698 and equations. *Environmental Modelling & Software*, **83**, 356-386.
- 699 Jain SK, Sudheer K (2008) Fitting of hydrologic models: a close look at the Nash–Sutcliffe  
 700 index. *Journal of hydrologic engineering*, **13**, 981-986.
- 701 Jakeman AJ, Hornberger GM (1993) How much complexity is warranted in a rainfall-runoff  
 702 model? *Water Resources Research*, **29**, 2637-2649.
- 703 Jakeman AJ, Letcher RA (2003) Integrated assessment and modelling: features, principles and  
 704 examples for catchment management. *Environmental Modelling & Software*, **18**, 491-  
 705 501.
- 706 Jakeman AJ, Letcher RA, Norton JP (2006) Ten iterative steps in development and evaluation of  
 707 environmental models. *Environmental Modelling & Software*, **21**, 602-614.

- 708 Jarritt NP, Lawrence DSL (2007) Fine sediment delivery and transfer in lowland catchments:  
 709 modelling suspended sediment concentrations in response to hydrological forcing.  
 710 *Hydrological Processes*, **21**, 2729-2744.
- 711 Jarvie HP, Sharpley AN, Spears B, Buda AR, May L, Kleinman PJA (2013a) Water Quality  
 712 Remediation Faces Unprecedented Challenges from “Legacy Phosphorus”.  
 713 *Environmental Science & Technology*, **47**, 8997-8998.
- 714 Jarvie HP, Sharpley AN, Withers PJA, Scott JT, Haggard BE, Neal C (2013b) Phosphorus  
 715 Mitigation to Control River Eutrophication: Murky Waters, Inconvenient Truths, and  
 716 “Postnormal” Science. *J. Environ. Qual.*, **42**, 295-304.
- 717 Jin L, Whitehead PG, Sarkar S *et al.* (2015) Assessing the impacts of climate change and socio-  
 718 economic changes on flow and phosphorus flux in the Ganga river system.  
 719 *Environmental Science: Processes & Impacts*, **17**, 1098-1110.
- 720 Jordan-Meille L, Rubæk GH, Ehlert PaI *et al.* (2012) An overview of fertilizer-P  
 721 recommendations in Europe: soil testing, calibration and fertilizer recommendations. *Soil*  
 722 *Use and Management*, **28**, 419-435.
- 723 Kavetski D, Clark MP (2011) Numerical troubles in conceptual hydrology: Approximations,  
 724 absurdities and impact on hypothesis testing. *Hydrological Processes*, **25**, 661-670.
- 725 Kavetski D, Kuczera G, Franks SW (2006a) Calibration of conceptual hydrological models  
 726 revisited: 1. Overcoming numerical artefacts. *Journal of Hydrology*, **320**, 173-186.
- 727 Kavetski D, Kuczera G, Franks SW (2006b) Calibration of conceptual hydrological models  
 728 revisited: 2. Improving optimisation and analysis. *Journal of Hydrology*, **320**, 187-201.
- 729 Kinnell PIA (2010) Event soil loss, runoff and the Universal Soil Loss Equation family of  
 730 models: A review. *Journal of Hydrology*, **385**, 384-397.
- 731 Kirchner JW (2006) Getting the right answers for the right reasons: Linking measurements,  
 732 analyses, and models to advance the science of hydrology. *Water Resources Research*,  
 733 **42**, W03S04.
- 734 Kleinman P, Sharpley A, Buda A, McDowell R, Allen A (2011) Soil controls of phosphorus in  
 735 runoff: Management barriers and opportunities. *Canadian Journal of Soil Science*, **91**,  
 736 329-338.
- 737 Krueger T, Freer J, Quinton JN, Macleod CJA (2007) Processes affecting transfer of sediment  
 738 and colloids, with associated phosphorus, from intensively farmed grasslands: a critical  
 739 note on modelling of phosphorus transfers. *Hydrological Processes*, **21**, 557-562.
- 740 Lazar AN, Butterfield D, Futter MN *et al.* (2010) An assessment of the fine sediment dynamics  
 741 in an upland river system: INCA-Sed modifications and implications for fisheries.  
 742 *Science of the Total Environment*, **408**, 2555-2566.
- 743 Lefrançois J, Grimaldi C, Gascuel-Oudou C, Gilliet N (2007) Suspended sediment and discharge  
 744 relationships to identify bank degradation as a main sediment source on small agricultural  
 745 catchments. *Hydrological Processes*, **21**, 2923-2933.
- 746 Leopold LB, Maddock Jr T (1953) The hydraulic geometry of stream channels and some  
 747 physiographic implications. pp Page.
- 748 Lindström G, Pers C, Rosberg J, Strömquist J, Arheimer B (2010) Development and testing of  
 749 the HYPE (Hydrological Predictions for the Environment) water quality model for  
 750 different spatial scales. *Hydrology research*, **41**, 295-319.
- 751 Luo Y, Arnold J, Allen P, Chen X (2012) Baseflow simulation using SWAT model in an inland  
 752 river basin in Tianshan Mountains, Northwest China. *Hydrol. Earth Syst. Sci.*, **16**, 1259-  
 753 1267.

- 754 Mackay DJ (2003) *Information theory, inference and learning algorithms*, Cambridge university  
755 press.
- 756 Martin-Ortega J, Perni A, Jackson-Blake L *et al.* (2015) A transdisciplinary approach to the  
757 economic analysis of the European Water Framework Directive. *Ecological Economics*,  
758 **116**, 34-45.
- 759 Mccollum RE (1991) Buildup and Decline in Soil Phosphorus: 30-Year Trends on a Typic  
760 Umprabuult. *Agronomy Journal*, **83**, 77-85.
- 761 Mccray JE, Kirkland SL, Siegrist RL, Thyne GD (2005) Model Parameters for Simulating Fate  
762 and Transport of On-Site Wastewater Nutrients. *Ground Water*, **43**, 628-639.
- 763 Menzel R (1980) Enrichment ratios for water quality modeling. *CREAMS: A Field-Scale Model  
764 for Chemicals, Runoff, and Erosion from Agricultural Management Systems  
765 Conservation Research Report Number 26, May, 1980. p 486-492, 1 Fig, 2 Tab, 11 Ref.*
- 766 Merritt WS, Letcher RA, Jakeman AJ (2003) A review of erosion and sediment transport  
767 models. *Environmental Modelling & Software*, **18**, 761-799.
- 768 Messiga AJ, Ziadi N, Plénet D, Parent LE, Morel C (2010) Long-term changes in soil  
769 phosphorus status related to P budgets under maize monoculture and mineral P  
770 fertilization. *Soil Use and Management*, **26**, 354-364.
- 771 Mooij WM, Trolle D, Jeppesen E *et al.* (2010) Challenges and opportunities for integrating lake  
772 ecosystem modelling approaches. *Aquatic Ecology*, **44**, 633-667.
- 773 Neal C, Jarvie HP (2005) Agriculture, community, river eutrophication and the Water  
774 Framework Directive. *Hydrological Processes*, **19**, 1895-1901.
- 775 Oeurng C, Sauvage S, Sánchez-Pérez J-M (2010) Dynamics of suspended sediment transport and  
776 yield in a large agricultural catchment, southwest France. *Earth Surface Processes and  
777 Landforms*, **35**, 1289-1301.
- 778 Oreskes N, Belitz K (2001) Philosophical issues in model assessment. *Model validation:  
779 Perspectives in hydrological science*, **23**.
- 780 Panagos P, Borrelli P, Meusburger K, Alewell C, Lugato E, Montanarella L (2015) Estimating  
781 the soil erosion cover-management factor at the European scale. *Land Use Policy*, **48**, 38-  
782 50.
- 783 Pappenberger F, Beven K, Frodsham K, Romanowicz R, Matgen P (2007) Grasping the  
784 unavoidable subjectivity in calibration of flood inundation models: A vulnerability  
785 weighted approach. *Journal of Hydrology*, **333**, 275-287.
- 786 Perrin C, Michel C, Andréassian V (2001) Does a large number of parameters enhance model  
787 performance? Comparative assessment of common catchment model structures on 429  
788 catchments. *Journal of Hydrology*, **242**, 275-301.
- 789 Radcliffe DE, Cabrera ML (2006) *Modeling phosphorus in the environment*, CRC Press.
- 790 Radcliffe DE, Freer J, Schoumans O (2009) Diffuse Phosphorus Models in the United States and  
791 Europe: Their Usages, Scales, and Uncertainties. *J. Environ. Qual.*, **38**, 1956-1967.
- 792 Ratliff LF, Ritchie JT, Cassel DK (1983) Field-Measured Limits of Soil Water Availability as  
793 Related to Laboratory-Measured Properties1. *Soil Science Society of America Journal*,  
794 **47**.
- 795 Raue A, Kreutz C, Maiwald T, Bachmann J, Schilling M, Klingmüller U, Timmer J (2009)  
796 Structural and practical identifiability analysis of partially observed dynamical models by  
797 exploiting the profile likelihood. *Bioinformatics*, **25**, 1923-1929.
- 798 Renard KG, Foster GR, Weesies GA, Porter JP (1991) RUSLE: Revised universal soil loss  
799 equation. *Journal of soil and Water Conservation*, **46**, 30-33.

- 800 Robson BJ (2014) When do aquatic systems models provide useful predictions, what is  
801 changing, and what is next? *Environmental Modelling & Software*, **61**, 287-296.
- 802 Sample J (2015) Statistics notes for environmental modelling. pp Page, GitHub.
- 803 Schaeffli B, Gupta HV (2007) Do Nash values have value? *Hydrological Processes*, **21**, 2075-  
804 2080.
- 805 Seibert J (2003) Reliability of Model Predictions Outside Calibration Conditions. *Paper*  
806 *presented at the Nordic Hydrological Conference (Røros, Norway 4-7 August 2002)*, **34**,  
807 477-492.
- 808 Sharpley A, Jarvie HP, Buda A, May L, Spears B, Kleinman P (2013) Phosphorus Legacy:  
809 Overcoming the Effects of Past Management Practices to Mitigate Future Water Quality  
810 Impairment. *J. Environ. Qual.*, **42**, 1308-1326.
- 811 Sharpley AN (1980) The Enrichment of Soil Phosphorus in Runoff Sediments1. *J. Environ.*  
812 *Qual.*, **9**, 521-526.
- 813 Sivapalan M (2005) Pattern, process and function: elements of a unified theory of hydrology at  
814 the catchment scale. *Encyclopedia of hydrological sciences*.
- 815 Sivapalan M (2006) *Predictions in ungauged basins: promise and progress*, International Assn  
816 of Hydrological Sciences.
- 817 Spiegelhalter DJ, Best NG, Carlin BP, Van Der Linde A (2002) Bayesian measures of model  
818 complexity and fit. *Journal of the Royal Statistical Society: Series B (Statistical*  
819 *Methodology)*, **64**, 583-639.
- 820 Stollenwerk KG (1996) Simulation of phosphate transport in sewage-contaminated groundwater,  
821 Cape Cod, Massachusetts. *Applied Geochemistry*, **11**, 317-324.
- 822 Stutter MI, Demars BOL, Langan SJ (2010) River phosphorus cycling: Separating biotic and  
823 abiotic uptake during short-term changes in sewage effluent loading. *Water Research*, **44**,  
824 4425-4436.
- 825 Stutter MI, Langan SJ, Cooper RJ (2008) Spatial contributions of diffuse inputs and within-  
826 channel processes to the form of stream water phosphorus over storm events. *Journal of*  
827 *Hydrology*, **350**, 203-214.
- 828 Stutter MI, Langan SJ, Lumsdon DG, Clark LM (2009) Multi-element signatures of stream  
829 sediments and sources under moderate to low flow conditions. *Applied Geochemistry*, **24**,  
830 800-809.
- 831 Syers JK, Johnston AE, Curtin D (2008) Efficiency of soil and fertilizer phosphorus use.  
832 Reconciling changing concepts of soil phosphorus behaviour with agronomic  
833 information. In: *Fertilizer and plant nutrition bulletins*. pp Page, Rome, Food and  
834 Agriculture Organisation of the United Nations (FAO).
- 835 Trimble SW (2010) Streams, valleys and floodplains in the sediment cascade. *Sediment*  
836 *Cascades: An Integrated Approach*, 307-343.
- 837 Twarakavi NKC, Sakai M, Šimůnek J (2009) An objective analysis of the dynamic nature of  
838 field capacity. *Water Resources Research*, **45**, n/a-n/a.
- 839 Usda (2004) National Engineering Handbook, Part 630 - Hydrology, Chapter 11 (Snowmelt). pp  
840 Page, United States Department of Agriculture, Natural Resources Conservation Service.
- 841 Van Dijk A (2010) Climate and terrain factors explaining streamflow response and recession in  
842 Australian catchments. *Hydrology and Earth System Sciences*, **14**, 159-169.
- 843 Van Griensven A, Meixner T, Grunwald S, Bishop T, Diluzio M, Srinivasan R (2006) A global  
844 sensitivity analysis tool for the parameters of multi-variable catchment models. *Journal*  
845 *of Hydrology*, **324**, 10-23.

- 846 Van Meter KJ, Basu NB (2015) Catchment legacies and time lags: a parsimonious watershed  
847 model to predict the effects of legacy storage on nitrogen export. *PLoS one*, **10**, e0125971.
- 848 Wade AJ, Butterfield D, Griffiths T, Whitehead PG (2007) Eutrophication control in river-  
849 systems: an application of INCA-P to the River Lugg. *Hydrol. Earth Syst. Sci.*, **11**, 584-  
850 600.
- 851 Wade AJ, Durand P, Beaujouan V *et al.* (1999) A nitrogen model for European catchments:  
852 INCA, new model structure and equations. *Hydrol. Earth Syst. Sci.*, **6**, 559-582.
- 853 Wade AJ, Whitehead PG, Butterfield D (2002) The Integrated Catchments model of Phosphorus  
854 dynamics (INCA-P), a new approach for multiple source assessment in heterogeneous  
855 river systems: model structure and equations. *Hydrol. Earth Syst. Sci.*, **6**, 583-606.
- 856 Watson A, Evans R (2007) Water erosion of arable fields in North-East Scotland, 1985 – 2007.  
857 *Scottish Geographical Journal*, **123**, 107-121.
- 858 Wellen C, Kamran-Disfani A-R, Arhonditsis GB (2015) Evaluation of the Current State of  
859 Distributed Watershed Nutrient Water Quality Modeling. *Environmental Science &*  
860 *Technology*, **49**, 3278-3290.
- 861 Whitehead PG, Crossman J, Balana BB *et al.* (2013) A cost-effectiveness analysis of water  
862 security and water quality: impacts of climate and land-use change on the River Thames  
863 system. *Philosophical Transactions of the Royal Society A: Mathematical, Physical and*  
864 *Engineering Sciences*, **371**.
- 865 Whitehead PG, Wilson EJ, Butterfield D (1998) A semi-distributed Integrated Nitrogen model  
866 for multiple source assessment in Catchments (INCA): Part I — model structure and  
867 process equations. *Science of the Total Environment*, **210–211**, 547-558.
- 868 Wischmeier WC, Smith DD (1965) *Predicting rainfall-erosion losses from cropland east of the*  
869 *Rocky Mountains.*, Washington DC, US Department of Agriculture (USDA).
- 870 Wischmeier WC, Smith DD (1978) *Predicting rainfall erosion losses - a guide to conservation*  
871 *planning*, Washington DC, US Department of Agriculture (USDA).
- 872 Wittenberg H (1999) Baseflow recession and recharge as nonlinear storage processes.  
873 *Hydrological Processes*, **13**, 715-726.
- 874 Wolman M, Miller J, Leopold L (1964) Fluvial processes in geomorphology. *San Francisco*.
- 875 Young RA, Onstad C, Bosch D, Anderson W (1989) AGNPS: A nonpoint-source pollution  
876 model for evaluating agricultural watersheds. *Journal of soil and water conservation*, **44**,  
877 168-173.

878

879

880 Table 1: SimplyP model parameters, including default values, recommended ranges and possible  
 881 data sources. ‘Spatial’ column describes whether the parameter varies spatially by land use (LU),  
 882 in which case by which LU type (A: agricultural, S: semi-natural, Ar: arable, IG: improved  
 883 grassland), or sub-catchment/reach (SC/R). Parameters likely to be key in most settings are  
 884 marked with an asterisk. Many of those without an asterisk are optional. Q is discharge.

Type	Param	Units	Description	Spatial	Tarland	Default	Min	Max	Data sources
Snow	D <sub>snow,0</sub>	mm	Initial snow depth	–	0	0	0	1000	Meteorological records
	f <sub>DSDM</sub>	mm dd°C <sup>-1</sup>	Degree-day factor for snow melt	–	2.74	2.74	1.6	6	Literature, e.g. USDA (2004)
Hydrology	*T <sub>s</sub>	days	Soil water time constant	LU (A, S)	A: 2 S: 10	A: 1 S: 10	> 0	30	Calibration
	f <sub>quick</sub>	none	Proportion of precipitation routed to quick flow	–	0.02	0.02	0	0.2	Calibration
	alpha	none	PET reduction factor	–	1	1	0.4	1.2	Literature, e.g. Allen <i>et al.</i> (1998)
	*FC	mm	Soil field capacity	–	290	300	100	400	Soils database, or from soil texture using conversion charts (e.g. Appendix, Figure A1)
	*beta	none	Baseflow index	–	0.70	0.60	0	1	Local or global databases (e.g. Beck <i>et al.</i> , 2013)
	*T <sub>g</sub>	days	Baseflow recession constant	–	65	65	> 0	100	May be estimated from Q data using methods of Van Dijk (2010); see Beck <i>et al.</i> (2013) for a global analysis
	Q <sub>g,min</sub> a	mm d <sup>-1</sup> m <sup>-2</sup>	Minimum groundwater flow Gradient of stream velocity-Q relationship	– –	0.4 0.5	0.0 0.5	0 0.1	2 0.8	Calibration Empirically-derived from paired velocity and Q measurements (e.g. from flow gauging)
Q <sub>r0_init</sub>	m <sup>3</sup> s <sup>-1</sup>	Initial in-stream Q	–	1.0	1.0	> 0	N/A	Q observations	
Sediment	C <sub>cover</sub>	None	Vegetation cover factor (ratio of erosion rates under the land class vs bare soil)	LU (Ar, IG, S)	A: 0.2 S: 0.021 IG: 0.09	A: 0.2 S: 0.021 IG: 0.09	0	1	(R)USLE literature, e.g. Panagos <i>et al.</i> (2015)
	*E <sub>M</sub>	kg mm <sup>-1</sup>	Sediment input scaling factor	–	1500	1500	0	5000	Calibration
	*k <sub>M</sub>	none	Sediment input non-linear coefficient	–	2.0	2.0	1.2	3	Empirical relationship between Q and SS observations or literature (e.g. Asselman, 2000)
	d <sub>maxE,spr</sub>	none	Julian day with max erodibility; spring-sown crops	–	60	60	1	365	Local agronomic practices
	d <sub>maxE,aut</sub>	none	Julian day with max erodibility, autumn-sown crops	–	304	304	1	365	Local agronomic practices
Dissolved P	*P <sub>soilConc</sub> <sub>l</sub>	mg kg <sup>-1</sup>	Initial total soil P content	LU (A, S)	A: 1458 S: 873	A: 1458 S: 873	0- 400	>300 0	Soils database. Estimate from soil test P data using an empirical relationship
	*P <sub>netInput</sub>	kg ha <sup>-1</sup> yr <sup>-1</sup>	Net annual P input to the soil (negative if uptake > input); S fixed at 0	LU (A)	10	10	-30	30	Fertilizer and manure application surveys, literature for P uptake, national P balance inventories (e.g. eurostat, 2013, for EU countries)
	*EPC <sub>0,ini</sub> <sub>t</sub>	mg l <sup>-1</sup>	Initial soil water TDP concentration on agricultural land	LU (A)	0.1	0.1	0	2	Direct measurements, literature
	*M <sub>soil,m2</sub>	kg m <sup>-2</sup>	Soil mass per m <sup>2</sup> , important in determining the initial soil labile P mass	–	95	100	>0	800	Soils data (bulk density and depth)



Type	Param	Units	Description	Spatial	Tarland	Default	Min	Max	Data sources
	*TDP <sub>eff</sub>	kg day <sup>-1</sup>	Reach effluent TDP inputs	SC/R	0.1	0	0	N/A	Water company/environment protection agency data Direct measurements or literature
	*TDP <sub>g</sub>	mg l <sup>-1</sup>	Groundwater TDP concentration	–	0.02	0	0	2	
PP	*E <sub>pp</sub>	none	PP enrichment factor	–	1.6	1	1	6	Direct measurements or literature (e.g. Sharpley, 1980)

885 Table 2: Comparison of numbers of model parameters required for SimplyP and INCA-P.

Category	INCA-P (excluding hydrology model parameters)	SimplyP
Total, no spatial variability	138	23
Total, with spatial variability (land class)	146	24 – 27
Parameters that vary by sub-catchment and/or reach	64	1
Not measurable (purely calibrated)	43	4 or 5
Additional parameters held constant over land use/reach/sub-catchment	12	4
Parameters used in the study catchment	48 (additional 45 to simplify the setup by removing processes)	22

886

887 Table 3: Model performance statistics in the calibration and validation period.

Variable	Model	Calibration					Validation				
		n <sup>a</sup>	Bias (%)	SR <sup>b</sup>	NS <sup>c</sup>	NS (logs) <sup>c</sup>	n <sup>a</sup>	Bias (%)	SR <sup>b</sup>	NS <sup>c</sup>	NS (logs) <sup>c</sup>
Q	SimplyP	716	0	0.92	0.80	0.81	3213	12	0.87	0.73	0.72
	INCA-P		0	0.91	0.73	0.79		12	0.87	0.55	0.72
SS	SimplyP	448	-6	0.54	0.13	0.10	189	-27	0.23	0.13	-0.10
	INCA-P		-16	0.46	0.02	0.34		-43	0.31	0.05	0.33
TP	SimplyP	428	0	0.25	0.16	-0.01	0				
	INCA-P		-14	0.37	0.07	0.13					
PP	SimplyP	428	-3	0.19	0.10	-0.27	0				
	INCA-P		-43	0.28	0.01	-0.06					
TDP	SimplyP	449	0	0.41	0.12	0.05	105	-11	0.54	0.15	0.22
	INCA-P		9	0.34	-0.24	-0.14		7	0.44	0.10	0.17

888 <sup>a</sup>Number of observations, <sup>b</sup>Spearman's Rank correlation coefficient, <sup>c</sup>Nash Sutcliffe efficiency of  
889 untransformed or logged data. NS are only provided for water quality parameters for  
890 comparability with other studies.

891

892 Figure 1: Schematic of the main stores, processes and pathways included in the model. White  
893 boxes show the state variables whose volume (water) or mass (sediment, P species) is tracked.  
894 Variables within small grey boxes are implicitly included in the model, but are not tracked.  
895 Arrows show fluxes within and between compartments. P: phosphorus, SS: suspended sediment,  
896 TDP: total dissolved P, PP: particulate P, ET: evapotranspiration.

897 Figure 2: The Tarland catchment, with simplified land use, the location of effluent inputs and  
898 monitoring points, and the sub-catchments used in the INCA-P application. Eastings and  
899 northings (km) are relative to the British National Grid.

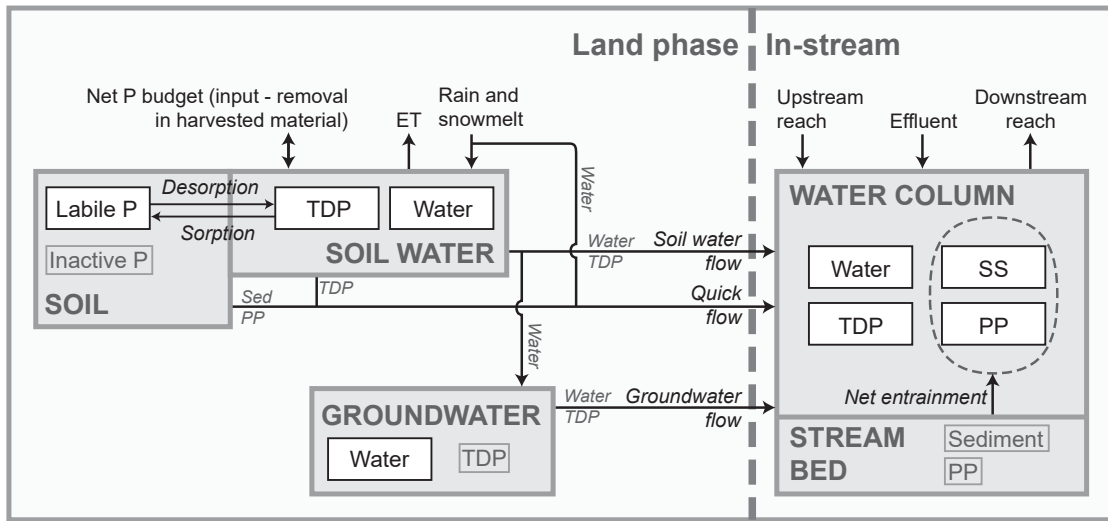
900 Figure 3: Q-Q plots for the calibration and validation periods. Quantiles of the simulated data are  
901 plotted against corresponding quantiles of the observed data; if observed and simulated data are  
902 from similar distributions, points will lie close to the 1:1 line. Median and interquartile ranges  
903 (IQR) are shown. Units are  $\text{mg l}^{-1}$  for suspended sediment (SS) and  $\mu\text{g l}^{-1}$  for all P species. Note  
904 log scales.

905 Figure 4: Time series of observed and simulated discharge (Q) and water quality during the  
906 calibration period. Note the log scales for SS, PP and TP.

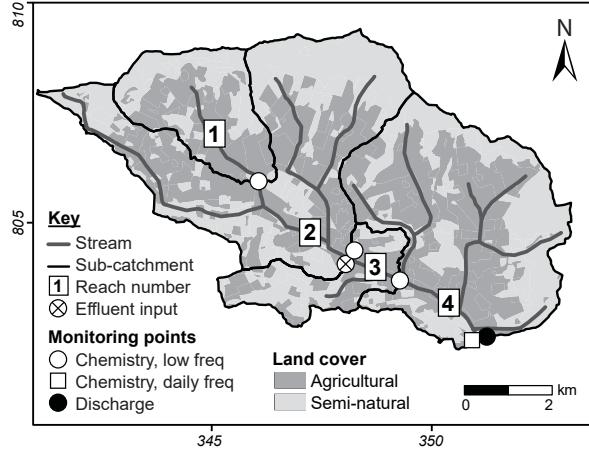
907 Figure 5: Time series of observed and simulated discharge (Q) and water quality during the  
908 validation period. Note the log scales for SS, PP and TP.

909 Figure 6: Simulated changes over a 30-year period in (a) agricultural soil water  $EPC_0$  (the  
910 equilibrium phosphorus concentration, closely linked to soil water TDP concentration), and (b)  
911 in-stream mean TDP concentration, comparing the first and last 5 years of the study period.  
912 Results are shown for baseline 'business as usual' inputs and for three fertilizer and manure  
913 reduction scenarios (reductions of 25%, 50% and 100%).

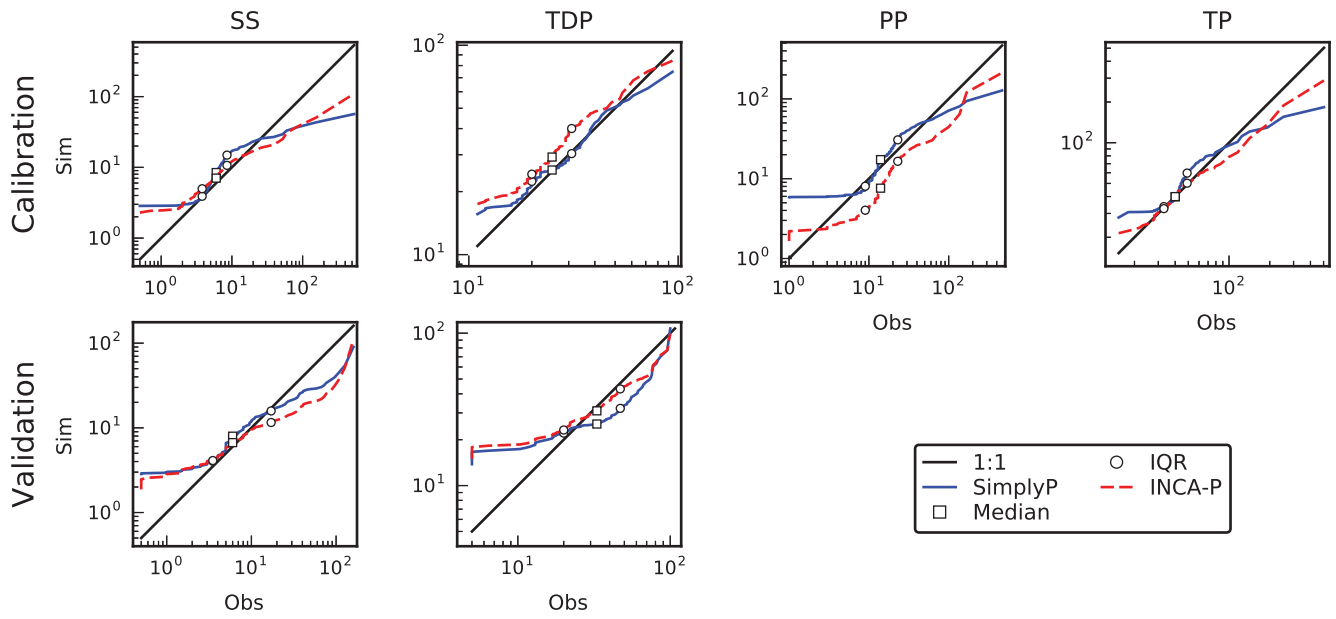
**Figure 1.**



**Figure 2.**

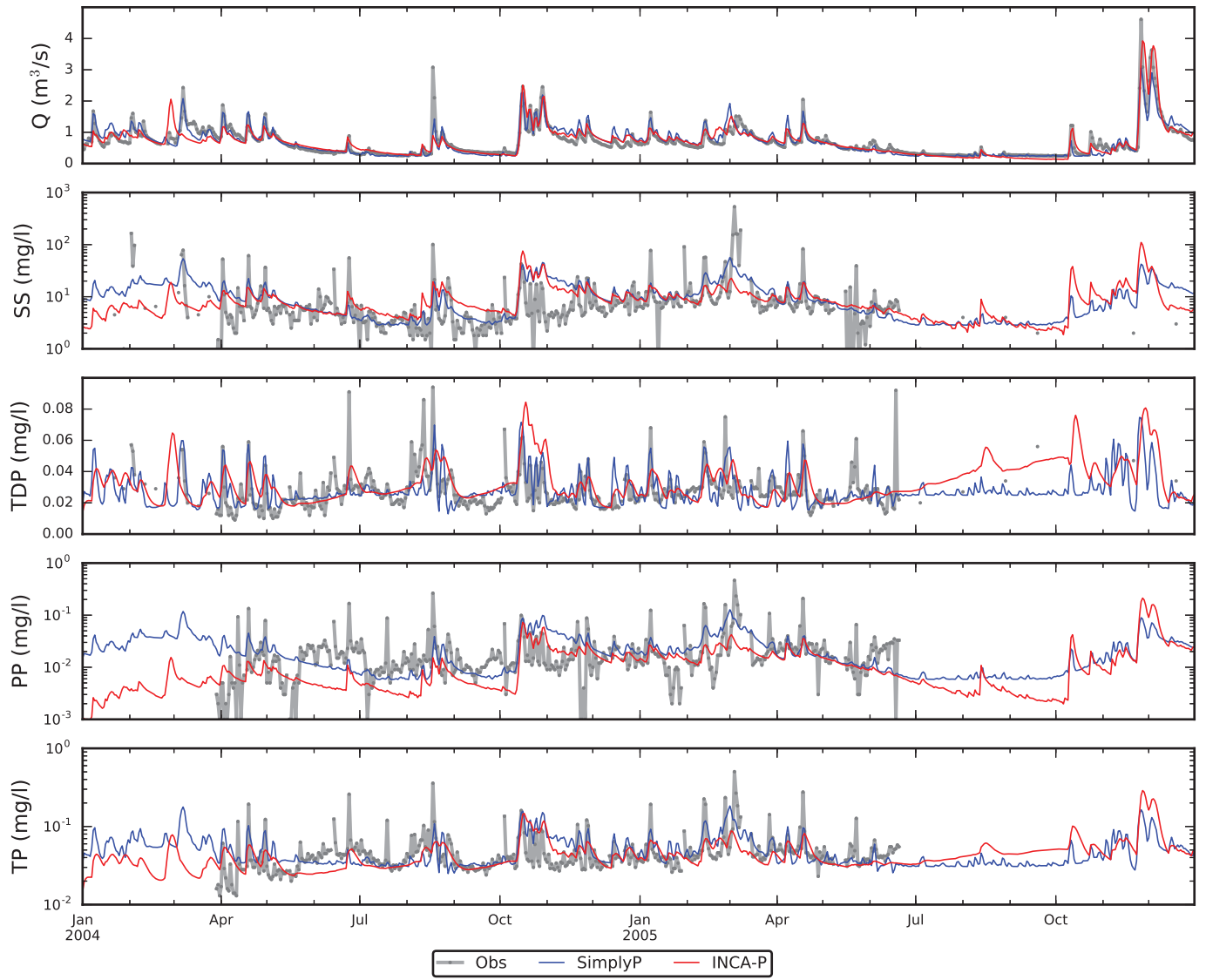


**Figure 3.**

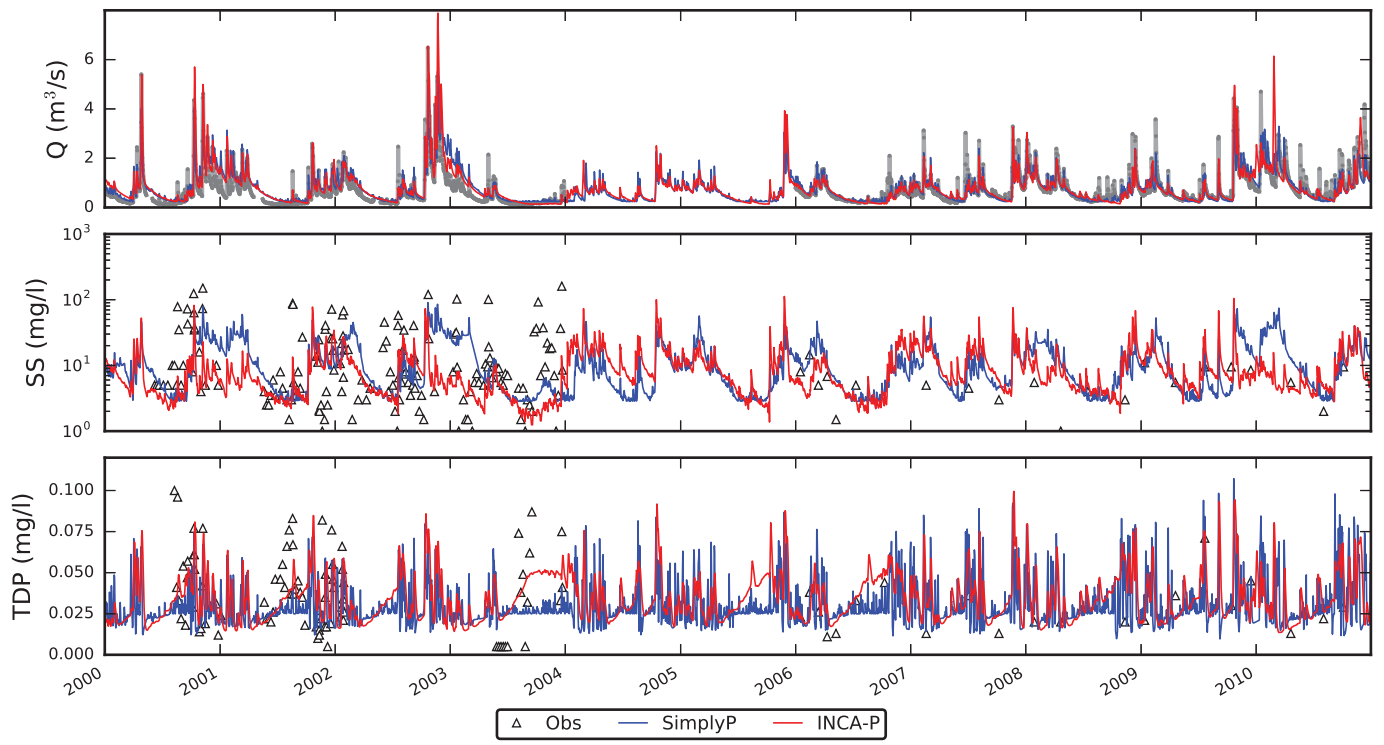




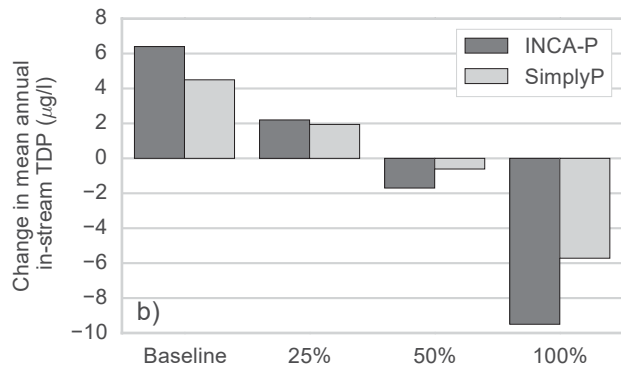
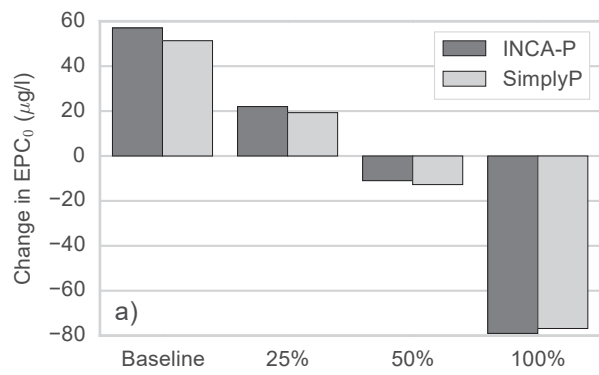
**Figure 4.**



**Figure 5.**



**Figure 6.**



## **Are our dynamic water quality models too complex? A comparison of a new parsimonious phosphorus model, SimplyP, and INCA-P**

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### **Contents of this file**

Text S1

### **Introduction**

This supplementary information contains a full description of the SimplyP model, a newly-developed parsimonious catchment-scale dynamic water quality model for simulating hydrology, phosphorus and sediment dynamics in catchments. The model was originally developed in 2015 at the James Hutton Institute (Scotland), as part of L. Jackson-Blake's PhD. In the following document, a full description is provided of model aims, scope and scale, the processes and equations included in SimplyP v1.0 and the underlying scientific rationale, a description of numerical methods used to solve the equations, and a suggestion of model development priorities.

# SimplyP v1.0 model description

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## 1. Introduction

SimplyP is a parsimonious catchment-scale dynamic water quality model, which simulates hydrology, phosphorus (P) and sediment dynamics in catchments. The model was originally developed in 2015 at the James Hutton Institute (Scotland), as part of L. Jackson-Blake's PhD. The model is under development, lead by NIVA (Norway), with input from the James Hutton Institute. Here, we present model aims, scope and scale (Section 3) and give a detailed overview of the processes and equations included in SimplyP v1.0, as well as the underlying scientific rationale. A suggestion of model development priorities is provided in Section 5.

## 2. Model availability

SimplyP v1.0 model code is open source (<https://github.com/LeahJB/SimplyP>). Running the model requires a Python installation able to run iPython notebooks (e.g. WinPython; <http://winpython.sourceforge.net/>); instructions for installing WinPython and running the model using an example dataset are provided in the GitHub repository. Model parameters are input to the model via a simple Excel interface; recommendations for default, minimum and maximum values and potential data sources are provided in Table 11.

## 3. Model aims, scope and scale

### 3.1 Model aims

SimplyP aims to be process-based, i.e. model equations reflect hypotheses about the processes governing system behaviour. The aim in developing SimplyP was to minimize the process representation to only those processes that appear to control the catchment response, whilst maintaining the flexibility and functionality required for the model to be useful in hypothesis and scenario testing. The process representation aims to be simple enough to allow parameter values to be constrained using available observational data. What is presented here is a first prototype, the aim being to attempt a proof-of-concept that simple can be as good as complex. The hope is that this simple model could provide a useful benchmark when choosing between different models, or, after further testing, be a useful modelling tool in its own right.

SimplyP was developed with a number of potential uses in mind, including: (1) interpolation of sparse monitoring data, to provide more ecologically-relevant in-stream phosphorus concentrations or more accurate estimates of loads delivered downstream to lakes or estuaries; (2) hypothesis testing and highlighting knowledge and data gaps. This in turn could be used to help design monitoring programmes, highlight experimental needs, and prioritise areas for future model development; (3) exploring the potential response of the system to future change, especially in terms of anticipated storm and low-flow dynamics; and (4) providing evidence to support decision-making, for example to help set water quality and load reduction goals and to advise on the best means of achieving those goals.

A particular requirement at present is for models which can predict time lags in the system due to stores of 'legacy' P, P which has accumulated in the catchment along transport pathways in the land-freshwater continuum. These legacy P stores may become net sources of P if inputs to the store are reduced, potentially confounding management efforts aimed at reducing in-stream P concentrations (Sharpley et al., 2013). Stores of legacy P include: (1) soil P, from historic applications of fertilizer and manure in excess of crop requirements; (2) terrestrial sediment-bound P, stored in areas where local topography promotes sediment deposition; (3) groundwater P, due to percolation of P-rich water from agriculture or sewage; (4) P in up-stream impoundments (e.g. lakes, reservoirs and canals); and (5) P in in-stream bed sediments. The latter may be sourced from the deposition of particulate P in areas of slower flow (e.g. pools, floodplains), or from the adsorption of dissolved P from the water column, particularly downstream of sewage treatment works. The aim here is for the model to reproduce the first of these stores, soil P, as this is often the largest and the most pervasive legacy source of P to the environment (Jarvie et al., 2013a; Kleinman et al., 2011; Sharpley et

al., 2013). The remaining legacy P stores are beyond the scope of this initial version of the model, though recommendations are provided for how more legacy P sources could be incorporated.

In the future, it is likely that well-devised auto-calibration and uncertainty analysis routines will become prerequisites for model applications. To date, attempts to bring about a shift in modeller behaviour have focused on improving algorithms and making them more available, but have largely over-looked other important barriers such as the subjectivity of the analyses (Jackson-Blake and Starrfelt, 2015) and the often prohibitively large amounts of time required to set up and conduct such analyses. We believe that the use of auto-calibration and uncertainty analysis tools would increase substantially if more attention were paid to: (1) developing models with fewer parameters, so all uncertain parameters can be included in an analysis; (2) reducing the number of interacting parameters, to reduce non-identifiability issues and the need for time-consuming *ad hoc* code to be written; and (3) maximising the number of parameters which can in principle be measured, and therefore given informative priors. SimplyP was developed with these three aims in mind. In practice, the number of parameters that can be calibrated in a given study area depends on data available for model calibration and for constraining model parameters to plausible ranges. However, studies have rarely successfully explored more than 40-dimensional parameter spaces (e.g. Dean et al., 2009; Jackson-Blake and Starrfelt, 2015; Starrfelt and Kaste, 2014), so an upper limit of 40 parameters was decided on.

### 3.2 Model temporal and spatial scale

The model is dynamic and currently runs at a daily time step, short enough to capture much of the variability in catchment hydrology and the associated delivery of dissolved and particulate matter to the water course, yet not so short that computing run times become prohibitively long when the model is run to explore longer term trends. A daily time step is also compatible with the majority of widely-available meteorological data sets used to drive the model.

The model is spatially semi-distributed, as a compromise between the complexity of fully-distributed methodologies and the lack of spatial process representation in fully lumped models. The catchment is broken down into perceived biophysical regions, thereby allowing a certain amount of the spatial variability in processes and outputs to be simulated, whilst reducing input data requirements and computing run times. The main disadvantage compared to fully-distributed models is that the interconnectedness of different parts of the landscape is not included, but in most areas this is justified by the lack of input data for a finer-scale division of the landscape and the reduced computing run times. The catchment area may be split into:

1. *Sub-catchments and associated reaches*, which should be defined based on the presence of monitoring stations, sewage treatment work inputs, or major changes in terrestrial conditions such as geology, topography or soil type. The model is run for each sub-catchment in turn, and reach outputs are fed sequentially down-stream.
2. *Grouped soil properties and broad land management, termed the land class*. A summary of the land class sub-divisions is given in Table 1. For dissolved P processes, two land classes are considered, a ‘*high P*’ class and a ‘*low P*’ class. Land within a class should have a similar annual P budget, soil P content and hydrological characteristics, or area-weighted properties should be used. A third optional ‘*newly-converted*’ class may also be included, to take into account legacy soil P when land use conversion occurs, or the lack of legacy soil P in new agricultural land. For sediment and particulate P processes, the high P class may be further sub-divided in two to account for differences in erodibility (e.g. agricultural land could be split into improved grassland and arable land). Finally, the proportion of spring versus autumn-sown crops that make up any arable land may be taken into account when calculating the variation in soil erodibility due to plant cover through time.

In highly agricultural areas where there is no ‘low P’ land, if the model is to be used to explore impacts of changing fertilizer or manure inputs or land use, the expected inactive P content for semi-

natural land in the area must still be provided, to provide a reference point for the P enrichment of agricultural soils, but the ‘low P’ class coverage of the catchment would be set to zero.

Processes	Landscape division		
Dissolved P	High P <i>e.g. arable land, improved grassland</i>		Low P <i>e.g. unfertilized forest, moorland, rough grassland</i>
Sediment & particulate P	High P		Low P
	High erodibility* <i>e.g. arable</i>	Low erodibility* <i>e.g. improved grassland</i>	
	Spring-sown*	Winter-sown*	

Table 1: Land class sub-divisions available for use in SimplyP. These differ according to the process being simulated (dissolved or particulate phosphorus processes). \*Optional

#### 4. SimplyP model structure and equations

A summary of the main stores and fluxes of water, sediment and P is provided in Figure 1. The model includes the following components:

- A snow accumulation and melt model (Section 4.1.1)
- Rainfall-runoff (Section 4.1.2) and in-stream hydrology (Section 4.1.3)
- Sediment delivery to the watercourse and in-stream transport (Section 4.2)
- Terrestrial and in-stream P processes (Section 0)

Dissolved and particulate P are simulated separately as total dissolved P (TDP) and particulate P (PP). PP is assumed to be sediment-bound and no distinction is made between organic and mineral P.

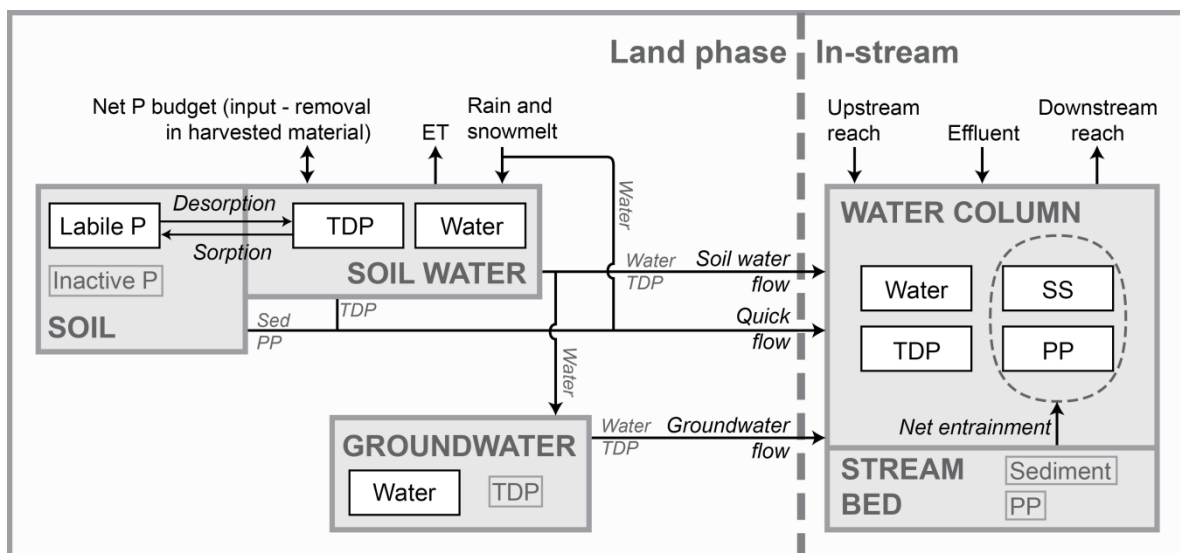


Figure 1: Schematic of the main stores, processes and pathways included in the model. White boxes show the state variables whose volume (water) or mass (sediment, P species) is tracked. Arrows show fluxes within and between compartments. P: phosphorus, SS: suspended sediment, TDP: total dissolved P, PP: particulate P, ET: evapotranspiration.

#### 4.1 Hydrology

##### 4.1.1 Hydrological inputs

Input time series of precipitation and potential evapotranspiration (PET) are required. If the snow module is not used, then these are used to drive hydrological processes in the model. If the snow accumulation and melt

module is used, then air temperature must also be supplied, and a time series of rain plus snowmelt is calculated and used to drive hydrological processes in the model. Parameters and variables used in the hydrological input equations are defined in Table 2.

Variable	Description	Units	Source
$D_{snow}$	Snowpack depth	mm	Equation 3
$D_{snow,0}$	Initial snowpack depth	mm	Input parameter
$f_{DDSM}$	Degree-day factor for snowmelt	mm/degree-day °C	Input parameter
$P$	Hydrological input to the model	mm day <sup>-1</sup>	Equation 4
$P_{melt,max}$	Potential maximum snowmelt	mm day <sup>-1</sup>	Equation 2
$P_{rain}$	Precipitation as rain	mm day <sup>-1</sup>	Equation 1
$P_{snow}$	Precipitation as snow	mm day <sup>-1</sup>	Equation 1
$P_{total}$	Total precipitation	mm day <sup>-1</sup>	Input time series
$T_{air}$	Mean daily air temperature	°C	Input time series

Table 2: Parameters and variables used in calculating hydrological inputs to the model

Within the snow model, precipitation falls as snow when the mean daily air temperature is below 0°C (Equation 1). Potential daily snow melt is calculated using a simple degree-day factor method (USDA, 2004), assuming that melting begins once the air temperature rises above 0°C (Equation 2). Both temperature thresholds are hard-coded into the model at present, but could be readily converted to user-supplied parameters. The degree-day approach to simulating snow melt is one of the simplest formulations. Key limitations are discussed in USDA (2004), in particular: (1) the degree-day factor is assumed to be constant, whilst in reality it varies seasonally and by location; (2) snow melt is only controlled by temperature, and therefore ignores important factors such as snow density; and (3) it is not valid for rain-on-snow events.

Equation 1: Partitioning of total precipitation into rain,  $P_{rain}$ , and snow,  $P_{snow}$  (mm day<sup>-1</sup>)

$$\begin{aligned} \text{When } T_{air} > 0: P_{rain} &= P_{total}, P_{snow} = 0 \\ \text{Otherwise: } P_{rain} &= 0, P_{snow} = P_{total} \end{aligned}$$

Equation 2: Potential daily snowmelt,  $P_{melt,max}$  (mm day<sup>-1</sup>)

$$\text{When } T_{air} > 0: P_{melt,max} = f_{DDSM}(T_{air} - 0)$$

Snow pack depth is then calculated as initial depth plus the change due to snowfall and snowmelt, with the latter limited by the snow pack depth (Equation 3). As snowfall and melt are constant over a day, there is no need for Equation 3 to be formulated as a differential equation. Finally, the sum of rain and snowmelt is used as input to the hydrology model (Equation 4).

Equation 3: Snow pack depth,  $D_{snow}$  (mm), where superscript  $t$  denotes the current time step, and  $t-1$  the previous time step. This calculation requires a user-supplied initial snowpack depth,  $D_{snow,0}$

$$D_{snow}^t = D_{snow}^{t-1} + P_{snow}^t - \text{minimum}(P_{melt,max}^t, D_{snow}^{t-1})$$

Equation 4: Hydrological inputs to the model,  $P$  (mm day<sup>-1</sup>)

$$P = P_{rain} + P_{melt}$$

An example of output from the snow module for the Tarland Burn catchment for the period 2004-2005 is shown in Figure 2.

The snow model uses mean daily air temperature as input, which could lead to under- or over-estimation of snowfall and snowmelt. In areas where there is significant winter accumulation of snow, a possible future modification to the model would be to use a more sophisticated representation of temperature variation throughout a day, for example using a triangular or a sinusoidal shape.

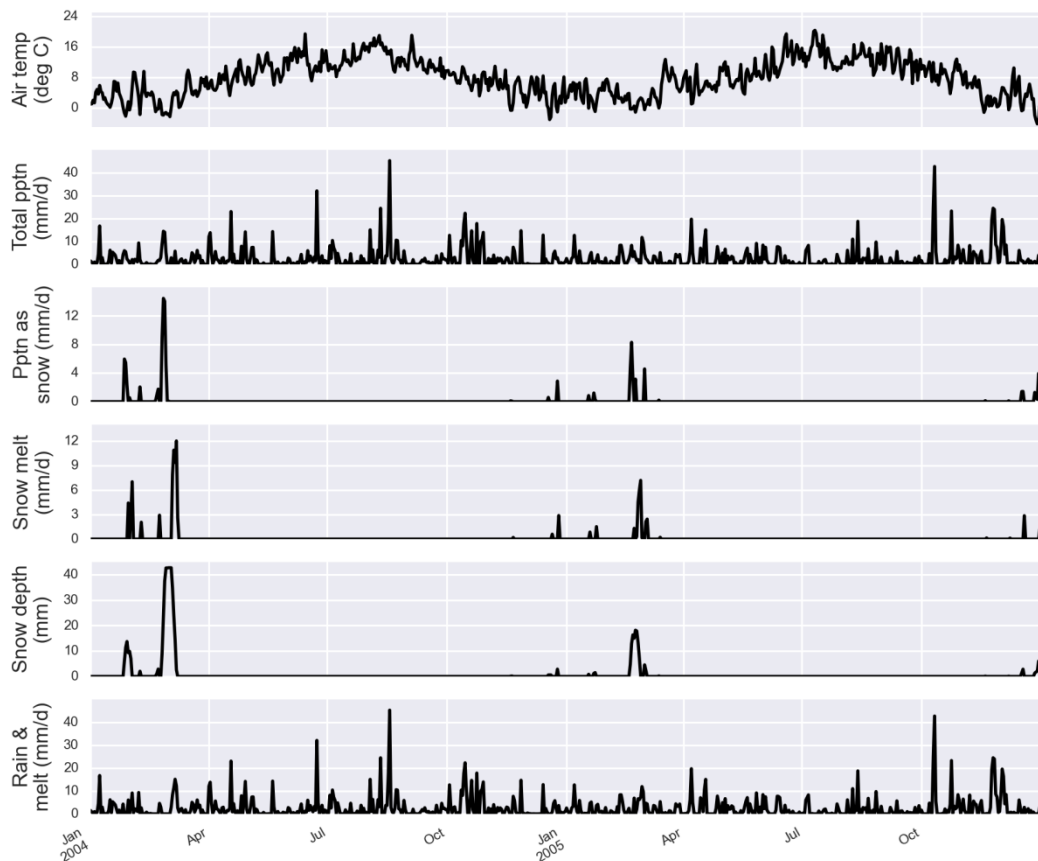


Figure 2: Inputs to and outputs from the snow accumulation and melt module, using input data for the Tarland Burn catchment. 'Pptn' is precipitation. Snow depths are given as mm of water equivalent.

#### 4.1.2 Terrestrial hydrology

A hydrology model provides the foundation for any water quality model, as the flow of water transports matter from the land to the stream. To simulate hydrology alone, simple models may be appropriate, with just a couple of calibration parameters (e.g. IHACRES, Croke et al., 2006). However, to be able to simulate the transport of both dissolved and particulate P under varying flow conditions, a slightly more complex representation of terrestrial hydrology is needed. Here, three terrestrial flow paths are taken into account: (1) quick flow, to simulate water, sediment and P inputs to the watercourse during larger rainfall events and when soils are dry (and therefore little soil water flow occurs); (2) soil water flow, responsible for TDP leaching from soils and groundwater recharge, and (3) groundwater flow, which is important for baseflow P concentrations.

The soil water and groundwater equations used were based on those described by Sample (2015), who provides a full description of their derivation (last accessed March 2016). For convenience, volumes and fluxes are expressed as water depths per unit area in units of mm or  $\text{mm day}^{-1}$ . Associated real volumes can be derived by multiplying by the catchment area,  $A_{SC}$  ( $\text{km}^2$ ), with unit conversions:  $1 \text{ m}^3 = 10^3 A_{SC} \text{ mm}$ . Parameters and variables used in the terrestrial hydrology equations are defined in Table 3.

Variable	Description	Units	Source
$\alpha$	Potential evapotranspiration correction factor	none	Input parameter
$\beta$	Base flow index	none	Input parameter
$dQ_g/dt$	Change in groundwater flow with time	mm day <sup>-1</sup> day <sup>-1</sup>	Equation 13
$dQ_s/dt$	Change in soil water flow with time	mm day <sup>-1</sup> day <sup>-1</sup>	Equation 10
$dQ_s/dV_s$	Change in soil water flow with soil water volume	mm day <sup>-1</sup> mm <sup>-1</sup>	Equation 9
$dV_g/dt$	Change in groundwater volume with time	mm day <sup>-1</sup>	Equation 11
$dV_s/dt$	Change in soil water volume with time	mm day <sup>-1</sup>	Equation 6
$E_a$	Actual evapotranspiration	mm day <sup>-1</sup>	Equation 7
$E_p$	Potential evapotranspiration	mm day <sup>-1</sup>	Input time series
$f_E(V_s)$	Function to limit evapotranspiration when soil water level drops below field capacity	none	Equation 7
$f_{quick}$	Proportion of hydrological inputs to the soil that contribute to quick flow	none	Input parameter
$f_{sw}(V_s)$	Function to limit soil water flow once soil water level reaches field capacity	none	Equation 8
$P$	Hydrological inputs to the soil (rain plus snowmelt)	mm day <sup>-1</sup>	Equation 4
$Q_g$	Groundwater flow	mm day <sup>-1</sup>	Equation 13
$Q_{g,min}$	Minimum groundwater flow	mm day <sup>-1</sup>	Input parameter
$Q_q$	Quick flow	mm day <sup>-1</sup>	Equation 5
$Q_s$	Soil water flow	mm day <sup>-1</sup>	Equation 10
$T_g$	Baseflow recession constant	days	Input parameter
$T_s$	Soil water time constant	days	Input parameter
$V_g$	Groundwater volume	mm	Equation 11
$V_{FC}$	Field capacity	mm m <sup>-1</sup>	Input parameter
$V_s$	Soil water volume	mm	Equation 6

Table 3: Parameters and variables used in the terrestrial hydrology equations

#### a) Quick flow

Quick flow is conceptualised to include a host of rapid flow pathways, including infiltration and saturation excess overland flow, tile drainage, runoff from impervious surfaces and macropore or preferential flow through soils. In practice, it is difficult to differentiate between these various rapid flow paths when calibrating using in-stream discharge data. Therefore as a starting point all were lumped into a single input to the stream, calculated as a function of incoming precipitation. A number of options for characterising quick flow were considered (in order of increasing complexity):

1. Assume quick flow is directly proportional to incoming precipitation and is routed instantaneously to the stream. This involves just one calibration parameter,  $f_{quick}$ , the proportion of precipitation that contributes to quick flow:

$$Q_q = f_{quick}P$$

2. Assume quick flow only occurs above some precipitation threshold,  $I_{max}$ , with all precipitation routed instantaneously to the stream above this threshold. As with option (1), this involves just one calibration parameter:

$$Q_q = \max\{(P - I_{max}), 0\}$$

3. A third option builds on option 2, including a factor to describe the proportion of the precipitation that contributes to quick flow once the threshold has been exceeded. It therefore has two parameters,  $f_{quick}$  and  $I_{max}$ :

$$Q_q = f_{quick} \max\{(P - I_{max}), 0\}$$

4. Adopt one of the above approaches to describe the hydrological inputs to a quick store of water, and track the change in volume and flow of water in the store. This involves an additional user-input parameter, the time constant of the store, and therefore involves two or three user-supplied parameters. This approach is used by many process-based catchment water quality models, e.g. INCA.

Option 4 was discounted as being unnecessarily complex: the time constant is likely to be set to a small value in most catchments, and so the assumption in options 1 to 3 of quick flow directly entering the stream without a time lag is usually justifiable. As a starting point option 1 was chosen, being the simplest (Equation 5), but future work comparing options within a formal statistical framework would be useful.

*Equation 5:* Quick flow inputs to the stream,  $Q_q$  (mm day<sup>-1</sup>)

$$Q_q = f_{quick}P$$

Despite being simple, this approach allows summer flow events to be simulated, as a proportion of all precipitation enters the stream even when soil water level is below field capacity (often the case during the summer in temperate regions), when no soil water flow is simulated. It is important to be able to simulate these summer flow events, as they are often associated with nutrient peaks. Several models address the problem by adding in an additional quick flow path when soil water drops below field capacity (e.g. PERSiST, Futter et al., 2014). However, it is conceptually more consistent for this process to occur whatever the soil water level, as in Equation 5.

An important limitation of the adopted approach is a lack of seasonality in the generation of quick flow; in reality, quick flow is likely to be higher when soils are saturated, which is often the case during winter in temperate regions. A potential future extension to the model would be to include this saturation excess flow, which would require a re-formulation of the soil water equations.

#### *b) Soil water*

The soil water ordinary differential equations (ODEs) are solved separately for semi-natural and agricultural land, so the equations described in this section are present in the model for both land use classes. The change in soil water volume with time is given by Equation 6. Inputs to the soil water are from rainfall and snowmelt (Section 4.1.1), taking into account the proportion that is routed to quick flow; outputs are through evapotranspiration ( $E_a$ ) and soil water flow.

*Equation 6:* Rate of change in soil water volume,  $V_s$ , with respect to time (mm day<sup>-1</sup>)

$$\frac{dV_s}{dt} = (1 - f_{quick})P - E_a - Q_s$$

$E_a$  is calculated from a user-supplied time series of potential evapotranspiration ( $E_p$ ), taking into account: (1) differences between land cover and topography in the study catchment compared to reference values used to compute  $E_p$ , through the optional use of a correction factor, and (2) moisture limitation once soil water drops below field capacity (Equation 7). To achieve the link between evapotranspiration and soil water content, an additional variable is needed in Equation 7 which tends to 1 as  $V_s$  approaches field capacity and to 0 as  $V_s$  tends to 0. A convenient function which displays this behaviour is  $f_E(V_s) = 1 - e^{-\mu V_s}$ , where  $\mu$  is a tuning parameter that determines the shape of the curve (Fenicia et al., 2011). The value of  $\mu$  is determined within the model as a function of field capacity: for the desired behaviour,  $E_A$  should be close to  $E_P$  when the soil water is at field capacity, i.e:

$$E_P = k E_A \text{ when } V_s = V_{FC}, \text{ where } k \text{ is near } 1$$

Substituting this into Equation 7 and re-arranging gives  $\mu = -\ln(1-k)/V_{FC}$ . The  $f_E(V_s)$  function is plotted in Figure 3 for a variety of values of  $k$  and for the minimum and maximum likely field capacity values (100 to 450 mm/m; Ratliff et al., 1983). Based on this plot,  $k$  was fixed at 0.99 so that  $f_E(V_s)$  is close to 1 at field capacity and drops away relatively quickly below field capacity.

Equation 7: Actual evapotranspiration,  $E_a$  ( $\text{mm day}^{-1}$ ). The function  $f_E(V_s)$  limits evapotranspiration when soil water content drops below field capacity

$$E_a = \alpha E_p f_E(V_s) = \alpha E_p (1 - e^{-\mu V_s}), \text{ where } \mu = \frac{-\ln(0.01)}{V_{FC}}$$

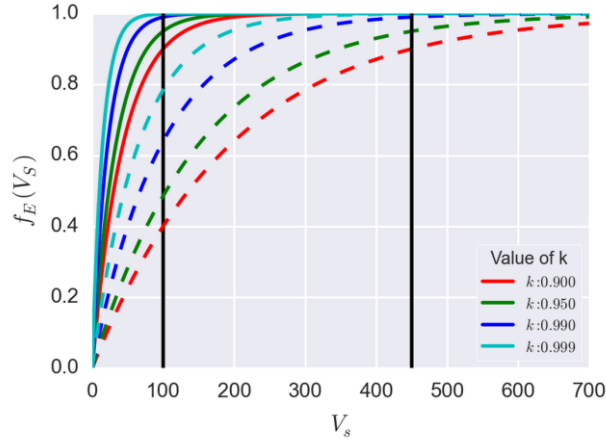


Figure 3: Relationship between  $f_E(V_s)$  and soil water volume ( $V_s/\text{mm}$ ) for a variety of  $k$  factors, where  $f_E(V_s) = 1 - e^{-\mu V_s}$  and  $\mu = -\ln(k)/V_{FC}$ . The vertical lines mark the minimum and maximum likely values for field capacity (FC). Solid lines:  $FC=100$ ; dashed lines:  $FC=450 \text{ mm m}^{-1}$ .

It is assumed that soil water flow only takes place when the soil water level is above field capacity and that flow is proportional to the volume of water above field capacity (Equation 8). The constant of proportionality is  $1/T_s$ , where  $T_s$  is the soil water time constant. The additional function in Equation 8,  $f_{sw}(V_s)$ , prevents soil water flow from occurring when soil water content drops below field capacity. One option is for this function to involve a set of logical conditions (e.g.  $f_{sw}(V_s) = 0$  when  $V_s > V_{FC}$ ; otherwise  $f_{sw}(V_s) = 1$ ). However, this kind of logic introduces non-differentiable discontinuities into the ODE. Instead, a continuous sigmoid function was used (Fenicia et al., 2011), which yields a curve which switches rapidly from zero to one around field capacity (Figure 4).

Equation 8: Discharge from the soil water store,  $Q_s$  ( $\text{mm day}^{-1}$ )

$$Q_s = \frac{1}{T_s} (V_s - V_{FC}) f_{sw}(V_s) = \frac{1}{T_s} (V_s - V_{FC}) \left( \frac{1}{1 + e^{(V_{FC} - V_s)}} \right)$$

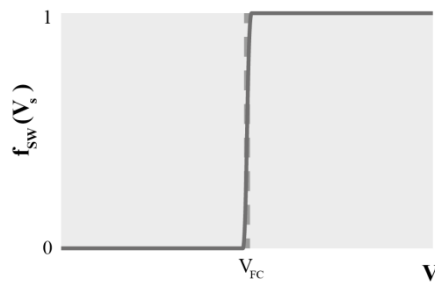


Figure 4: Schematic demonstrating the form  $f_{sw}(V_s)$  takes when a sigmoid curve is used

To derive an equation for the rate of change in soil water flow with time,  $dQ_s/dt$ , Equation 8 must be differentiated with respect to time. To do this,  $dQ_s/dV_s$  is first defined by differentiating Equation 8 with respect to soil water volume (Equation 9), which is then used to derive  $dQ_s/dt$  (Equation 10).

Equation 9: Rate of change in soil water flow,  $Q_s$ , with respect to soil water volume ( $\text{day}^{-1}$ )

$$\frac{dQ_s}{dV_s} = \frac{(V_s - V_{FC})e^{V_{FC} - V_s}}{T_s(e^{V_{FC} - V_s} + 1)^2} + \frac{1}{T_s(e^{V_{FC} - V_s} + 1)}$$



*Equation 10:* Rate of change in soil water flow,  $Q_s$ , with respect to time (mm day<sup>-2</sup>)

$$\frac{dQ_s}{dt} = \frac{dV_s}{dt} \frac{dQ_s}{dV_s}$$

Finally, a proportion ( $\beta$ ) of the discharge from the soil box is assumed to percolate to groundwater, whilst the remainder of the soil water flow ( $1 - \beta Q_s$ ) is assumed to travel to the stream along shallow flow pathways.

### c) *Groundwater*

The rate of change of groundwater volume with time is controlled by the balance of inputs from the soil water and outputs via groundwater flow (Equation 11). Percolation from the soil water is calculated as a fraction ( $\beta$ ) of the soil water outflow (where  $\beta$  is the baseflow index). Groundwater flow is assumed to be directly proportional to groundwater volume (Equation 12), and can be differentiated with respect to  $V_g$  to give  $1/T_g$ , where  $T_g$  is the baseflow recession constant. As with the soil water flow, the rate of change in groundwater flow with time is then calculated as the product of  $dV_g/dt$  and  $dQ_g/dV_g$  (Equation 13). The baseflow recession constant is determined through model calibration or from discharge observations using hydrograph separation techniques (e.g. Van Dijk, 2010). Beck et al. (2013) have produced a global dataset of baseflow index and recession constants which could provide useful starting points for model calibration.

*Equation 11:* Rate of change of groundwater volume,  $V_g$ , with time (mm day<sup>-1</sup>)

$$\frac{dV_g}{dt} = \beta Q_s - Q_g$$

*Equation 12:* Relationship between groundwater flow and volume

$$Q_g = \frac{1}{T_g} V_g; \text{ therefore } \frac{dQ_g}{dV_g} = \frac{1}{T_g}$$

*Equation 13:* Rate of change of groundwater flow,  $Q_g$ , with time (mm day<sup>-1</sup> day<sup>-1</sup>)

$$\frac{dQ_g}{dt} = \frac{dV_g}{dt} \frac{dQ_g}{dV_g} = \frac{\beta Q_s - Q_g}{T_g}, \text{ where } Q_g = \text{maximum}(Q_{g,\text{min}}, Q_g)$$

The minimum groundwater flow parameter in Equation 13,  $Q_{g,\text{min}}$ , prevents groundwater flow from dropping below a user-specified threshold. Without this, sustained periods when soil water is below field capacity may result in little groundwater recharge and under-simulation of low flows (red line in Figure 5 for the Tarland catchment). This threshold is implemented by testing whether the groundwater flow at the end of the day is below the user-specified threshold. If it is, the initial conditions at the start of the next time step are set to the threshold. It is therefore possible for groundwater flow within a day to drop below the threshold, but generally not by much.

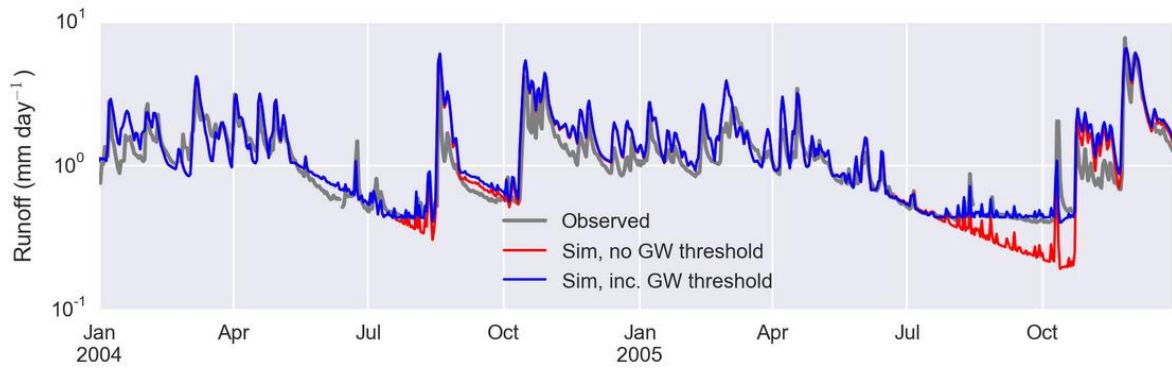


Figure 5: Comparison of simulated runoff with and without inclusion of a minimum groundwater flow in the Tarland catchment. Note log scale.

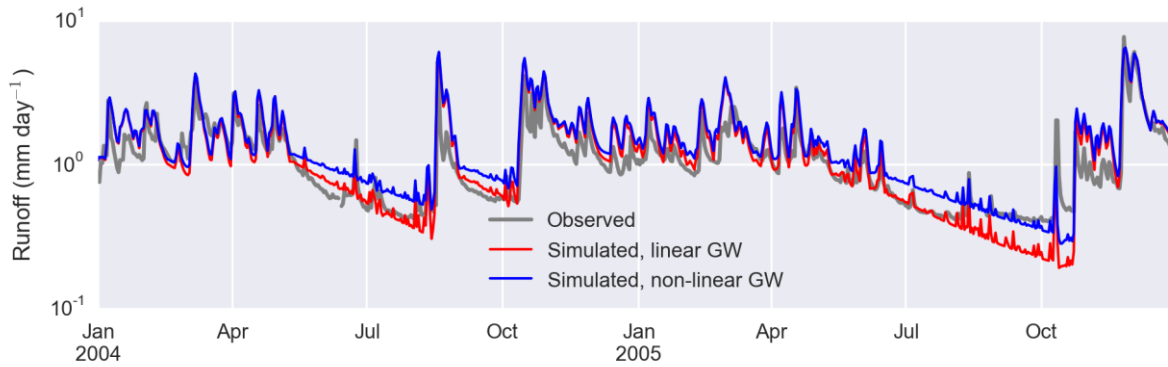


Figure 6: Comparison of simulated runoff generated using a linear and a non-linear groundwater reservoir in the Tarland. Note the log scale.

Poor representation of low flows is a common weakness in hydrological simulations (Fenicia et al., 2006), leading to potentially large errors in simulated solute concentrations during the ecologically-sensitive summer period. Whilst preventing groundwater flow from dropping below a certain threshold improves the simulation, it is not an ideal solution: (1) it circumvents the fact that something is wrong with the model conceptualisation if sustained summer baseflows cannot be simulated, and (2) it does not satisfy the internal catchment water balance, as the excess water required to sustain groundwater at the user-specified threshold is not sourced from within the catchment. This approach therefore works for the purposes of developing a prototype model, and indeed is that adopted by e.g. INCA. However, alternative options were also considered, and should be a priority for future development of the model. These include:

- 1) Replacing the linear relationship between groundwater volume and flow with a non-linear relationship, so that  $V_g = T_g Q^k$ , as described by Wittenberg (1999), where  $k$ , the non-linear coefficient, reflects the influence of aquifer properties on  $Q_g$ . Equations for the rates of change in groundwater volume and flow therefore become:

$$\frac{dQ_g}{dV_g} = \frac{V_g^{\frac{1-k}{k}}}{kT_g^{\frac{1}{k}}} \text{ (which simplifies to } \frac{1}{T_g} \text{ when } k = 1)$$

$$\frac{dV_g}{dt} = \beta Q_s - \left(\frac{V_g}{T_g}\right)^{\frac{1}{k}}$$

$$\frac{dQ_g}{dt} = \frac{dQ_g}{dV_g} \frac{dV_g}{dt}$$

A comparison of simulations using a linear and a non-linear groundwater store in the Tarland are shown in Figure 6. In this case the non-linear model produces a flatter recession, but simulated low flows are

too high. Discussions as to whether the groundwater storage-discharge relationship should be considered linear or non-linear have been on-going in the literature for some time, and certainly in some cases a non-linear reservoir appears to perform better (e.g. Gan and Luo, 2013). Other researchers have added in additional storage boxes to help improve model performance (e.g. Luo et al., 2012). In cases this may be justified, but Fenicia et al. (2006) make a strong argument for non-linear reservoirs often appearing to perform better only when important fluxes into or out of the groundwater storage zone have been neglected.

- 2) The second option considered was therefore that the model is missing an additional flux into the groundwater, e.g. slow recharge from the unsaturated zone. Possible alternative formulations of the soil water store, which would allow for some groundwater recharge to occur when the soil water level drops below field capacity, include:
  - a. Adding in a small, constant flux from the soil water box to the groundwater, which is independent of soil water content. This would require a user-calibrated parameter to set the flux, and a function as used in Equation 7 to prevent negative soil water volumes.
  - b. Changing the shape of the sigmoid function used to limit soil water drainage below field capacity, so that it behaves less like a step function and allows some continued percolation to groundwater below field capacity. This is a mechanistically justifiable option, as soils continue to produce water when water contents drop below field capacity, although the fluxes involved vary with soil type and texture (Twarakavi et al., 2009). Some practicalities of this option would need careful consideration, e.g. choosing an appropriate shape parameter for all possible values of field capacity, to ensure zero flow when water level drops to zero.

The model only considers average conditions over the catchment, whilst in reality, although catchment-average soil water content may be at or below field capacity, soils in parts of the catchment (e.g. at the foot of slopes or in hollows) are likely to remain above field capacity, and therefore able to feed water into groundwater and surface watercourses. This is a limitation of using a semi-distributed approach, and provides further justification for using a less steep sigmoid function.

In summary, the simple linear store with a user-supplied minimum groundwater flow provides a working solution to the problem of simulating summer low flows, and is suitable for the purposes of the prototype model being developed here. However, improved realism should be achievable without much increase in model complexity, and exploring options to achieve this should be a high priority for any future development efforts.

#### *d) Example model output*

An example of terrestrial hydrology output for the Tarland Burn catchment for the period 2004-2005 is shown in Figure 7, using time constants of 1 day for agricultural land and 10 days for semi-natural land. For both land use classes, soil water volume is at or above field capacity for most of the winter and then drops below field capacity during the summer, when quick flow provides the only soil input to the stream. The larger soil water time constant in semi-natural land means that it responds more slowly to changing inputs than agricultural soil water, with lower, broader peaks in flow and volume after rainfall. The groundwater time constant is much longer than the soil water time constants (65 days), so changes in groundwater flow and volume are a highly damped version of the changes in the soil water stores.

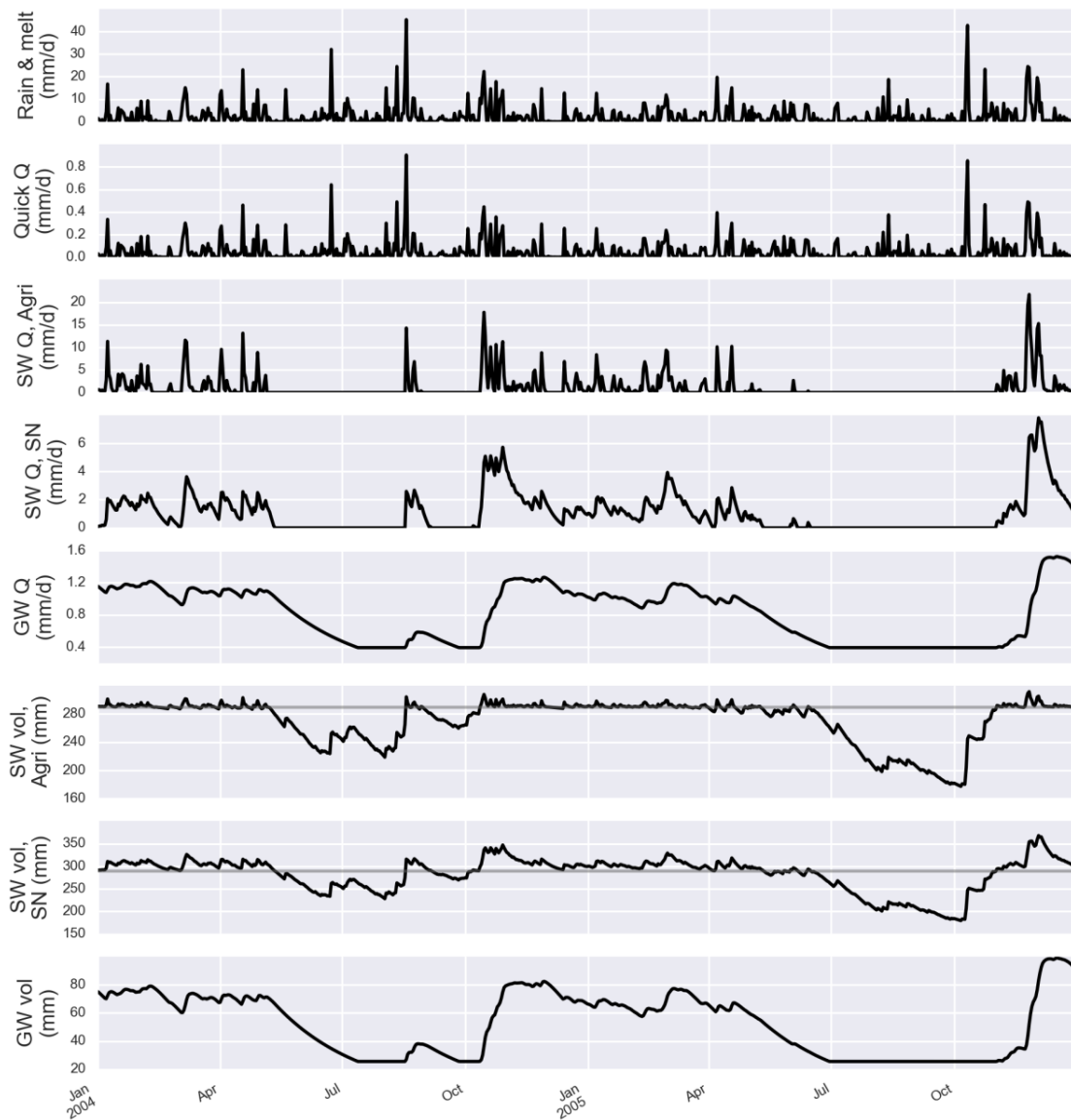


Figure 7: Terrestrial compartment hydrology results in the Tarland catchment. *Q*: discharge, *Vol*: volume, *SW*: soil water, *GW*: groundwater, *Agri*: agricultural land, *SN*: semi-natural land. Grey lines on the soil water volume plots mark the field capacity. *N.B.* volumes and fluxes are per unit area.

#### 4.1.3 In-stream hydrology

Observed discharge can often be simulated without accounting for within-reach water travel times. However, the water quality model requires estimates of reach volume and discharge, to allow concentrations and fluxes from the reach to be calculated. Parameters and variables used in the instream hydrological equations are defined in Table 4. Note that, as in the terrestrial compartment, all volumes and fluxes are calculated using units of depth per unit area. The simulated daily mean flow is then converted to cumecs for comparison with observations ( $1 \text{ m}^3 \text{ s}^{-1} = 10^3 \text{ 86400}^{-1} A_{SC} \text{ mm day}^{-1}$ , where  $A_{SC}$  is sub-catchment area in  $\text{km}^2$ ).

Variable	Description	Units	Source
$a$	Gradient of in-stream velocity-discharge relationship	$m^{-2}$	Input parameter
$b$	Exponent of in-stream velocity-discharge relationship	None	Constant (0.42)
$\beta$	Base flow index	None	Input parameter
$dQ_r/dt$	Rate of change in reach discharge with time	$mm\ day^{-1}\ day^{-1}$	Equation 17
$dQ_{r,av}/dt$	Rate of change in daily mean flow with time	$mm\ day^{-1}\ day^{-1}$	Equation 18
$dV_r/dt$	Rate of change in reach water volume with time	$mm\ day^{-1}\ day^{-1}$	Equation 14
$f_A$	Proportion of agricultural land in the sub-catchment	None	Input parameters ( $f_A + f_G$ )
$f_S$	Proportion of semi-natural in the sub-catchment	None	Input parameter
$L_{reach}$	Reach length	M	Input parameter
$Q_g$	Groundwater flow	$mm\ day^{-1}$	Equation 13
$Q_q$	Quick flow	$mm\ day^{-1}$	Equation 5
$Q_s^A$	Soil water inputs from agricultural land	$mm\ day^{-1}$	Equation 10
$Q_s^S$	Soil water inputs from semi-natural land	$mm\ day^{-1}$	Equation 10
$Q_r$	Outflow from the reach	$mm\ day^{-1}$	Equation 17
$Q_{r,av}$	Daily mean flow from the reach	$mm\ day^{-1}$	Equation 18
$Q_{r,US}$	Inputs to the reach from upstream reaches	$mm\ day^{-1}$	Model calculates
$T_r$	Reach time constant	Days	Equation 16
$V_r$	Reach water volume	Mm	Equation 14

Table 4: Parameters and variables used in the instream hydrology equations

The instream hydrology equations used are similar to those used in other water quality models. The change in water volume in each reach is assumed to be proportional to the difference between input and output fluxes (Equation 14). Input fluxes are from quick flow, soil water flow, groundwater flow and inflow from upstream reaches, and water leaves via the reach outflow. The soil water input to the reach is calculated as the sum of inputs from semi-natural and agricultural land in the catchment.

Equation 14: Rate of change in reach volume,  $V_r$ , with time ( $mm\ day^{-1}$ )

$$\frac{dV_r}{dt} = Q_q + (1 - \beta)(f_A Q_s^A + f_S Q_s^S) + Q_g + Q_{r,US} - Q_r$$

Flow downstream,  $Q_r$ , is assumed to be proportional to the reach volume (Equation 15), with a constant of proportionality  $1/T_r$  (where  $T_r$  is the reach time constant in days).  $T_r$  is not however constant as it is in the terrestrial stores, but is inversely proportional to water velocity to account for the shorter residence time of faster flowing water (Equation 16). Water velocity is estimated using an empirical relationship with discharge (Equation 16) (Chapter 14, Chapra, 2008; Leopold and Maddock Jr, 1953), where  $a$  is a user-supplied parameter, derived where possible from velocity profiling carried out as part of flow gauging, and  $b$  is a non-linear coefficient. The  $a$  parameter is the most site-specific, whilst  $b$  is usually between 0.3 and 0.5. To reduce model complexity and interactions between these two parameters, the value of  $b$  was therefore set as a constant with a value of 0.42, corresponding to the average from over 200 river cross sections in the US and Europe (Wolman et al., 1964). The units of  $a$  ( $m^{-2}$ ) assume that observed velocity and discharge have units of  $m\ s^{-1}$  and  $m^3\ s^{-1}$ , respectively.

Equation 15: Relationship between reach discharge,  $Q_r$  ( $mm\ day^{-1}$ ) and volume,  $V_r$  (mm)

$$V_r = T_r Q_r = \frac{L_{reach}}{86400 a} Q_r^{(1-b)}$$

Equation 16: Reach time constant,  $T_r$  (days), where  $U$  is the water velocity ( $m\ s^{-1}$ )

$$T_r = \frac{L_{reach}}{U}; U = a Q_r^b, \text{ so } T_r = \frac{L_{reach}}{86400 a Q_r^b}$$

The rate of change in discharge with time is given by Equation 17. The time-varying nature of  $T_r$  gives rise to the  $(1-b)$  factor in the denominator. To get a time series of daily mean flow, the rate of change in discharge with time is integrated with initial conditions set to zero at the start of each day (Equation 18), to provide the

total flux of water leaving the reach over a day. The units of this daily mean flow time series are then converted to cumecs for comparison with observations.

*Equation 17:* The rate of change in reach discharge,  $Q_r$ , with time ( $\text{mm day}^{-1} \text{ day}^{-1}$ )

$$\frac{dQ_r}{dt} = \frac{1}{T_r(1-b)} (Q_q + (1-\beta)(f_A Q_s^A + f_S Q_s^S) + Q_g + Q_{r,US} - Q_r)$$

*Equation 18:* Change in daily mean flow,  $Q_{r,av}$  ( $\text{mm day}^{-1}$ ), with time

$$\frac{dQ_{r,av}}{dt} = Q_r$$

The daily mean flow is used to determine the flux from the up-stream reach,  $Q_{r,US}$ . For the top reach, this is set to zero. For all other reaches, it is set equal to the daily mean flow from the upstream reach for the same time step. In this sense, the reaches are not fully coupled, as simulated within-day changes in flow are not cascaded from reach to reach. However, this assumption simplifies the coding considerably and should be appropriate in all but large, highly flashy systems.

## 4.2 Sediment processes

### 4.2.1 In-stream suspended sediment

In-stream SS concentrations are highly variable spatially and temporally, changing in response to terrestrial delivery, stream bank erosion, entrainment of bed sediment material and sediment deposition on floodplains and the stream bed. Terrestrial delivery is in turn controlled by the detachment of soil particles by raindrop impact, flow erosion and transport through the catchment, with deposition in areas of lower water velocity. Important factors affecting in-stream processes include stream power, particle size and type, stream bed morphology, macrophyte cover and antecedent conditions (Merritt et al., 2003). Incorporating these processes into a model would require many parameters to be calibrated, even with a simple formulation. In intensively-studied catchments some terrestrial data may be available to help constrain parameter values, but in most areas calibration is done using only in-stream SS concentration time series, and it is doubtful that these time series contain enough information for such a level of process representation.

Despite the varied and complex processes which represent sediment fluxes to and within streams, in-stream SS concentration has long been known to be well-explained by a simple power law with in-stream discharge:  $SS = aQ_r^b$ , where  $SS$  is suspended sediment concentration,  $Q_r$  is in-stream discharge, and  $a$  and  $b$  are parameters determined by regression (Colby, 1956). There are therefore strong indications that, at the catchment scale, this complexity may be simplified to a remarkably straightforward relationship. Here, this simple power law is therefore taken as the basis for simulating the change in SS mass with time in each stream reach. Parameters and variables used in the sediment equations are defined in Table 5.

Variable	Description	Units	Source
$A_{SC}$	Sub-catchment area	km <sup>2</sup>	Input parameter
$C_{cover}$	Erosion soil cover factor	none	Equation 26
$C_{measures}$	Erosion management factor	none	Input parameter
$dM_{sus}/dt$	Rate of change in reach suspended sediment mass with time	kg day <sup>-1</sup>	Equation 19
$dM_{sus,tot}/dt$	Change in total daily flux of sediment from the stream reach	kg day <sup>-1</sup>	Equation 23
$E_M$	Sediment input scaling factor	kg mm <sup>-1</sup>	Input parameter
$E_{sus}$	Sediment-discharge rating coefficient	kg mm <sup>-1</sup>	Equation 21
$f_{Ar}$	Fraction of arable land in the sub-catchment	none	Input parameter
$f_{IG}$	Fraction of improved grassland in the sub-catchment	none	Input parameter
$f_S$	Fraction of semi-natural land in the sub-catchment	none	Input parameter
$k_M$	Instream erosion and entrainment non-linear coefficient	none	Input parameter
$M_{input}$	Flux of sediment to the reach from terrestrial and instream sources	kg day <sup>-1</sup>	Equation 20
$M_{sus}$	Reach suspended sediment mass	kg	Equation 19
$M_{sus,DS}$	Flux of sediment downstream out of the reach	kg day <sup>-1</sup>	Equation 22
$M_{sus,US}$	Flux of sediment from upstream reaches	kg day <sup>-1</sup>	Model calculates
$M_{sus,tot}$	Total daily flux of sediment from the stream reach	kg day <sup>-1</sup>	Equation 23
$Q_r$	Reach discharge	mm day <sup>-1</sup>	Equation 17
$Q_{r,av}$	Daily mean discharge	mm day <sup>-1</sup>	Equation 18
$S_{SC}$	Sub-catchment slope	°	Input parameter
$S_{reach}$	Reach slope	°	Input parameter
$SS_r$	Mean daily concentration of suspended sediment in the reach	mg l <sup>-1</sup>	Equation 24
$V_r$	Volume of water in the reach	mm	Equation 14

Table 5: Parameters and variables used in the in-stream sediment equations

The rate of change in SS mass with time is controlled by the difference between sediment input and output fluxes (Equation 19). Inputs from the terrestrial compartment, in-stream channel erosion and entrainment are grouped into a single input term,  $M_{input}$ , assumed to be related to in-stream flow using a power law (Equation 20). It was originally envisaged that Equation 19 would include separate terms for sediment delivery from the land (proportional to quick flow) and instream entrainment and erosion (proportional to instream discharge). However, adding a quick flow-dependent term to Equation 20 made little difference to model output and was therefore discarded, and the entrainment term was re-formulated to represent both terrestrial and instream inputs.

Equation 19: Rate of change in suspended sediment mass in the stream reach,  $M_{sus}$ , with time (kg day<sup>-1</sup>), where superscript  $i$  denotes the land use class.  $f^i$  is one of  $f_{Ar}$ ,  $f_{IG}$  or  $f_S$ .

$$\frac{dM_{sus}}{dt} = \left( \sum_i f^i M_{input}^i \right) + M_{sus,US} - M_{sus,DS}$$

Equation 20: Flux of sediment to the stream from terrestrial and in-stream sources,  $M_{input}$  (kg day<sup>-1</sup>)

$$M_{input} = E_{sus} Q_r^{k_M}$$

This simple treatment of the sediment inputs to the reach assumes that the majority of in-stream SS is generated from within- or near-channel sources, as is often observed (Bowes et al., 2005). A further assumption is made that these near-channel sediment sources are directly controlled by catchment erodibility and delivery to the watercourse, so that a change in terrestrial erodibility causes an instant reduction in in-stream SS concentration. This assumption is based on the observation that the coefficient in Equation 20,  $E_{sus}$ , relates to the erodibility of soils in the catchment (reviewed in Asselman, 2000). To build in a link between terrestrial processes and in-stream SS, the value of  $E_{sus}$  therefore incorporates data on the relative differences in expected erosion fluxes from different land units used in the Universal Soil Loss Equation (USLE; Kinnell, 2010; Renard et al., 1991; Wischmeier and Smith, 1965, 1978).  $E_{sus}$  is therefore calculated per land class (e.g. arable, improved grassland and semi-natural) and sub-catchment by multiplying a user-calibrated scaling factor with factors representing erodibility and sediment delivery to the stream (Equation 21). These factors include average slope ( $S_{SC}$ , which affects the transport capacity of quick flow), a

vegetation cover factor ( $C_{cover}$ ) and a management factor ( $C_{measures}$ ), all of which may vary with land use, and the cover factor may vary through the year if desired (Section 4.2.2).

*Equation 21:* Sediment-discharge rating coefficient,  $E_{sus}$ , ( $\text{kg mm}^{-1}$ ), where superscript  $i$  indicates that the variable or parameter varies by land use, and superscript  $j$  by sub-catchment.

$$E_{sus}^{i,j} = E_M S_{reach}^j S_{SC}^{i,j} C_{cover}^i C_{measures}^i$$

The cover factor,  $C_{cover}$ , describes the ratio between the erodibility of a bare soil plot and the land use class; its value therefore ranges from 1 (maximum erodibility) to 0 (no erosion). Cover factors can be sourced from USLE-related literature reviews, selecting an appropriate geo-climatic region and range of vegetation and crop types. For example, Panagos et al. (2015) have collated crop type factors for typical European crops (Appendix, Table A1) and other European land cover (Appendix, Table A2). The user can also incorporate relative differences in inherent soil erodibility of different land classes into the relative differences in  $C_{cover}$ , i.e. differences due to soil properties such as texture and organic matter content (generally termed the  $K$  factor in USLE-related literature). A potential future extension to the model for areas which are dominated by semi-natural land could be to build in a link between the cover factor on semi-natural land and pressures which are known to increase soil erodibility such as grazing, burning and tree felling.

The management factor,  $C_{measures}$ , allows the user to explore the effects of sediment reduction measures and should be in the range 0 to 1, where 0 implies 100% reduction in sediment yield. Measures that could be taken into account could, for example, relate to the effects of tillage, cover crops or measures to reduce sediment connectivity to the stream (e.g. buffers or fences). The model requires the user to know the effectiveness of the chosen measure for a given land class. Values for effectiveness can be obtained for example from the USLE literature (e.g. Panagos et al., 2015) or from experimental work within the study catchment.

Sediment input to the watercourse should not only vary with terrestrial erodibility and transport capacity, but also with changes in in-stream inputs. A large body of empirical and theoretical work has shown that in-stream sediment transport is controlled by stream power, i.e. the rate of energy expenditure on the stream bed and banks (Bagnold, 1966). In-stream sediment inputs to the watercourse were therefore assumed to be proportional to stream power per unit length,  $\omega = \rho g S_{reach} Q_r$ . This equation includes terms for the density of water ( $\rho$ ) and gravitational acceleration ( $g$ ), both of which are constant and therefore grouped into the user-supplied scaling factor ( $E_M$ ) in Equation 21. The remaining term, the reach slope ( $S_{reach}$ ) is then an additional factor in Equation 21.

Additional sediment inputs to the stream reach are via flow from any upstream reaches and sediment is lost via flow from the reach (Equation 22). The integral of the flux out of the reach over each day, starting with an initial condition of 0, then provides a time series of the total sediment flux from the reach per day (Equation 23), which is used to calculate daily mean SS concentration (Equation 24). The latter is output by the model for comparison with observations.

*Equation 22:* Reach suspended sediment outflow from the reach bottom,  $M_{sus,DS}$  ( $\text{kg day}^{-1}$ )

$$M_{sus,DS} = \frac{M_{sus}}{V_r} Q_r$$

*Equation 23:* Rate of change in the flux of sediment from the reach,  $M_{sus,tot}$  ( $\text{kg day}^{-1}$ )

$$\frac{dM_{sus,tot}}{dt} = M_{sus,DS}$$



Equation 24: Mean daily concentration of SS in the stream reach,  $SS_r$  ( $\text{mg l}^{-1}$ )

$$SS_r = \frac{M_{sus,tot}}{Q_{r,av}} \frac{1}{A_{SC}}$$

Connectivity between sediment source areas and the water course is an important factor in determining sediment yield to a water course. This is not explicitly accounted for at present, although it is indirectly included in the value assigned to the scaling factor,  $E_M$ , in a given area. A potential improvement would be to explicitly include a connectivity factor in Equation 20, for example by: (1) using drainage density as a proxy for connectivity, (2) only considering the characteristics of land within a certain distance of a drainage ditch/watercourse, as land most likely to be a potential sediment source area; (3) factoring in field size and the presence of barriers to flow such as walls and hedges; (4) calibrating the sediment yield scaling factor by sub-catchment, rather than keeping it constant over the whole catchment. In addition, the sub-catchment slope factor could be altered to be more representative of potential sediment source areas, for example it could be the average slope of land within a certain distance of a watercourse.

Assuming that the amount of sediment in near-channel sources is directly proportional to terrestrial erodibility is a big simplification. An implication of this assumption is that a reduction in terrestrial erodibility causes an instant reduction in in-stream SS concentration. In reality, hysteresis is often seen in the sediment-discharge relationship, reflecting the change in sediment source distance or supply during a rainfall event (e.g. Oeurng et al., 2010). As the store of sediment in near-channel sources is not tracked, there is no ability to simulate source-exhaustion over successive storm events (Bowes et al., 2005). Test applications are required to determine whether this is an issue in a given study catchment. Over the longer term, we might expect a time lag between changes in erodibility and in-stream effects as in-stream sources become exhausted. For example, typical lag times of decades or more have been reported for the retention of bulk sediment in river channels (Trimble, 2010). However, here we are primarily concerned with the fine sediment fraction (silt and clay), as the fraction that is of greatest significance for P transport due to its relatively high P content. This finer sediment fraction is substantially more mobile, with residence times of less than a year reported for many rivers, excluding storage on floodplains (Sharpley et al., 2013, and references therein).

Other issues with this simple formulation are that sediment deposition is not explicitly accounted for, and so the model cannot simulate a net flux of sediment from the water column to the stream bed. This could be a problem in some areas, for example in catchments with a big difference in slope and sediment supply between reaches. Future work is needed to determine under which circumstances deposition needs taking into account, and how it should best be done in the simplest way possible. Another potential future improvement could be to split bank erosion and entrainment from terrestrial delivery. Bank erosion and entrainment may be a key sediment input (Lefrançois et al., 2007), and assuming terrestrial sediment reduction measures cause a proportional reduction in in-stream sediment load ignores the fact that bank erosion will be unaffected by these measures. Finally, the instream sediment equations only consider allochthonous particles sourced from the catchment. However, autochthonous particles, generated in-stream by biological processes, may make up an important part of suspended matter (Stutter et al., 2009), and in some areas it may be appropriate to consider both.

#### 4.2.2 *Dynamic cover factor*

On arable land, the key risk period for soil erosion is between preparation of the seed bed and establishment of the crop, when fine ploughing results in bare soils with low cohesion. To take this temporal change in erodibility into account in the model, there is the option to replace the user-supplied constant cover factor on arable land (hereafter termed  $C_{cov,av}$ ) with a dynamic factor, which changes during the course of the year (hereafter termed  $C_{cover}$ ). This dynamic cover factor is calculated so that its annual average is the user-specified cover factor, to preserve the user's knowledge of the ratio in long-term erodibility between land use classes. In most temperate areas, high-risk seed beds will be present during both spring and autumn, as many farmers cultivate a mixture of spring- and autumn-sown crops. Arable land may therefore be further sub-

divided into spring-sown (e.g. spring cereals) and autumn sown (e.g. winter cereals) if the user wishes to take dynamic erodibility into account.

Two options were explored for calculating the dynamic cover factor (associated parameters and variables are defined in Table 6). The first approach uses a cosine wave (Equation 25). This is appealing in that it is smooth and only requires one user-supplied parameter, the date of maximum erodibility. In much of northern Europe, for example, this could be around the end of February (day 60) for spring-sown crops and the end of October (day 300) for autumn-sown crops. The amplitude of the curve can be fixed to ensure that the annual mean is equal to  $C_{cov,av}$  (Equation 25). The downside of this formulation is that it assumes that points of maximum and minimum erodibility are half a year apart. For autumn-sown cereals in particular this is unlikely.

Variable	Description	Units	Source
$C_{cover}$	Erosion soil cover factor	None	Equation 26 (if dynamic) or $C_{cover,av}$
$C_{cover,av}$	Average soil cover factor for erodibility	None	Input parameter
$C_{measures}$	Erosion management factor	None	Input parameter
$d_{E,max}$	Date of maximum soil erodibility	None	Input parameter (for spring- and autumn-sown)
$d_{E,start}$	Start of the high erodibility period	None	Model calculates ( $D_{E,max}-30$ )
$d_{E,end}$	End of the high erodibility period	None	Model calculates ( $D_{E,max}+30$ )
$d_{year}$	Julian day of the year	None	Model calculates
$f_{spr}$	Fraction of arable land that is spring sown	None	Input parameter

Table 6: Parameters and variables used in the erodibility equations

Equation 25: Dynamic crop cover factor for arable land calculated using a cosine wave, where superscript  $i$  indicates the crop type (spring-sown or winter-sown)

$$C_{cover}^i = \frac{C_{cov,av}^i}{2} \left( \cos\left(\frac{2\pi}{365} d_{year} + d_{Emax}^i\right) + 1 \right)$$

The alternative approach adopted instead was to assume a constant cover factor throughout the year, apart from during a high risk period defined by a user-specified maximum erodibility date. Within this high risk period, the factor follows a triangular shape (Figure 8), which smooths the transition from lower to higher erodibility risk, to take into account differences in ploughing dates across the catchment. The difference between  $C_{cov,av}$  and the dynamic cover factor outside the high risk period is calculated so that the annual average of the dynamic cover factor equals  $C_{cov,av}$  (Figure 8 and Equation 26). To provide comparable simplicity to the sine curve option, the length of the high erodibility period is fixed. This period should encompass the likely variability in seed bed presence in both space and time in the catchment, whilst not being so wide as to reduce the cover factor during the remainder of the year to below the average values on improved grassland and semi-natural land – we would generally expect arable land, with its higher proportion of bare soil, compaction and tramlines, to have higher erosion risk than the other two land classes. A period of two months (60 days) provided a good compromise, although the sensitivity of the model to this factor could be assessed in the future. Within the high risk period, the value of the dynamic cover factor is then calculated by linear interpolation (Equation 26), and the results for spring- and autumn-sown crops are averaged to give the overall factor to be used in Equation 21.

Equation 26: Dynamic cover factor for arable land,  $C_{cover}$ , calculated using a triangular wave during the high risk period, where superscript  $i$  indicates the crop type (spring-sown or winter-sown)

If the day of the year,  $d_{year}$ , is within the period  $d_{E,max}^i \pm 30$  days:

$$\text{If } d_{year} < d_{E,max}^i: C_{cover}^i = C_{cov,av}^i + \frac{(1 - C_{cov,av}^i)(d_{year} - d_{E,start}^i)}{d_{E,max}^i - d_{E,start}^i}$$

$$\text{If } d_{year} > d_{E,max}^i: C_{cover}^i = 1 + \frac{(C_{cov,av}^i - 1)(d_{year} - d_{E,max}^i)}{d_{E,end}^i - d_{E,max}^i}$$

Otherwise:

$$C_{cover}^i = C_{cov,av}^i - \left( \frac{60(1 - C_{cov,av}^i)}{2(365 - 60)} \right)$$

Averaging over arable land classes:

$$C_{cover} = f_{spr} C_{cover}^{spring} + (1 - f_{spr}) C_{cover}^{autumn}$$

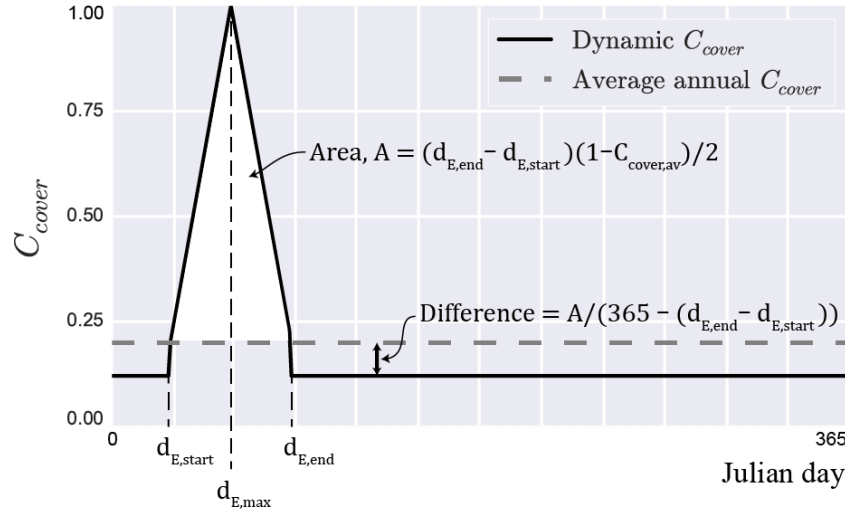


Figure 8: Schematic illustrating the shape of the dynamic crop cover factor ( $C_{cover}$ ) over a year. The period of high erodibility starts on  $d_{E,start}$ , is at its maximum at  $d_{E,max}$  and finishes at  $d_{E,end}$ .

Model testing, preferably in a formal statistical framework, is required to determine whether the additional complexity of the dynamic cover factor is warranted. A good place to test this would be in an area where sediment fluxes are believed to change throughout the year in response to changing arable crop cover. It would also be worth exploring how suitable the dynamic cover factor formulation is for autumn-sown crops, which are likely to have relatively bare soils throughout the winter.

### 4.3 Phosphorus processes

#### 4.3.1 Soil processes

##### a) Overview

Soil P processes are calculated separately for two land use classes – a ‘high P’ class and a ‘low P’ class. Below, the high P class is referred to as agricultural land, and the low P class as semi-natural, but other land uses could be assigned to these classes. For particulate P fluxes, a further distinction may be made between high and low erodibility land uses in the high P class, e.g. between arable and improved grassland, to take the different erodibility (and therefore sediment and PP transport) into account (Section 4.2.1). The model also includes the ability to simulate semi-natural land newly-converted from agricultural land and vice versa (discussed further in Section 4.3.1 c).

In the model, P is present in the soil in three forms: (1) dissolved P (TDP) in the soil water, (2) labile soil P, which can take part in sorption reactions with soil water TDP, and (3) inactive soil P. The masses of dissolved and labile soil P change through time, whilst the mass of inactive soil P is constant. Parameters and variables used in the soil P equations are defined in Table 7.

Variable	Description	Units	Source
$A_{SC}$	Sub-catchment area	km <sup>2</sup>	Input parameter
$\beta$	Baseflow index	None	Input parameter
$dP_{labile}/dt$	Rate of change of labile soil P mass with time	kg day <sup>-1</sup>	Equation 33
$dTDP_s/dt$	Rate of change of soil water TDP mass with time	kg day <sup>-1</sup>	Equation 34
$EPC_0$	Agricultural soil equilibrium P concentration of zero sorption	kg mm <sup>-1</sup>	Equation 29 or $EPC_{0,user}$
$EPC_{0,user}$	User-supplied initial $EPC_0$ for agricultural soil	mg l <sup>-1</sup>	Input parameter
$f_i$	Fraction of land use in each of the possible land use classes, $i$ , including agricultural (A; $f_{Ar} + f_{IG}$ ), arable (Ar), improved grassland (IG), semi-natural (SN), and newly-converted versions of all 3 (NC <sub><math>i</math></sub> )	None	Input parameters
$K_f$	Soil P adsorption coefficient	mm kg soil <sup>-1</sup>	Equation 28
$M_{soil}$	Soil mass	kg	Equation 32
$M_{soil,m2}$	Soil mass per m <sup>2</sup> (soil depth $\times$ bulk density)	kg m <sup>-2</sup>	Input parameter
$P_{inactive}$	Soil inactive P mass	kg	Equation 30
$P_{labile}$	Soil labile P mass	kg	Equation 33
$P_{labile,0}$	Initial soil labile P content	kg	Equation 31
$P_{netInput}$	Net annual input (or uptake) of P to the land class	kg ha <sup>-1</sup> yr <sup>-1</sup>	Input parameter
$P_{soilConc,A}$	Total soil P content in agricultural land as a mass ratio	mg P (kg soil) <sup>-1</sup>	Input parameter
$P_{soilConc,S}$	Total soil P content in semi-natural land as a mass ratio	mg P (kg soil) <sup>-1</sup>	Input parameter
$Q_q$	Quick flow	mm day <sup>-1</sup>	Equation 5
$Q_s$	Soil water flow	mm day <sup>-1</sup>	Equation 10
$TDP_{g,conc}$	Groundwater TDP concentration	mg l <sup>-1</sup>	Input parameter
$TDP_{g,land}$	Groundwater TDP input to the reach	kg day <sup>-1</sup>	Equation 37
$TDP_{q,land}$	Quick flow TDP input to the reach	kg day <sup>-1</sup>	Equation 36
$TDP_s$	TDP mass in the soil water	kg	Equation 34
$TDP_{s,land}$	Soil water TDP input to the reach	kg day <sup>-1</sup>	Equation 35
$V_s$	Soil water volume	mm	Equation 6

Table 7: Parameters and variables used in the soil and groundwater P equations

### b) Interactions between soil P and dissolved soil water P

The labile soil P store and dissolved P in the soil water are assumed to be in equilibrium, and a simple linear relationship is used to relate soil total P concentration and  $EPC_0$ , the equilibrium TDP concentration at which there is no net sorption or desorption of P (Equation 27; Figure 9). This relationship can be conceptualised as accounting for sorption and mineralization/immobilization reactions. This linear relation cannot simulate P saturation, but because of its simplicity it is recommended for use in catchment models, as long as soil water TDP concentration is below 1 to 10 mg l<sup>-1</sup> (McCray et al., 2005).

Equation 27: Relationship between soil P content ( $P_{soil,conc}$ ; kg P kg soil<sup>-1</sup>) and soil water TDP concentration (expressed as the equilibrium P concentration,  $EPC_0$ ; kg mm<sup>-1</sup>)

$$P_{soil,conc} = K_f EPC_0 + 10^{-6} P_{soilConc,S}$$

Soil water in semi-natural areas tends to have low TDP concentrations ( $Q_{75} < 5 \mu\text{g l}^{-1}$ ; unpublished James Hutton Institute data), implying tight retention of any P released from the soil matrix. It is therefore assumed that semi-natural land does not contain labile soil P, that semi-natural soil water TDP concentration is zero, and that all soil P in semi-natural land is in the inactive soil P store (Equation 30). The soil P content of semi-natural land is therefore used as the y-axis intercept in Equation 27, and the inactive soil P store on agricultural land is assumed to be the same as in semi-natural land (Figure 9).

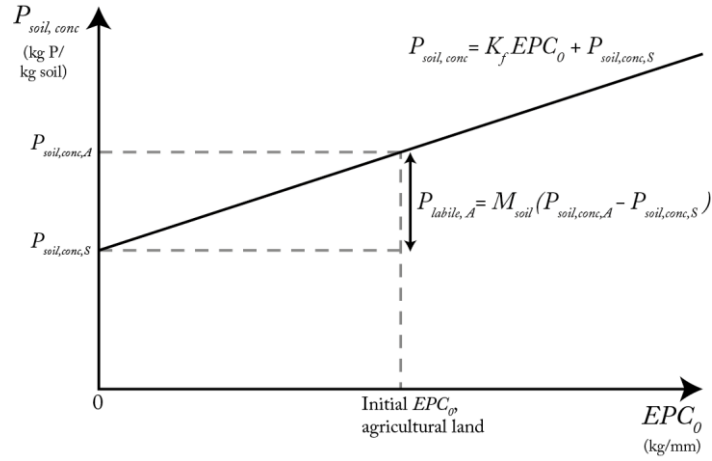


Figure 9: Illustration of the conceptual model used to link soil P content and soil water TDP concentration, expressed as  $EPC_0$ , the equilibrium TDP concentration of zero sorption.

Having defined the y-intercept, there are then two unknowns in Equation 27 for a given soil total P content: the adsorption coefficient ( $K_f$ ) and  $EPC_0$ . It is very important for simulated soil water TDP concentrations to be in the right range, as in diffuse pollution-dominated systems near-surface soil water flow often controls in-stream TDP peaks. Initial agricultural soil water TDP concentration, assumed to be equivalent to soil water  $EPC_0$ , was therefore chosen to be the calibrated parameter, and  $K_f$  is calculated internally by the model using Equation 28. Once agricultural  $EPC_0$  has been determined through calibration,  $K_f$  output by the model from the calibration period is then supplied as an input parameter for model runs in simulation mode and  $EPC_0$  is calculated instead within the model (Equation 29). Initial  $EPC_0$  is still an input parameter in any validation and scenario runs, but merely to provide the initial conditions for the soil water P content. This formulation removes much of the need for careful thinking and parameterisation from the modeller, thereby reducing the risk of highly inappropriate sorption equations, and therefore unrealistic simulations of the impacts of changes in fertilizer or manure inputs or land use change.

Equation 28: The adsorption coefficient,  $K_f$  ( $\text{mm kg soil}^{-1}$ ), calculated during the calibration period

$$K_f = \frac{10^{-6}(P_{\text{soilConc},A} - P_{\text{soilConc},S})}{EPC_0}$$

Equation 29:  $EPC_0$ , the equilibrium TDP concentration of zero sorption ( $\text{kg mm}^{-1}$  in the equation below; supplied by the user in  $\text{mg l}^{-1}$ ). N.B. the user may also opt for  $EPC_0$  to be constant

$$EPC_0 = \frac{P_{\text{labile}}}{K_f M_{\text{soil}}}$$

Having assumed that the inactive soil P store on agricultural land is equivalent to the total soil P content on semi-natural land, initial labile P content in agricultural land is then calculated as the difference between cultivated and semi-natural total P content (Equation 31). This assumption is only appropriate if soils under the two land classes have similar P sorption capacity (controlled primarily by iron oxide and clay content).

Equation 30: Inactive soil P content in agricultural and semi-natural land,  $P_{\text{inactive}}$  (kg)

$$P_{\text{inactive}} = 10^{-6} P_{\text{soilConc},S} M_{\text{soil}}$$

Equation 31: Initial labile soil P content in agricultural land,  $P_{\text{labile},0}$  (kg)

$$P_{\text{labile},0} = 10^{-6} (P_{\text{soilConc},A} - P_{\text{soilConc},S}) M_{\text{soil}}$$

Converting from soil P concentration to mass of P in the labile and inactive stores requires an estimate of the sub-catchment soil mass (Equation 32). The user-specified areal soil mass parameter ( $M_{\text{soil},m2}$ ) can be

calculated by multiplying soil bulk density with an estimate of soil depth; topsoil depth is recommended, being the depth of soil which contains highest soil P concentrations. These two parameters are lumped together as one user input parameter to reduce parameter non-identifiability issues during auto-calibration.

*Equation 32:* Sub-catchment topsoil mass,  $M_{soil}$  (kg)

$$M_{soil} = M_{soil,m^2} 10^6 A_{SC}$$

The change in mass of P in the labile P store due to a change in TDP concentration in the soil water can then be calculated and is assumed to control the rate of change in soil labile P in agricultural land with time (Equation 33). Inputs from fertilizer and manure are all assumed to occur in liquid form and to bring about an increase in labile P mass through adsorption. Conversely, a change in labile P content may cause a change in soil water TDP concentration due to a shift in  $EPC_0$  (Equation 29). The model also includes the option for  $EPC_0$  to be constant over time, to simplify the model for short model runs where no shift in soil water TDP concentration is expected.

*Equation 33:* Rate of change in soil labile P mass,  $P_{labile}$ , with time ( $\text{kg day}^{-1}$ )

$$\frac{dP_{labile}}{dt} = K_f M_{soil} \left( \frac{TDP_s}{V_s} - EPC_0 \right)$$

The rate of change of soil water TDP mass with time in agricultural land is controlled by the balance of input and output fluxes (Equation 34). Potential inputs are from the application of fertilizer and manure and net release of soil P. Outputs are via plant uptake, sequestration into soil P, soil water flow and quick flow. The latter is included as it is assumed that quick flow also inherits soil water TDP concentration. Fertilizer, manure and plant uptake fluxes are grouped together into a single annual P budget parameter ( $P_{netInput}$ ;  $\text{kg ha}^{-1} \text{yr}^{-1}$ ), which is then evenly applied (or subtracted, if there is net output) over the course of the year. This grouping greatly reduces the number of parameters required, and the  $P_{netInput}$  parameter may be readily informed by budgeting studies or published national P surplus values (e.g. eurostat, 2013). This simplified treatment of terrestrial P inputs and outputs assumes a relatively constant TDP concentration in soil water throughout the year. Whilst this is clearly a simplification, previous modelling work has suggested the additional complexity involved in attempting to simulate the daily changes in soil water TDP concentration in response to variations in fertilizer, manure and plant uptake fluxes is not justified (Jackson-Blake et al., 2015). At present the model takes as input a single constant value. An easy future extension to the model would be to provide the option for this to be replaced by an annual time series of values.

*Equation 34:* Rate of change of soil water TDP mass,  $TDP_s$ , with time ( $\text{kg day}^{-1}$ )

$$\frac{d TDP_s}{dt} = \frac{100 A_{SC}}{365} P_{netInput} - \frac{dP_{labile}}{dt} - Q_s \frac{TDP_s}{V_s} - Q_q \frac{TDP_s}{V_s}$$

This representation of soil P processes greatly simplifies the actual processes involved. In reality soil P is present in a continuum of interlinked states of varying extractability, and hysteresis effects are common in P transfers between the states. However, the understanding of how detailed soil chemical processes upscale to the catchment-scale is arguably not yet advanced enough for fine-scaled geochemical principles to be usefully incorporated into a catchment-scale model, and there is certainly a lack of data to constrain such processes at a catchment scale. A potential future change to the model would however be to use more detailed geochemical models or lab experiments to derive isotherm parameters for a suite of soil types, using soil properties such as Fe and Al oxide content (Dari et al., 2015).

Example soil P results for agricultural soils in the Tarland catchment are shown in Figure 10, assuming an initial labile soil P content of  $585 \text{ mg kg}^{-1}$ , an initial  $EPC_0$  of  $0.1 \text{ mg l}^{-1}$ , soil depth of 9.5 cm and annual net P inputs of  $10 \text{ kg ha}^{-1} \text{yr}^{-1}$ . Soil water TDP concentrations are slightly higher than the  $EPC_0$  because of P inputs to the soil water, resulting in net adsorption and a gradual increase in labile P and  $EPC_0$  over time.

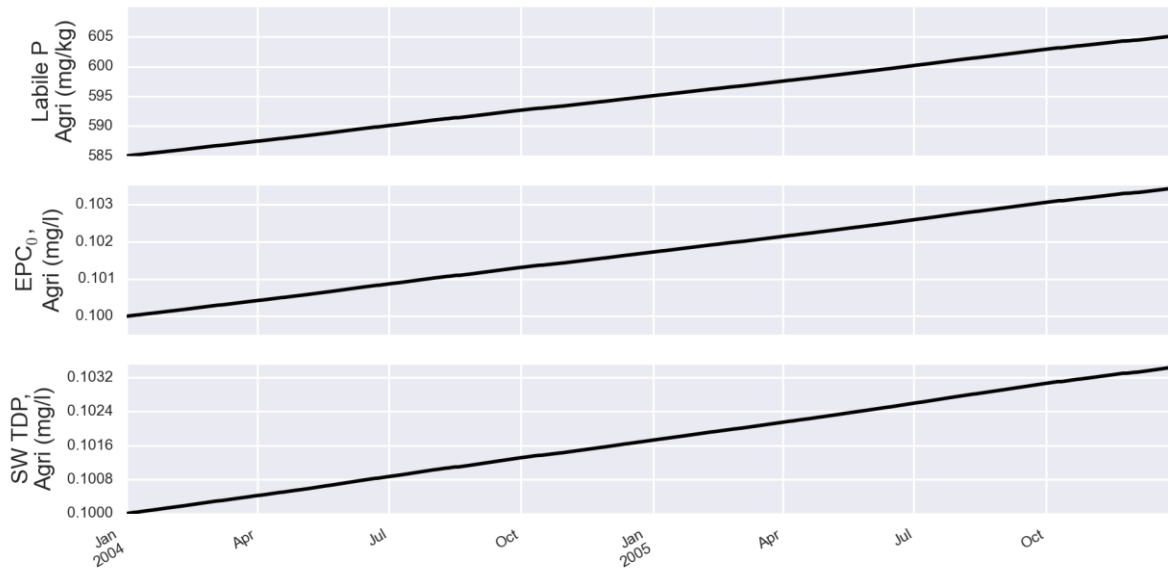


Figure 10: Simulated change in agricultural soil labile P content, soil water (SW) EPC<sub>0</sub> and soil water TDP concentration over a two year period, assuming a soil depth of 9.5 cm and net P inputs of 10 kg ha<sup>-1</sup> year<sup>-1</sup>.

### c) Newly-converted land

A potential use of the model is to explore the impact of land use change on surface water P concentrations and loads. This land use change could be the conversion of agricultural land to semi-natural land, or vice versa. Land that has recently changed use will retain many of its previous characteristics, and cannot therefore be grouped with long-established land of the same use. Of particular importance for P and water quality is legacy soil P, the store of P that builds up in agricultural soil over years of high P application rates. Such legacy P may result in sustained high leaching and PP losses from old agricultural land potentially for several decades after reductions in fertilization (Jarvie et al., 2013b). Likewise the lack of legacy soil P in new agricultural land, recently converted from semi-natural land, may result in low P losses compared to well-established agricultural land.

To allow such effects to be simulated, a third ‘newly-converted’ land class was introduced into the model. Within each sub-catchment, this newly-converted land can be either semi-natural (initial labile soil P is equivalent to that on agricultural land) or agricultural (no labile soil P at the start of the model run). Two additional ODEs are then introduced: the change in labile soil P on newly-converted land with time and the change in soil water TDP with time. These take the same form as Equation 33 and Equation 34, respectively. EPC<sub>0</sub> is also calculated for the newly-converted class, and there is one additional user-input parameter,  $P_{netInput}$ . On new semi-natural land this is likely to be a negative, with net uptake of P from the soil. Otherwise, newly converted semi-natural land is grouped with existing semi-natural land, and likewise for agricultural, for other parameterisations and processes.

### d) TDP flux to the stream from soil water and quick flow

The TDP input to the stream transported by soil water flow is calculated by summing the inputs from agricultural land and any newly-converted semi-natural or agricultural land (Equation 35).

Equation 35: TDP input to the reach from soil water flow,  $TDP_{s,land}$  (kg day<sup>-1</sup>), where  $i$  denotes the land use class (A: agricultural, NC: newly-converted semi-natural or agricultural)

$$TDP_{s,land} = \sum_{i=A,NC} f_i(1 - \beta)Q_s \left( \frac{TDP_s^i}{V_s} \right)$$

The flux of TDP to the water course from the reach via quick flow is given by Equation 36. The majority of the flow pathways that make up quick flow inputs to the stream interact with the soil surface (e.g. infiltration and saturation excess flow) or are sourced from soil water (e.g. tile drainage). It was therefore assumed that quick flow inherits soil water TDP concentration. This may be conservative in areas where there is substantial runoff from farmyards, which may have TDP (and PP) concentrations which are well above those found in soil water, or if quick flow events occur directly after fertilizer or manure are applied.

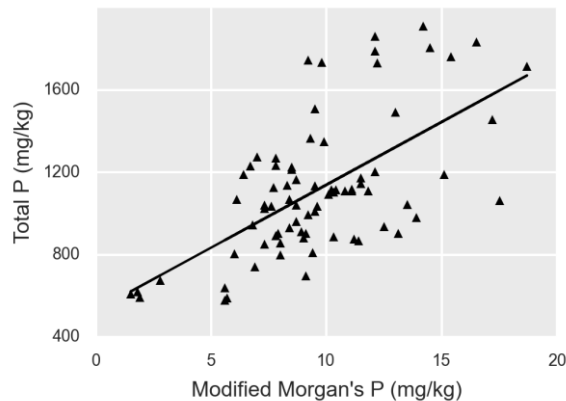
*Equation 36:* Quick flow TDP input to the reach from the land,  $TDP_{q,land}$  ( $\text{kg day}^{-1}$ ), where  $i$  denotes the land use class (A: agricultural, NC: newly-converted semi-natural or agricultural)

$$TDP_{q,land} = \sum_{i=A,NC} f_i Q_q \left( \frac{TDP_s^i}{V_s} \right)$$

#### e) Incorporating soil test P data

Soil P content is usually measured for agronomic purposes, where the aim is to measure plant-available P to help choose appropriate fertilizer application rates. Many procedures exist which aim to determine plant-available soil P; indeed, there are more than ten official methods used in Europe alone (Jordan-Meille et al., 2012). This soil test P data is much more common than total soil P data, so it would be useful for the model to be able to incorporate soil test P data, rather than relying on total soil P data alone. In principle soil test P could replace labile soil P in Equation 27, as long as two additional relationships can be defined:

- (1) A relationship between soil test P and total soil P, as total soil P content is still required for the PP simulation. There is always likely to be considerable scatter in this relationship due to varying soil chemistry, composition and texture. An analysis of Scottish soils data, for example, revealed a weak but significant relationship between total soil P and Modified Morgan's P:  $P_{total} = 61.1 P_{soilTest} + 529$  ( $n=77$ ,  $R^2=0.62$ ,  $p<0.001$ ), although as is clear in Figure 11, the uncertainty in total P predictions based on this equation would be substantial.



*Figure 11: Relationship between soil test P (Modified Morgan's P) and total soil P from a range of Scottish soils (M. Stutter, pers. comm.)*

- (2) A relationship describing the proportion of net total P inputs (e.g. from fertilizer and manure minus uptake) that enters the labile, soil test P store. Model testing showed that this ratio cannot be the same as that derived from the relationship between soil test P and total soil P. If this ratio were the same, a total P to soil test P ratio of around 60 (from the Scottish soils dataset above) would imply that  $1/60^{\text{th}}$  of net total P inputs enter the available P store. However, with a net P input of  $10 \text{ kg ha}^{-1} \text{ yr}^{-1}$  (typical for Scottish catchments), model testing showed that a ratio of  $<25$  is required to maintain plant-available P stores at their present-day value, and that the model is extremely sensitive to the value chosen.



The fact that these two additional relationships must be independently specified causes an increase in model complexity that was not felt to be justified by an increase in model realism. In particular, if linear relationships are used to relate total soil P and soil test P, and to relate soil test P and soil water  $EPC_0$ , then by definition there will also be a linear relationship between total soil P and soil water  $EPC_0$ , meaning the increase in complexity is not justified. It was therefore decided to maintain the model structure described in Section 4.3.1 (b). However, if soil test P data are available instead of total soil P data for a given area, the user could use a linear regression between soil test P and total soil P to derive the latter (e.g. using the regression derived above for Scottish soils data). A potential future extension to the model is for this calculation to be performed internally, using user-specified regression coefficients.

### 4.3.2 Groundwater phosphorus

The concentration of TDP in groundwater, as in soils, depends on historic P inputs and the P sorption capacity of the aquifer matrix. The latter is often largely controlled by the iron oxide content of the aquifer, with groundwater pH and dissolved oxygen content also playing an important role (Domagalski and Johnson, 2011), whilst co-precipitation with calcium carbonate is important in calcareous aquifers. These processes substantially reduce P mobility within the sub-surface, and traditionally groundwater has therefore only been considered to have negligible TDP concentrations and to dilute surface water P concentrations. However, it is now being increasingly recognised that groundwater TDP concentrations can become elevated by anthropogenic activities (e.g. Holman et al., 2008). Some areas in which groundwater has become enriched in P, for example due to elevated agricultural P inputs or prolonged disposal of sewage effluent, may potentially become net sources of P for decades after the original source of P has been removed (Stollenwerk, 1996).

Ideally, the model would therefore include a link between soil water and groundwater TDP concentrations, taking into account aquifer and groundwater geochemistry. However, the process-understanding needed to formalise this link is arguably not yet developed enough, and certainly the data on groundwater and aquifer geochemistry is hard to come by in many areas. There are therefore good practical reasons for adopting a simpler approach which does not take this process understanding into account. In addition, changes in groundwater TDP concentration over time are likely to be slow, being buffered by potentially large groundwater residence times and sorption reactions, and smaller than associated changes in soil water and effluent fluxes which will drive any changes in groundwater state. For these reasons, a very simplistic approach is taken in the model: dissolved P transport to the stream occurs via groundwater flow, but groundwater TDP concentration is assumed to be constant through time, maintained at a user-specified value ( $TDP_{g,conc}$ ; Equation 37. Variables are defined in Table 7).

*Equation 37:* Groundwater TDP input to the reach,  $TDP_{g,land}$  (kg day<sup>-1</sup>)

$$TDP_{g,land} = A_{SC} Q_g TDP_{g,conc}$$

This simplistic approach is a good starting point, but is only valid where the groundwater TDP concentration is indeed unlikely to change over the course of the model run. This is likely to be the case over sub-decadal time periods, in areas with large aquifers, where the groundwater matrix is rich in Fe oxides and/or where the groundwater is oxic. Caution should otherwise be employed. This is a potential area for future model development, the ultimate aim being to derive a simple relationship between soil water and groundwater TDP concentration using readily-measurable groundwater properties. A linear relationship could be a suitable starting point. The gradient of the line could be derived by making some assumptions to help estimate the location of two points on the line: point 1 could be current measured groundwater TDP concentration, corresponding with sub-catchment averaged soil water TDP concentration. The second point would require an estimate of the ‘pristine’, non-anthropogenic groundwater TDP concentration (e.g. based on space-for-time substitution of measured data), associated with soil water TDP concentrations in semi-natural land, plus knowledge or assumptions of the time taken for semi-natural groundwater to reach its current state.

### 4.3.3 In-stream phosphorus

The in-stream P process model simulates in-stream dilution of diffuse and point source P inputs and downstream transport. Parameters and variables used in the in-stream P equations are defined in Table 8.

Variable	Description	Units	Source
$A_{SC}$	Sub-catchment area	km <sup>2</sup>	Input parameter
$dPP_r/dt$	Change of PP mass in the reach with time	kg day <sup>-1</sup>	Equation 40
$dPP_{r,df}/dt$	Daily flux of PP from the stream reach	kg day <sup>-1</sup>	Equation 41
$dTDP_r/dt$	Rate of change of TDP mass in the reach with time	kg day <sup>-1</sup>	Equation 38
$dTDP_{r,df}/dt$	Daily flux of TDP from the stream reach	kg day <sup>-1</sup>	Equation 41
$E_{PP}$	Particulate P enrichment factor	None	Input parameter
$f_i$	Fraction of land use in each of the possible land use classes, $i$ , including agricultural (A; $f_{Ar} + f_{IG}$ ), arable (Ar), improved grassland (IG), semi-natural (SN), and newly-converted versions of all 3 (NC_i)	None	Input parameters
$M_{input}$	Sediment mass input to the reach from the land and in-stream entrainment	kg day <sup>-1</sup>	Equation 20
$M_{soil}$	Soil mass	kg	Equation 32
$P_{inactive}$	Soil inactive P mass	kg	Equation 30
$P_{labile}$	Soil labile P mass	kg	Equation 33
$PP_{input}$	PP input to the reach from the land and in-stream entrainment	kg day <sup>-1</sup>	Equation 39
$PP_r$	Mass of PP in the reach	kg	Equation 40
$PP_{r,conc}$	Daily mean concentration of PP in the reach	mg l <sup>-1</sup>	Equation 42
$PP_{r,df}$	Mean daily flux of PP from the reach	kg day <sup>-1</sup>	Equation 41
$PP_{r,US}$	PP input to the reach from upstream reaches	kg day <sup>-1</sup>	Model calculates
$Q_q$	Quick flow	mm day <sup>-1</sup>	Equation 5
$Q_r$	Instantaneous reach discharge	mm day <sup>-1</sup>	Equation 17
$Q_{r,av}$	Daily mean reach flow	mm day <sup>-1</sup>	Equation 18
$TDP_{eff}$	Effluent TDP input to the reach	kg day <sup>-1</sup>	Input parameter
$TDP_{g,land}$	Groundwater TDP input to the reach	kg day <sup>-1</sup>	Equation 37
$TDP_{q,land}$	Quick flow TDP input to the reach	kg day <sup>-1</sup>	Equation 36
$TDP_r$	Mass of TDP in the reach	kg	Equation 38
$TDP_{r,conc}$	Daily mean concentration of TDP in the reach	mg l <sup>-1</sup>	Equation 42
$TDP_{r,df}$	Mean daily flux of TDP from the reach	kg day <sup>-1</sup>	Equation 41
$TDP_{r,US}$	TDP input to the reach from upstream reaches	kg day <sup>-1</sup>	Model calculates
$TDP_{s,land}$	Soil water TDP input to the reach	kg day <sup>-1</sup>	Equation 35
$V_r$	Reach volume	mm	Equation 14

Table 8: Parameters and variables used in the in-stream P equations.

#### a) TDP

The rate of change in instream TDP mass with time depends on the difference between input and output fluxes. A simplistic representation is used, where inputs are from the land phase (quick, soil water and groundwater flow), sewage and upstream reaches, and the only output is reach outflow (Equation 38).

Equation 38: Rate of change in reach TDP mass,  $TDP_r$ , with time (kg day<sup>-1</sup>)

$$\frac{d TDP_r}{dt} = TDP_{q,land} + TDP_{s,land} + TDP_{g,land} + TDP_{eff} + TDP_{r,US} - Q_r \frac{TDP_r}{V_r}$$

This simple formulation assumes that instream TDP is in a state of dynamic equilibrium, i.e. instream sinks of TDP (e.g. adsorption and biological uptake) are balanced by instream sources (e.g. desorption and mineralisation). Studies have indicated that this balance between sources and sinks may in fact change through the year in response to changing concentrations (e.g. Stutter and Lumsdon, 2008). Retention is thought to be particularly important during low flows, due to biological uptake and sorption (House, 2003). Omitting TDP sinks from the model could therefore result in other P sources being over-estimated, particularly groundwater and effluent inputs. To determine whether an in-stream TDP sink is significant in a particular study catchment, data are needed to quantify the sink directly or to provide good constraints on groundwater and effluent inputs. In-stream processes may also become net sources or sinks of TDP if

equilibrium has not yet been reached or is disturbed, e.g. by a change in external loading. For example, reducing effluent P inputs may cause a reduction in water column TDP concentration, which may cause P-enriched bed sediments to release TDP until a new equilibrium state is reached (Stutter et al., 2010). By not incorporating this potential interaction between bed sediments and the water column, the model is not able to represent legacy sewage effluent P. However, as explained in Section 3.1, this legacy store is thought to be much smaller than other potential legacy P stores in the catchment, and to have a more rapid turnover time.

In many countries, soluble reactive P (SRP) is used by regulators to assess compliance with water quality standards, rather than TP or TDP. It is therefore desirable to be able to convert TDP to SRP. Models such as INCA-P do this using a simple linear regression with regression parameters supplied by the user. This approach works well in the majority of rivers, and as a starting point is recommended here. It has not been coded into the model, but the user can easily transform model output using their own regression equation. Different TDP sources may have very different SRP:TDP ratios, and a potential future extension could be to factor in different SRP:TDP ratios of different P sources.

#### b) PP

All PP is assumed to be sediment-bound, and so PP inputs to the water column are assumed to be proportional to sediment inputs (Equation 39). The mass of PP input to the stream is therefore simply the mass of sediment transported to the stream from each land use class,  $M_{input}$ , multiplied by the P content of the soil in that class and assuming unlimited soil P. This approach has the same limitations and caveats as the sediment equations (Section 4.2.1). It also assumes that changes in the P content of soils are instantly reflected in the composition of in-stream sediments, discounting time lags or potential in-stream PP stores. In-stream stores of P are relatively small and short-lived compared to terrestrial stores (Jarvie et al., 2013a), so it was felt that the additional complexity needed to account for these in-stream processes was not justified.

*Equation 39:* PP input to the reach,  $PP_{input}$  (kg day<sup>-1</sup>), where superscript i denotes the land use class

$$PP_{input} = E_{PP} M_{input}^i \sum_i f^i \frac{(P_{labile}^i + P_{inactive}^i)}{M_{soil}}$$

An enrichment factor,  $E_{PP}$ , represents the selective delivery to the stream of finer particles enriched in P compared to source soils (Sharpley, 1980). The use of a constant enrichment factor is a simplification; in reality there is a well-documented decrease in PP loss with increasing erosion (Radcliffe and Cabrera, 2006). This is because as runoff and erosion increase there is less particle size sorting, so P-enriched finer sediment makes up a smaller proportion of the total sediment mobilised. When assembling enrichment ratio information for the CREAMS model, Menzel (1980) concluded that a log-relationship between enrichment ratio and sediment yield appears to hold in a variety of conditions:  $\ln(E_{PP}) = 2.00 - 0.16 \ln(Y_{sed})$ , where  $Y_{sed}$  is the sediment yield (kg ha<sup>-1</sup>). A potential future extension to the model would be to investigate whether this additional complexity is warranted in some areas.

In Equation 39, PP inputs to the stream are summed over up to six land use classes: arable, improved grassland, semi-natural, and newly-converted versions of each (Section c). The sediment flux for newly-converted land corresponds to the same flux for established land. The rate of change in the mass of PP in the water column with time is then given by Equation 40. As with TDP, a simplistic representation of the associated fluxes is adopted: inputs are from the land phase and entrainment (grouped as one flux) and upstream reaches; the only output is via outflow from the reach. Sewage PP inputs are not included, as the majority of effluent P tends to be in dissolved form (Neal et al., 2005; Withers and Jarvie, 2008). As a starting point, in-stream desorption of TDP from PP is not accounted for. This is likely to be justified in rivers with relatively short residence times, but potentially less so in larger, slower-flowing rivers.

Equation 40: Rate of change in reach PP mass,  $PP_r$ , with time ( $\text{kg day}^{-1}$ )

$$\frac{d PP_r}{dt} = PP_{input} + PP_{r,US} - Q_r \frac{PP_r}{V_r}$$

c) Daily fluxes and mean daily concentrations of TDP and PP

Time series of total daily fluxes of TDP and PP leaving the reach are obtained by integrating the instantaneous fluxes with respect to time, starting each day with initial conditions of zero (Equation 41). These total daily fluxes are then used in the calculation of daily mean TDP and PP concentrations (Equation 42), converted from units of  $\text{kg mm}^{-1}$  to  $\text{mg l}^{-1}$  for comparison with observations.

Equation 41: Rate of change of daily flux of dissolved and particulate P from the stream reach ( $\text{kg day}^{-1}$ )

$$\frac{dTDP_{r,df}}{dt} = Q_r \frac{TDP_r}{V_r}; \quad \frac{dPP_{r,df}}{dt} = Q_r \frac{PP_r}{V_r}$$

Equation 42: Daily mean concentrations of TDP and PP in the stream reach,  $TDP_{r,conc}$  and  $PP_{r,conc}$  ( $\text{mg l}^{-1}$ )

$$TDP_{r,conc} = \frac{TDP_{r,df}}{Q_{r,av}} \frac{1}{A_{SC}}; \quad PP_{r,conc} = \frac{PP_{r,df}}{Q_{r,av}} \frac{1}{A_{SC}}$$

#### 4.4 Summary of equations, initial conditions and input parameters

Table 9 summarises the 19 ODEs which are solved simultaneously for each reach in the catchment. For the first time step initial conditions must be supplied for each ODE. To define these, three parameters are specified by the user: in-stream flow in the top reach, total soil P content and soil water TDP concentration in the ‘high P’ class. If the snow module is run, initial snow depth is also required. All other initial conditions are derived from these parameters or using simple assumptions – details are provided in Table 9. Initial instream masses of SS, PP and TDP are set to 0, so a burn-in period is required (the length of burn-in depends on the residence time in the reach, but should be of the order of days – weeks).

ODE	Equation	Initial conditions (first time step)
$dV_s/dt$ For agricultural & semi-natural	Equation 6	$V_{s,0} = V_{FC}$
$dQ_s/dt$ For agricultural & semi-natural	Equation 10	$Q_{s,0}^i = \frac{V_s^i - V_{FC}}{T_s^i(1 + e^{V_{FC} - V_s^i})}$ ; where superscript i denotes the land class
$dV_g/dt$	Equation 11	$V_{g,0} = Q_{g,0} T_g$
$dQ_g/dt$	Equation 13	$Q_{g,0} = \beta Q_{s,0}$
$dV_r/dt$	Equation 14	$V_{r,0} = Q_{r,0} T_{r,0}$ ; where $T_{r,0} = \frac{L_{reach}}{8.64 \times 10^4 a Q_{r,0}^{0.42}}$
$dQ_r/dt$	Equation 17	Reach 1: Input parameter $Q_{r,0,init}$ (units converted to $\text{mm day}^{-1}$ in model) Downstream reaches: $Q_{r,0} = Q_{r,av}$ from the upstream reach for day 1
$dQ_{r,av}/dt$	Equation 18	0.0
$dM_{sus}/dt$	Equation 19	0.0
$dM_{sus,out}/dt$	Equation 23	0.0
$dP_{labile}/dt$ For arable & newly-converted	Equation 33	Equation 31
$dTDP_s/dt$ For agricultural & new semi-natural	Equation 34	$TDP_{s,0} = A_{SC} EPC_{0,user} V_s$
$dTDP_r/dt$	Equation 38	0.0
$dTDP_{r,out}/dt$	Equation 41	0.0
$dPP_r/dt$	Equation 40	0.0
$dPP_{r,out}/dt$	Equation 41	0.0

Table 9: Ordinary differential equations (ODEs) solved within the model and information on how the initial conditions are defined for the first time step.

The model requires a number of parameters which should be calculated for example using a GIS (Table 10). These parameter values are likely to be well-constrained, and therefore generally will not form part of any calibration procedure (although if they are uncertain they could be included in an uncertainty analysis).

Param	Units	Description
$A_{SC}$	km <sup>2</sup>	Sub-catchment area
$f_{Ar}$	none	Proportion of arable or other high soil P, high erodibility land (excluding newly-converted from SN)
$f_{IG}$	none	Proportion of improved grassland or other high soil P, moderate erodibility land (excluding newly-converted from SN)
$f_s$	none	Proportion of semi-natural and other low soil P land (excluding newly-converted from agricultural)
$f_{NC\_Ar}$	none	Proportion of newly-converted arable land (from SN)
$f_{NC\_IG}$	none	Proportion of newly-converted improved grassland (from SN)
$f_{NC\_S}$	none	Proportion of newly-converted semi-natural land (from agricultural)
$f_{spr}$	none	Proportion spring-sown crops make to total arable land area (assume rest is autumn-sown)
$S_{Ar}$	degrees	Mean slope of arable land in the sub-catchment
$S_{IG}$	degrees	Mean slope of improved grassland in the sub-catchment
$S_{SN}$	degrees	Mean slope of semi-natural land in the sub-catchment
$L_{reach}$	m	Reach length
$S_{reach}$	degrees	Reach slope (ideally length-weighted)

Table 10: General model parameters derived using a GIS, whose values will usually be kept constant during model calibration.

The remaining model parameters are likely to be less well constrained, and are summarised in Table 11, together with suggested default values, recommended ranges, and potential data sources that could be used to inform the parameter values. An additional model parameter,  $C_{measures}$ , is not a calibration parameter and is only given a value when the user wishes to investigate the impact of sediment reduction measures on in-stream SS and PP concentrations or loads. There are 23 parameters in Table 11, 24-27 when spatial variability between land use classes is taken into account. Only one of these varies by sub-catchment or reach (effluent inputs), and so model complexity will not increase substantially in larger systems compared to smaller ones. At least 8 of these model parameters are optional (before taking spatial variability into account; Table 11), so in a given setup the actual number of parameters requiring calibration may be much less than 27. Even in the most complex setup in which all 27 parameters are required, an algorithm could potentially search the entire parameter space so that all could be auto-calibrated, provided the user has a full suite of water quality observations for calibration and testing (i.e. observed discharge, suspended sediment, dissolved and particulate P concentrations under the full range of flow conditions). In addition, plausible ranges for the majority of parameters may be based on measured data or data derived from literature reviews. Only four or five parameters must be determined purely through calibration (Table 11). One of these unmeasurable parameters relates to the suspended sediment simulation ( $E_M$ ); the rest are hydrology parameters.

Table 11: SimplyP model parameters, including default values, recommended ranges and possible data sources. ‘Spatial’ column describes whether the parameter varies spatially by land use (LU), in which case by which LU type (A: agricultural, S: seminatural, Ar: arable, IG: improved grassland), or sub-catchment/reach (SC/R). Parameters likely to be key in most settings are marked with an asterisk. Many of those without an asterisk are optional. Q is discharge

Type	Param	Units	Description	Spatial	Tarland	Default	Min	Max	Data sources
Snow	D <sub>snow,0</sub>	mm	Initial snow depth	–	0	0	0	1000	Meteorological records
	f <sub>DDSM</sub>	mm dd°C <sup>-1</sup>	Degree-day factor for snow melt	–	2.74	2.74	1.6	6	Literature, e.g. USDA (2004)
Hydrology	*T <sub>s</sub>	days	Soil water time constant	LU (A, S)	A: 2 S: 10	A: 1 S: 10	> 0	30	<i>Calibration</i>
	f <sub>quick</sub>	none	Proportion of precipitation routed to quick flow	–	0.02	0.02	0	0.2	<i>Calibration</i>
	alpha	none	PET reduction factor	–	1	1	0.4	1.2	Literature, e.g. Allen et al. (1998)
	*FC	mm	Soil field capacity	–	290	300	100	400	Soils database, or from soil texture using conversion charts (e.g. Appendix, Figure A1)
	*beta	none	Baseflow index	–	0.70	0.60	0	1	Local or global databases (e.g. Beck et al., 2013)
	*T <sub>g</sub>	days	Baseflow recession constant	–	65	65	> 0	100	May be estimated from Q data using methods of Van Dijk (2010); see Beck et al. (2013) for a global analysis
	Q <sub>g,min</sub>	mm d <sup>-1</sup>	Minimum groundwater flow	–	0.4	0.0	0	2	<i>Calibration</i>
	a	m <sup>-2</sup>	Gradient of stream velocity-Q relationship	–	0.5	0.5	0.1	0.8	Empirically-derived from paired velocity and Q measurements (e.g. from flow gauging)
Q <sub>r0_init</sub>	m <sup>3</sup> s <sup>-1</sup>	Initial in-stream Q	–	1.0	1.0	> 0	N/A	Q observations	
Sediment	C <sub>cover</sub>	None	Vegetation cover factor (ratio of erosion rates under the land class vs bare soil)	LU (Ar, IG, S)	A: 0.2 S: 0.021 IG: 0.09	A: 0.2 S: 0.021 IG: 0.09	0	1	(R)USLE literature, e.g. Panagos et al. (2015)
	*E <sub>M</sub>	kg mm <sup>-1</sup>	Sediment input scaling factor	–	1500	1500	0	5000	<i>Calibration</i>
	*k <sub>M</sub>	none	Sediment input non-linear coefficient	–	2.0	2.0	1.2	3	Empirical relationship between Q and SS observations or literature (e.g. Asselman, 2000)
	d <sub>maxE,spr</sub>	none	Julian day with max erodibility; spring-sown crops	–	60	60	1	365	Local agronomic practices
	d <sub>maxE,aut</sub>	none	Julian day with max erodibility, autumn-sown crops	–	304	304	1	365	Local agronomic practices
Dissolved P	*P <sub>soilConc</sub>	mg kg <sup>-1</sup>	Initial total soil P content	LU (A, S)	A: 1458 S: 873	A: 1458 S: 873	0-400	>300	Soils database. Estimate from soil test P data using an empirical relationship
	*P <sub>netInput</sub>	kg ha <sup>-1</sup> yr <sup>-1</sup>	Net annual P input to the soil (negative if uptake > input); S fixed at 0	LU (A)	10	10	-30	30	Fertilizer and manure application surveys, literature for P uptake, national P balance inventories (e.g. eurostat, 2013, for EU countries)
	*EPC <sub>0,init</sub>	mg l <sup>-1</sup>	Initial soil water TDP concentration on agricultural land	LU (A)	0.1	0.1	0	2	Direct measurements, literature
	*M <sub>soil,m2</sub>	kg m <sup>-2</sup>	Soil mass per m <sup>2</sup> , important in determining the initial soil labile P mass	–	95	100	>0	800	Soils data (bulk density and depth)
	*TDP <sub>eff</sub>	kg day <sup>-1</sup>	Reach effluent TDP inputs	SC/R	0.1	0	0	N/A	Water company/environment protection agency data
	*TDP <sub>g</sub>	mg l <sup>-1</sup>	Groundwater TDP concentration	–	0.02	0	0	2	Direct measurements or literature
PP	*E <sub>PP</sub>	none	PP enrichment factor	–	1.6	1	1	6	Direct measurements or literature (e.g. Sharpley, 1980)

## 4.5 Numerical methods

The model equations summarised in Section 4.4 must be solved numerically. Simply put, this involves providing initial conditions describing the state of the system, and then using the model equations to project forward in time to predict the new state of the system at the end of the time step. This then becomes the initial condition for the next time step, and the process is repeated. This process of numerical approximation introduces errors, and minimizing these errors by formulating and solving the governing model equations in a robust way is an important part of the model development process. Indeed, Clark and Kavetski (2010) suggest that in some cases numerical errors may be larger than model structural errors. Additional benefits of a robust numerical model include a smoother objective function relating model input parameters and model output (Kavetski et al., 2006a), which may reduce model calibration difficulties by allowing powerful classical parameter analysis techniques for optimisation and uncertainty analysis to be used. Kavetski et al. (2006b) argue that many of the difficulties in hydrological modelling over the last two decades, which have prompted the development of complex parameter estimation tools, are in fact due to (1) discontinuous model structures, where sharp internal thresholds introduce non-smoothness into the objective function, and to (2) poor choice of ODE solver. An attempt was made to avoid the first of these issues by avoiding thresholds in the model equations (e.g. using continuous functions rather than logic checks in equations in Section 4.1.2b). The final part of the model-building process was then to choose an appropriate ODE solver. Three factors were taken into account: (1) whether the solver is appropriate for stiff or non-stiff equations, related to the time-stepping scheme used (see below); (2) popularity, and (3) availability.

Differential equations may be categorised as stiff or non-stiff. Generally speaking, stiff equations include some terms which can lead to rapid variation in the solution, which means that certain numerical methods for solving them are unstable unless the step size taken is excessively small in relation to the smoothness of the exact solution. Time-stepping in this context relates to the sub-steps the model time step is broken down into by the solver. Most of the classical numerical methods for solving ODEs are only suitable for non-stiff ODEs (e.g. the simple Euler method, the 4<sup>th</sup> order and various adaptive Runge-Kutta methods and the multi-step Adams' method). If applied to stiff systems, these methods are likely to be inaccurate or prohibitively slow. Many ODE systems are stiff in practice, and a wide range of off-the-shelf ODE solvers are available which are able to adapt their time-stepping routine and fluctuate between using stiff or non-stiff solvers. It is therefore surprising that many catchment models continue to use simple, often unsuitable solvers (Kavetski and Clark, 2011). Here, the LSODA solver was chosen, taken from the FORTRAN ODPEPACK library (Hindmarsh, 1983). LSODA starts using a non-stiff method (an Adams predictor-corrector method) and dynamically monitors the data, if necessary switching to a stiff method (the multi-step Backward Differentiation Formula method). LSODA is both widely-used and easy to implement using the SciPy.integrate module's odeint function.

The solver's error tolerance parameters affect the precision of the result, with a smaller error tolerance resulting in more time steps and greater precision but longer run times. Testing showed an approximate log relationship between run times and the relative error tolerance parameter (*rtol*), with a decrease in run times of around 70% for an increase in *rtol* from the default of  $1 \times 10^{-8}$  to 0.05. *rtol* was set to 0.01, to optimise the trade-off between decrease in run time and loss in accuracy. The maximum number of within-timestep function evaluations was set to 5000, to prevent the solver reaching the maximum threshold before finding a solution within the required error tolerance, which could introduce errors.

## 5. Future model development priorities

A number of potential areas for model improvement are highlighted throughout Section 4 and are summarised in Table 12. Most of these suggestions involve an increase in model complexity, and before being adopted any increase in complexity needs to be justified by demonstrating a substantial increase in model performance, preferably within a statistical model comparison framework. To help prioritise areas for model improvement from within this list (or indeed to highlight other areas), the model needs to be tested in

a range of contrasting catchments, including catchments where internal processes and fluxes have been measured.

Additional general recommendations for model improvement include:

- On a practical level, the model is currently slow to run compared to professionally-coded models such as INCA-P. This may be because of the choice of ODE solver, which is sophisticated compared to the solvers employed by most water quality models, or because the model is coded in Python rather than a faster, lower-level language such as C<sup>++</sup>. Other solvers should be investigated for speed.
- At present, there is no flexibility in the model in terms of the number of land use classes, which are fixed at two (for dissolved P processes) or three (for sediment and PP). This reduces the versatility of the model, and future development to increase flexibility in this regard could widen the appeal of the model. However, it would also require a re-conceptualisation of the soil P equations.
- As pointed out by Adams et al. (2016), new monitoring techniques mean that high frequency P concentration measurements are now available, e.g. at 30 minute resolution, and yet many popular water quality models are only able to simulate at a daily resolution. A simple change to the model described here would be to allow the user to specify the time step required.
- Improved representation of critical source areas, by taking spatial variability in hydrology, sediment and phosphorus sources, mobilisation processes and transport/delivery pathways into account in a fuller way.



<p><b>Hydrology and snow:</b></p> <ul style="list-style-type: none"> <li>• Add in a PET calculation, so that the model can be run using just precipitation and temperature as inputs.</li> <li>• Refinements needed to the simple degree-day approach to simulating snow melt in areas with higher snowfall?</li> <li>• Include a more detailed representation of temperature variation throughout a day in the snow melt calculation.</li> <li>• Is model performance improved by adding a parameter to define a lower threshold for precipitation inputs, below which quick flow is zero?</li> <li>• Should quick flow be varied by land class? If so, is there still a need for different soil water time constants in the land classes?</li> <li>• Add an upper limit to the soil water volume (at the saturation capacity); water above this is routed to quick flow.</li> <li>• Replace the minimum groundwater flow threshold parameter with a more process-based representation. E.g. factor in percolation from the soil when soil water level drops below field capacity, but at a reduced rate.</li> </ul>
<p><b>Sediment:</b></p> <ul style="list-style-type: none"> <li>• Should the sediment equations be amended to attempt to track the store of sediment in the near-channel sources, to be able to simulate source-exhaustion?</li> <li>• Soil erodibility may also be affected by soil wetness, which could be factored in to Equation 21.</li> <li>• The slope factor in Equation 21 could be altered to be more representative of potential sediment source areas. E.g. the average slope of land within a certain distance of the watercourse.</li> <li>• An additional factor could be introduced to Equation 21 to represent connectivity between sediment source areas and the watercourse.</li> <li>• The <math>C_{cover}</math> factor for semi-natural land could be extended to incorporate knowledge on the factors which affect erodibility, such as grazing, burning and felling.</li> <li>• More testing is required to determine whether the additional complexity of a dynamic <math>C_{cover}</math> factor is warranted, and if so whether the adopted approach is suitable.</li> <li>• Under what circumstances should sediment deposition to the stream bed be taken into account, and how could this relatively complex process be represented in a simple way?</li> <li>• Can reach sediment (and PP) inputs be split into inputs from the land versus bank erosion in a simple way? Work on sediment fingerprinting may help.</li> <li>• Should a distinction be made between allochthonous &amp; autochthonous in-stream sediment and PP?</li> </ul>
<p><b>Phosphorus:</b></p> <ul style="list-style-type: none"> <li>• Add in an option for the net P input parameter to be dynamic, for example as a user-input time series. In addition, a link between soil P content and net P uptake would improve simulations of the longer term soil P dynamics (though is likely to require soil test P to be simulated).</li> <li>• Geochemical models or lab experiments could inform the adsorption coefficient in Equation 27, e.g. by providing a range of parameters for a suite of soil types with a range of P sorption capacities.</li> <li>• Add the ability to input soil P as soil test P rather than total soil P. This could be a user-specified linear relationship, but a more advanced geochemical representation may be required for meaningful results to be obtained.</li> <li>• A dynamic PP enrichment factor could replace the constant, for example linked to discharge.</li> <li>• To simulate legacy groundwater TDP, a simple link is needed between soil water and groundwater TDP concentration, predictable using readily-measurable groundwater properties.</li> <li>• Add in an option for effluent inputs to be read in from a time series, rather than being constant.</li> <li>• When/where is it necessary to explicitly account for in-stream TDP sinks (e.g. adsorption or biological uptake of sewage effluent P)? A simple decay factor may be sufficient.</li> <li>• When/where should P desorption from the stream bed be simulated? How should this be done?</li> <li>• For reaches with longer residence times, a link may be needed between in-stream PP and TDP.</li> <li>• Sewage PP inputs could be added.</li> <li>• More process-based representation of septic tank inputs.</li> <li>• Ability to predict SRP concentrations, either using a simple linear regression between TDP and SRP, or by taking into account the TDP:SRP ratio of agricultural versus sewage effluent P inputs.</li> </ul>

Table 12: Examples of areas for future model development.

## References

- Allen, R., Pereira, L., Raes, D., and Smith, M. (1998). "Crop evapotranspiration – guidelines for computing crop water requirements. FAO irrigation and drainage paper 56."
- Asselman, N. E. M. (2000). Fitting and interpretation of sediment rating curves. *Journal of Hydrology* **234**, 228-248.
- Bagnold, R. (1966). An approach to the sediment transport problem. *General Physics Geological Survey, Prof. paper*.
- Beck, H. E., Dijk, A. I., Miralles, D. G., Jeu, R. A., McVicar, T. R., and Schellekens, J. (2013). Global patterns in base flow index and recession based on streamflow observations from 3394 catchments. *Water Resources Research* **49**, 7843-7863.

- Bowes, M. J., House, W. A., Hodgkinson, R. A., and Leach, D. V. (2005). Phosphorus–discharge hysteresis during storm events along a river catchment: the River Swale, UK. *Water Research* **39**, 751-762.
- Chapra, S. C. (2008). "Surface water-quality modeling," Waveland press.
- Clark, M. P., and Kavetski, D. (2010). Ancient numerical daemons of conceptual hydrological modeling: 1. Fidelity and efficiency of time stepping schemes. *Water Resources Research* **46**, W10510.
- Colby, B. (1956). "Relationship of sediment discharge to streamflow," Rep. No. 2331-1258. US Dept. of the Interior, Geological Survey, Water Resources Division.
- Croke, B. F., Andrews, F., Jakeman, A. J., Cuddy, S. M., and Luddy, A. (2006). IHACRES Classic Plus: a redesign of the IHACRES rainfall-runoff model. *Environmental Modelling & Software* **21**, 426-427.
- Dari, B., Nair, V., Colee, J., Harris, W., and Mylavarapu, R. (2015). Estimation of Isotherm Parameters: A Simple and Cost-effective Procedure. *Frontiers in Environmental Science* **3**.
- Dean, S., Freer, J., Beven, K., Wade, A. J., and Butterfield, D. (2009). Uncertainty assessment of a process-based integrated catchment model of phosphorus. *Stochastic environmental research and risk assessment* **23**, 991-1010.
- Domagalski, J. L., and Johnson, H. M. (2011). Subsurface transport of orthophosphate in five agricultural watersheds, USA. *Journal of Hydrology* **409**, 157-171.
- eurostat (2013). Agri-environmental indicator fact sheet - risk of pollution by phosphorus. In "European Union (EU) agri-environmental indicator fact sheets".
- Fenicia, F., Kavetski, D., and Savenije, H. H. G. (2011). Elements of a flexible approach for conceptual hydrological modeling: 1. Motivation and theoretical development. *Water Resources Research* **47**, n/a-n/a.
- Fenicia, F., Savenije, H. H. G., Matgen, P., and Pfister, L. (2006). Is the groundwater reservoir linear? Learning from data in hydrological modelling. *Hydrol. Earth Syst. Sci.* **10**, 139-150.
- Futter, M. N., Erlandsson, M. A., Butterfield, D., Whitehead, P. G., Oni, S. K., and Wade, A. J. (2014). PERSiST: a flexible rainfall-runoff modelling toolkit for use with the INCA family of models. *Hydrol. Earth Syst. Sci.* **18**, 855-873.
- Gan, R., and Luo, Y. (2013). Using the nonlinear aquifer storage–discharge relationship to simulate the base flow of glacier- and snowmelt-dominated basins in northwest China. *Hydrol. Earth Syst. Sci.* **17**, 3577-3586.
- Hindmarsh, A. C. (1983). ODEPACK, A Systematized Collection of ODE Solvers, RS Stepleman et al.(eds.), North-Holland, Amsterdam,(vol. 1 of), pp. 55-64. *IMACS transactions on scientific computation* **1**, 55-64.
- Holman, I. P., Whelan, M. J., Howden, N. J. K., Bellamy, P. H., Willby, N. J., Rivas-Casado, M., and McConvey, P. (2008). Phosphorus in groundwater—an overlooked contributor to eutrophication? *Hydrological Processes* **22**, 5121-5127.
- House, W. A. (2003). Geochemical cycling of phosphorus in rivers. *Applied Geochemistry* **18**, 739-748.
- Jackson-Blake, L. A., Dunn, S. M., Helliwell, R. C., Skeffington, R. A., Stutter, M. I., and Wade, A. J. (2015). How well can we model stream phosphorus concentrations in agricultural catchments? *Environmental Modelling & Software* **64**, 31-46.
- Jackson-Blake, L. A., and Starrfelt, J. (2015). Do higher data frequency and Bayesian auto-calibration lead to better model calibration? Insights from an application of INCA-P, a process-based river phosphorus model. *Journal of Hydrology* **527**, 641-655.
- Jarvie, H. P., Sharpley, A. N., Spears, B., Buda, A. R., May, L., and Kleinman, P. J. A. (2013a). Water Quality Remediation Faces Unprecedented Challenges from “Legacy Phosphorus”. *Environmental Science & Technology* **47**, 8997-8998.
- Jarvie, H. P., Sharpley, A. N., Withers, P. J. A., Scott, J. T., Haggard, B. E., and Neal, C. (2013b). Phosphorus Mitigation to Control River Eutrophication: Murky Waters, Inconvenient Truths, and “Postnormal” Science. *J. Environ. Qual.* **42**, 295-304.
- Jordan-Meille, L., Rubæk, G. H., Ehlert, P. A. I., Genot, V., Hofman, G., Goulding, K., Recknagel, J., Provolo, G., and Barraclough, P. (2012). An overview of fertilizer-P recommendations in Europe: soil testing, calibration and fertilizer recommendations. *Soil Use and Management* **28**, 419-435.
- Kavetski, D., and Clark, M. P. (2011). Numerical troubles in conceptual hydrology: Approximations, absurdities and impact on hypothesis testing. *Hydrological Processes* **25**, 661-670.
- Kavetski, D., Kuczera, G., and Franks, S. W. (2006a). Calibration of conceptual hydrological models revisited: 1. Overcoming numerical artefacts. *Journal of Hydrology* **320**, 173-186.
- Kavetski, D., Kuczera, G., and Franks, S. W. (2006b). Calibration of conceptual hydrological models revisited: 2. Improving optimisation and analysis. *Journal of Hydrology* **320**, 187-201.
- Kinnell, P. I. A. (2010). Event soil loss, runoff and the Universal Soil Loss Equation family of models: A review. *Journal of Hydrology* **385**, 384-397.

- Kleinman, P., Sharpley, A., Buda, A., McDowell, R., and Allen, A. (2011). Soil controls of phosphorus in runoff: Management barriers and opportunities. *Canadian Journal of Soil Science* **91**, 329-338.
- Lefrançois, J., Grimaldi, C., Gascuel-Oudou, C., and Gilliet, N. (2007). Suspended sediment and discharge relationships to identify bank degradation as a main sediment source on small agricultural catchments. *Hydrological Processes* **21**, 2923-2933.
- Leopold, L. B., and Maddock Jr, T. (1953). "The hydraulic geometry of stream channels and some physiographic implications," Rep. No. 2330-7102.
- Luo, Y., Arnold, J., Allen, P., and Chen, X. (2012). Baseflow simulation using SWAT model in an inland river basin in Tianshan Mountains, Northwest China. *Hydrol. Earth Syst. Sci.* **16**, 1259-1267.
- McCray, J. E., Kirkland, S. L., Siegrist, R. L., and Thyne, G. D. (2005). Model Parameters for Simulating Fate and Transport of On-Site Wastewater Nutrients. *Ground Water* **43**, 628-639.
- Menzel, R. (1980). Enrichment ratios for water quality modeling. *CREAMS: A Field-Scale Model for Chemicals, Runoff, and Erosion from Agricultural Management Systems Conservation Research Report Number 26, May, 1980. p 486-492, 1 Fig, 2 Tab, 11 Ref.*
- Merritt, W. S., Letcher, R. A., and Jakeman, A. J. (2003). A review of erosion and sediment transport models. *Environmental Modelling & Software* **18**, 761-799.
- Neal, C., Jarvie, H. P., Neal, M., Love, A. J., Hill, L., and Wickham, H. (2005). Water quality of treated sewage effluent in a rural area of the upper Thames Basin, southern England, and the impacts of such effluents on riverine phosphorus concentrations. *Journal of Hydrology* **304**, 103-117.
- Oeurng, C., Sauvage, S., and Sánchez-Pérez, J.-M. (2010). Dynamics of suspended sediment transport and yield in a large agricultural catchment, southwest France. *Earth Surface Processes and Landforms* **35**, 1289-1301.
- Panagos, P., Borrelli, P., Meusburger, K., Alewell, C., Lugato, E., and Montanarella, L. (2015). Estimating the soil erosion cover-management factor at the European scale. *Land Use Policy* **48**, 38-50.
- Radcliffe, D. E., and Cabrera, M. L. (2006). "Modeling phosphorus in the environment," CRC Press.
- Ratliff, L. F., Ritchie, J. T., and Cassel, D. K. (1983). Field-Measured Limits of Soil Water Availability as Related to Laboratory-Measured Properties1. *Soil Science Society of America Journal* **47**.
- Renard, K. G., Foster, G. R., Weesies, G. A., and Porter, J. P. (1991). RUSLE: Revised universal soil loss equation. *Journal of soil and Water Conservation* **46**, 30-33.
- Sample, J. (2015). Statistics notes for environmental modelling. GitHub.
- Sharpley, A., Jarvie, H. P., Buda, A., May, L., Spears, B., and Kleinman, P. (2013). Phosphorus Legacy: Overcoming the Effects of Past Management Practices to Mitigate Future Water Quality Impairment. *J. Environ. Qual.* **42**, 1308-1326.
- Sharpley, A. N. (1980). The Enrichment of Soil Phosphorus in Runoff Sediments1. *J. Environ. Qual.* **9**, 521-526.
- Starrfelt, J., and Kaste, O. (2014). Bayesian uncertainty assessment of a semi-distributed integrated catchment model of phosphorus transport. *Environmental Science: Processes & Impacts* **16**, 1578-1587.
- Stollenwerk, K. G. (1996). Simulation of phosphate transport in sewage-contaminated groundwater, Cape Cod, Massachusetts. *Applied Geochemistry* **11**, 317-324.
- Stutter, M. I., Demars, B. O. L., and Langan, S. J. (2010). River phosphorus cycling: Separating biotic and abiotic uptake during short-term changes in sewage effluent loading. *Water Research* **44**, 4425-4436.
- Stutter, M. I., Langan, S. J., Lumsdon, D. G., and Clark, L. M. (2009). Multi-element signatures of stream sediments and sources under moderate to low flow conditions. *Applied Geochemistry* **24**, 800-809.
- Stutter, M. I., and Lumsdon, D. G. (2008). Interactions of land use and dynamic river conditions on sorption equilibria between benthic sediments and river soluble reactive phosphorus concentrations. *Water Research* **42**, 4249-4260.
- Trimble, S. W. (2010). Streams, valleys and floodplains in the sediment cascade. *Sediment Cascades: An Integrated Approach*, 307-343.
- Twarakavi, N. K. C., Sakai, M., and Šimůnek, J. (2009). An objective analysis of the dynamic nature of field capacity. *Water Resources Research* **45**, n/a-n/a.
- USDA (2004). "National Engineering Handbook, Part 630 - Hydrology, Chapter 11 (Snowmelt)." United States Department of Agriculture, Natural Resources Conservation Service.
- Van Dijk, A. (2010). Climate and terrain factors explaining streamflow response and recession in Australian catchments. *Hydrology and Earth System Sciences* **14**, 159-169.
- Wischmeier, W. C., and Smith, D. D. (1965). "Predicting rainfall-erosion losses from cropland east of the Rocky Mountains.," US Department of Agriculture (USDA), Washington DC.

- Wischmeier, W. C., and Smith, D. D. (1978). "Predicting rainfall erosion losses - a guide to conservation planning," US Department of Agriculture (USDA), Washington DC.
- Withers, P. J. A., and Jarvie, H. P. (2008). Delivery and cycling of phosphorus in rivers: A review. *Science of the Total Environment* **400**, 379-395.
- Wittenberg, H. (1999). Baseflow recession and recharge as nonlinear storage processes. *Hydrological Processes* **13**, 715-726.
- Wolman, M., Miller, J., and Leopold, L. (1964). Fluvial processes in geomorphology. *San Francisco*.

## Appendix A: Data to help with model parameterisation

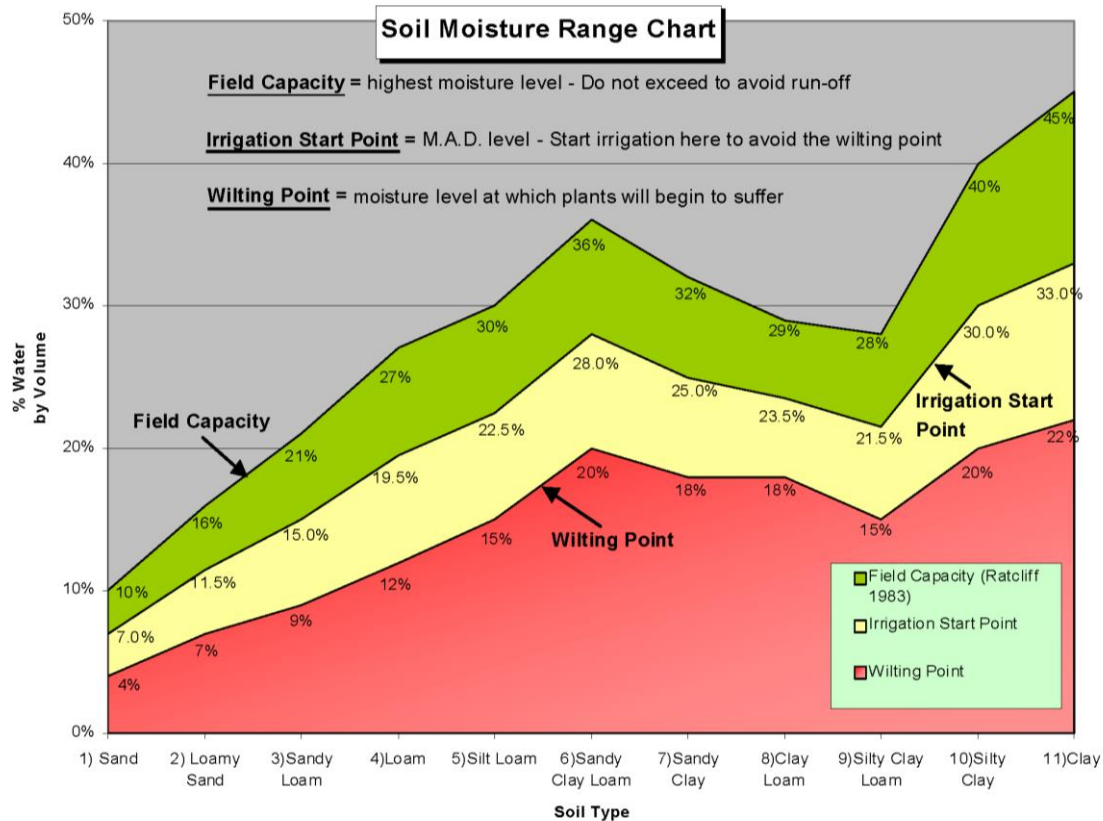


Figure A1: Chart for estimating field capacity based on soil texture, if only the latter is known.

Source: [ftp://ftp.dynamax.com/turf\\_irrigation/Soil%20Moisture%20Range%20Chart.pdf](ftp://ftp.dynamax.com/turf_irrigation/Soil%20Moisture%20Range%20Chart.pdf)

Crop type	C-factor
Common wheat and spelt	0.2
Durum wheat	0.2
Rye	0.2
Barley	0.21
Grain maize – corn	0.38
Rice	0.15
Dried pulses (legumes) and protein crop	0.32
Potatoes	0.34
Sugar beet	0.34
Oilseeds	0.28
Rape and turnip rape	0.3
Sunflower seed	0.32
Linseed	0.25
Soya	0.28
Cotton seed	0.5
Tobacco	0.49
Fallow land	0.5

Table A1: USLE cover factors for typical European crops (Panagos et al., 2015)

Group	Detailed class	Description	C-factor	UK mean
Permanent crops	Vineyards Fruit trees & berry plantations	Vineyards Fruit trees or shrubs: single/mixed fruit species, fruit trees with permanently grassed surfaces	0.15–0.45 0.1–0.3	
	Olive groves	Olive trees	0.1–0.3	
Pastures	Pastures	Dense graminoid grass cover of floral composition, not under a rotation system. Mainly used for grazing.	0.05–0.15	0.0867
Heterogeneous agricultural areas	Annual crops associated with permanent crops	Non-permanent crops (arable land or pasture) associated with permanent crops (<25% non-associated crops)	0.07–0.35	
	Complex cultivation patterns	Small parcels of annual crops, pasture and/or permanent crops (each occupy less than 75% of the total area)	0.07–0.2	0.1201
	Principally agriculture, significant areas of natural vegetation	Principally agricultural, with natural areas (agricultural land occupies 25 to 75% of the area)	0.05–0.2	0.1068
	Agro-forestry	Annual crops or grazing land under forested cover	0.03–0.13	
Forests	Broad-leaved, coniferous and mixed forest	Principally trees including shrub and bush understories	0.0001–0.003	0.0011
Scrub and/or herbaceous vegetation	Natural grasslands	Low productivity grassland, often on rough and uneven ground	0.01–0.08	0.0319
	Moors and heathland	Low and closed cover dominated by bushes, shrubs and herbaceous plants	0.01–0.1	
	Sclerophyllous vegetation	Bushy sclerophyllous vegetation, including maquis (dense, shrubby) and garrige	0.01–0.1	
	Transitional woodland-shrub	Bushy or herbaceous vegetation with scattered trees	0.003–0.05	0.0183
Open spaces with little or no vegetation	Beaches, dune, sands	Beaches, dunes and expanses of sand/pebbles. Coastal or continental	0	
	Bare rocks	Scree, cliffs, rocks and outcrops	0	
	Sparsely vegetated areas	Includes steppes, tundra, badlands. Scattered high-altitude vegetation	0.1–0.45	0.1825
	Burnt areas	Areas affected by recent fires, still mainly black	0.1–0.55	
	Glaciers and perpetual snow	Land covered by glaciers or permanent snowfields	0	

Table A2: USLE cover factors collated for European land cover classes (Panagos et al., 2015)