

Observation impact, domain length and parameter estimation in data assimilation for flood forecasting

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1 **Observation impact, domain length and parameter estimation in data** 2 **assimilation for flood forecasting.**

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7 **Abstract**

8 Accurate inundation forecasting provides vital information about the behaviour of fluvial flood water.
9 Using data assimilation with an Ensemble Transform Kalman Filter we combine forecasts from a numerical
10 hydrodynamic model with synthetic observations of water levels. We show that reinitialising the model
11 with corrected water levels can cause an initialization shock and demonstrate a simple novel solution. In
12 agreement with others, we find that although assimilation can accurately correct water levels at observation
13 times, the corrected forecast quickly relaxes to the open loop forecast. Our new work shows that the time
14 taken for the forecast to relax to the open loop case depends on domain length; observation impact is longer-
15 lived in a longer domain. We demonstrate that jointly correcting the channel friction parameter as well as
16 water levels greatly improves the forecast. We also show that updating the value of the channel friction
17 parameter can compensate for bias in inflow.

18 **Keywords** Data assimilation, inundation forecasting, fluvial flooding, observation impact, joint state-parameter
19 estimation, ensemble Kalman filter.

20 **Highlights**

- 21 • Data assimilation is applied to simulated flood forecasts and SAR-like observations
- 22 • Reinitialisation shock due to water level correction is removed using a novel method
- 23 • Observation impact is linked to domain length when updating only water levels
- 24 • Updating the channel friction parameter leads to marked improvement in forecast skill
- 25 • Updating the channel friction parameter can compensate for biased inflow

26 **Software Availability**

27 The inundation simulations in this work were generated using Clawpack 5.2.2, a collection of FORTRAN and
28 python code available from <http://www.clawpack.org/>. Details of the amended Clawpack source code as used
29 in this work are freely available on request from the corresponding author, as is the python code used to perform
30 data assimilation on the inundation simulation output. Please contact e.s.cooper@pgr.reading.ac.uk for details.

31 1 Introduction

32 Data assimilation can improve the accuracy of predictions from flood inundation models by combining forecasts
33 from the model with observations of the system, taking into account uncertainty in both the model predictions
34 and the observations. In this study we use a sequential data assimilation method comprising a forecast-update
35 dynamic feedback loop. During each forecast step, the numerical model runs an inundation simulation. When
36 an observation (or set of observations) is available the simulation is interrupted and the update step is performed;
37 updating combines observational data and model predictions to give a better estimate of the state. The next
38 forecast step then starts, with the adjusted water levels as the initial condition. An update is carried out each
39 time a new observation or set of observations is available.

40 There are a number of numerical inundation models that can predict the behaviour of flood water given
41 information about the topography of the domain and the amount of water flowing into the area, e.g. HEC-
42 RAS, Telemac, LISFLOOD-FP (HEC-RAS Development Team; Hervouet, 2000; Neal et al., 2012). In a real
43 flood situation, topographical information is often available in the form of a digital terrain model (DTM) and
44 inflow estimates may come from an upstream gauge, or as output from a hydrological model. Observations
45 of the flood may be available from a variety of different sources. These include river depth and flow rate
46 measurements from gauges, and authors have used these data in assimilation schemes, e.g. Mure-Ravaud et al.
47 (2016). However, many catchments are ungauged and the number of gauges worldwide is in decline (Vrsmarty
48 et al., 2001). Observations of flood extent can be obtained from aerial photos, although the cloudy conditions
49 associated with heavy rainfall often limit the usefulness of this information source. Recently, much attention
50 has been paid to the use of synthetic aperture radar (SAR) satellite images in delineating flood extent, since
51 such observing systems have all weather and day and night capability. Water depth information can then be
52 retrieved from SAR satellite images using a high quality digital terrain model (DTM) as described in Mason
53 et al. (2012) and Brown et al. (2016). Such techniques for extracting information from SAR images are well
54 established, e.g. Thornhill et al. (2012), Mason et al. (2010), Scott et al. (2008) and Scott and Mason (2007).

55 Various authors e.g. Lai and Monnier (2009), Matgen et al. (2007) and Schumann et al. (2009) have
56 used data assimilation techniques to highlight the fact that although observations from SAR can cover a large
57 spatial area, the usefulness of the information they contain is limited in time. Assimilating data from one or
58 more river gauges can help to mitigate this, as shown by Lai and Monnier (2009) and Hostache et al. (2010),
59 but we consider here the situation in which only time-sparse satellite derived water level data is available for
60 assimilation. This leads to a situation in which data assimilation can provide a good analysis - i.e. can correct
61 water levels very well at the time of observations, but the model forecast then moves quickly away from the
62 true water levels during the subsequent forecast step. This short lived improvement in the water levels has been
63 shown in studies such as Andreadis et al. (2007), Neal et al. (2009) and Garcia-Pintado et al. (2013), which use
64 ensemble Kalman Filter data assimilation algorithms, as well as in Matgen et al. (2010), where a particle filter
65 approach is taken. This result indicates that water levels in a river flood situation are not strongly sensitive to

66 initial conditions. In fact, water levels are likely to be more dependent on inflow and model parameter values,
67 and updating one or a combination of these is therefore necessary.

68 In order to address the short-lived nature of the forecast improvement, authors such as Andreadis et al.
69 (2007), Matgen et al. (2010), Giustarini et al. (2011), Garcia-Pintado et al. (2015), Garcia-Pintado et al. (2013)
70 and Mason et al. (2015) have carried out data assimilation including on-line correction of inflow along with
71 water levels. Inflow correction is shown in all of these studies to give much better forecast accuracy over time
72 than correcting water levels alone. Less attention has been paid to the effect of errors in model parameters
73 in sequential data assimilation, despite the fact that several studies, including Andreadis and Schumann (2014)
74 and the comprehensive review paper by Grimaldi et al. (2016), indicate that model parameters are likely to have
75 an important influence on the behaviour of the flow.

76 One study in which parameter effects are investigated is Garcia-Pintado et al. (2015), in which water levels,
77 inflows and several model parameter values were updated simultaneously using an ensemble Kalman filter tech-
78 nique. The study used LISFLOOD-FP to model the flooding of the river Severn and tributaries near Tewksbury,
79 UK, in 2014, assimilating real SAR-derived water level observations. A large improvement in forecast skill was
80 seen when inflow was corrected along with water levels, leading to good agreement between the forecast and
81 independently measured gauge data. In this case, channel friction parameter estimation alongside estimation of
82 water levels, inflows and other parameters was not found to improve the forecast significantly, despite the fact
83 that water behaviour is strongly influenced by this parameter. The question of whether the retrieved friction
84 parameter value was correct was left open as the true value for the system was not known.

85 In this study we address open questions about the role of the channel friction parameter in data assimilation
86 for inundation modelling. We use a similar data assimilation technique to that in Garcia-Pintado et al. (2015)
87 in twin experiments with an idealised topography and an unbiased inflow. This allows us to separate out and
88 further investigate the effect of channel friction retrieval on the forecast. We find that, in contrast with Garcia-
89 Pintado et al. (2015), online estimation of the channel friction parameter along with water levels leads to a
90 large improvement in the forecast skill in our experiments. The twin experiments also show that our data
91 assimilation method is capable of finding an accurate value for the channel friction parameter, even when water
92 depth observations are only available on the flood plain during a flood.

93 We also investigate the effect of domain length on forecast skill, showing that because the assimilation
94 is able to correct water levels in areas where there are no observations, the time taken for corrected water
95 levels to decay back to the open loop (no assimilation) case is longer for a physically longer domain. Further,
96 we demonstrate that when reinitialising the numerical model after an assimilation, an initialisation shock can
97 occur. We demonstrate an efficient and effective technique for removing this shock, leading to more accurate
98 forecasts in the hours immediately following an assimilation.

99 This paper is organised as follows: In section 2 the numerical inundation model is described, the data
100 assimilation method is outlined and our novel re-initialisation method is demonstrated. In section 3 the exper-
101 imental configurations for various simulations are described. Section 4 shows the effect of including online

102 channel friction parameter estimation along with water level estimation, and compares results from different
 103 length domains. Section 5 draws conclusions about the effects of domain length and channel friction parameter
 104 estimation.

105 2 Methodology

106 In this section we describe the methods used in this study. In section 2.1 the numerical inundation model is
 107 outlined. Section 2.2 contains information about the data assimilation method used. In section 2.3 we discuss
 108 the impact of assuming the water has only hydrostatic momentum at the start of a forecast step and describe
 109 our approach to dealing with problems caused by this assumption.

110 2.1 Numerical inundation model

111 In this study we use a numerical flood model we have developed using Clawpack (Clawpack Development
 112 Team, 2014; Mandli et al., 2016; LeVeque, 2002), an open source collection of FORTRAN and python code
 113 that can be used to solve a wide variety of conservation laws. Clawpack uses finite volume methods and
 114 sophisticated Riemann solvers to treat systems of partial differential equations; in this work the equations of
 115 interest are the 2D shallow water equations that describe how river and flood water will move in space and
 116 time. The model splits the domain of interest into N cells and calculates the water depth in each cell. The code
 117 is capable of dealing with shocks in the solution, such as bores that may occur following a sudden increase of
 118 inflow into a particular river stretch. Clawpack deals effectively with the wet-dry interfaces which are present
 119 in an inundation event, and preserves depth non-negativity (George, 2008).

120 The shallow water equations for two spatial dimensions, x and y , can be written as (e.g. LeVeque (2002))

$$\frac{\partial \mathbf{q}}{\partial t} + \frac{\partial \mathbf{F}(\mathbf{q})}{\partial x} + \frac{\partial \mathbf{G}(\mathbf{q})}{\partial y} = \mathbf{R}(\mathbf{q}), \quad (1)$$

121 where $\mathbf{R}(\mathbf{q})$ is a source term and \mathbf{q} is a vector of conserved quantities

$$\mathbf{q} = \begin{bmatrix} h \\ hu \\ hv \end{bmatrix}, \quad (2)$$

122 h represents depth of the fluid, and u and v represent velocity in the x and y directions respectively.

In equation (1), $\mathbf{F}(\mathbf{q})$ and $\mathbf{G}(\mathbf{q})$ represent fluxes of the conserved quantities in the x and y directions respectively. For the shallow water equations these are

$$\mathbf{F}(\mathbf{q}) = \begin{bmatrix} hu \\ hu^2 + \frac{1}{2}gh^2 \\ huv \end{bmatrix} \quad \text{and} \quad \mathbf{G}(\mathbf{q}) = \begin{bmatrix} hv \\ huv \\ hv^2 + \frac{1}{2}gh^2 \end{bmatrix}, \quad (3)$$

123 where g is acceleration due to gravity.

124 The effect of friction is modelled as a source term in Clawpack, since the friction force acts to reduce the
 125 momentum of the water. The magnitude of the momentum reduction is strongly dependent on a Manning’s
 126 friction coefficient, n , and the flow of water is very sensitive to the value of this parameter. We have also added
 127 an inflow source term to the Clawpack code to model water arriving in the river stretch of interest, as further
 128 described in Appendix A and Cooper et al. (2013). The time step for the hydrodynamic model is variable, and
 129 automatically adjusted in the code to preserve numerical stability.

130 Correct specification of the solution at the boundaries of the computational domain is vital for the stability
 131 of any numerical scheme. To achieve this, Clawpack adds a user-specified number of ‘ghost’ cells (2 by
 132 default) next to each cell at a domain boundary. The domain is effectively extended in all directions by the
 133 addition of these ghost cells and the behaviour of the solution at the boundaries then depends strongly on the
 134 values of calculated model quantities in the ghost cells. We use non-reflecting outflow (extrapolating) boundary
 135 conditions in which values of \mathbf{q} are extrapolated from the cell next to the boundary into the ghost cells at each
 136 time step. This is called a zero order extrapolation in LeVeque (2002).

137 Another important factor is the representation of the domain topography at and across the domain bound-
 138 aries. The default in the code is to copy the value of the domain elevation at the boundary into the ghost cells.
 139 This represents a situation where there is no slope in bathymetry or topography across any boundaries. This
 140 is not suitable for the downstream boundary in our experiments, at which the majority of the water leaves the
 141 domain. A more physically realistic situation for the downstream boundary is to extrapolate the slope of the
 142 domain into the ghost cells at the boundary and changes have been made to the code to accommodate this.

143 **2.2 Data assimilation**

144 **2.2.1 State estimation**

145 In data assimilation, a state vector is used to represent the state of a physical system. In this work the state vector,
 146 $\mathbf{x} \in \mathbb{R}^N$, comprises water depths in each of N computational cells. Sequential data assimilation algorithms
 147 comprise two steps: a forecast (or prediction) step and an update (or analysis) step. In the prediction step, an
 148 estimate of the state, \mathbf{x} is evolved forward in time using the forecast model

$$\mathbf{x}(t_{k+1}) = \mathfrak{M}(\mathbf{x}(t_k)), \quad (4)$$

149 where \mathfrak{M} is the forecast model, in this case the non-linear numerical shallow water equation model described
 150 in section 2.1. In the update step the forecast is updated to take account of observations of the state. We assume
 151 that the observations can be described by

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \epsilon, \quad (5)$$

152 where $\mathbf{y} \in \mathbb{R}^p$ is a vector of observations and \mathbf{x} is the true state of the system. Since the observations may be
 153 indirect and not located at model cell centres, an observation operator, $\mathbf{H} : \mathbb{R}^N \rightarrow \mathbb{R}^p$ is required, which maps
 154 the state vector into observation space. For this work, \mathbf{H} is assumed to be a linear operator. The observation

155 noise, ϵ is assumed to be unbiased stochastic noise with covariance $\mathbf{R} \in \mathbb{R}^{p \times p}$. The ensemble Kalman filter
 156 used here is based on the Kalman filter. In the Kalman filter, whenever observations are available the state and
 157 error covariance matrix are updated Kalman (1960) according to

$$\mathbf{x}^a = \mathbf{x}^f + \mathbf{K}(\mathbf{y}_{obs} - \mathbf{H}\mathbf{x}^f) \quad (6)$$

158 and

$$\mathbf{P}^a = (\mathbf{I} - \mathbf{K}\mathbf{H})\mathbf{P}^f, \quad (7)$$

159 where forecast and analysis quantities are denoted by f and a superscripts respectively, $\mathbf{I} \in \mathbb{R}^{N \times N}$ is the
 160 identity matrix and $\mathbf{P} \in \mathbb{R}^{N \times N}$ is the state error covariance matrix. The matrix $\mathbf{K} \in \mathbb{R}^{N \times p}$ is the Kalman gain,
 161 given by

$$\mathbf{K} = \mathbf{P}^f \mathbf{H}^T (\mathbf{H}\mathbf{P}^f \mathbf{H}^T + \mathbf{R})^{-1}, \quad (8)$$

162 and $\mathbf{R} \in \mathbb{R}^{p \times p}$ is the observation error covariance matrix.

163 In the ensemble Kalman filter (Evensen, 1994), an ensemble of state vectors is used to represent a statistical
 164 sample of the forecast or analysis uncertainty. Each ensemble member represents one possible realisation of
 165 the true state of the system, given uncertainties in initial conditions and/or model parameters. For an ensemble
 166 comprising M state vectors, \mathbf{x}_i , ($i = 1, 2, \dots, M$), a mean state at any time can be defined as

$$\bar{\mathbf{x}} = \frac{1}{M} \sum_{i=1}^M \mathbf{x}_i. \quad (9)$$

167 The mean of the ensemble, $\bar{\mathbf{x}}$, represents an estimate of the true state of the system.

168 For any ensemble, an ensemble perturbation matrix $\mathbf{X} \in \mathbb{R}^{N \times M}$ can be defined as

$$\mathbf{X} = \frac{1}{\sqrt{M-1}} (\mathbf{x}_1 - \bar{\mathbf{x}} \quad \mathbf{x}_2 - \bar{\mathbf{x}} \quad \dots \quad \mathbf{x}_M - \bar{\mathbf{x}}). \quad (10)$$

169 The ensemble error covariance matrix, $\mathbf{P} \in \mathbb{R}^{N \times N}$ can then be calculated from

$$\mathbf{P} = \mathbf{X}(\mathbf{X})^T. \quad (11)$$

170 The forecast step for an ensemble system requires each state vector in the ensemble to be evolved by the
 171 forecast model according to equation (4). In the update step the forecast ensemble is combined with observa-
 172 tions of the state to produce a ‘corrected’ ensemble of state vectors called the analysis ensemble. The analysis
 173 ensemble is then used as a set of initial conditions for the next forecast step. This forecast-update cycle can be
 174 repeated many times and an analysis ensemble calculated whenever observations of the system are available.
 175 The ensemble update equations separately update the ensemble mean and the ensemble perturbations according
 176 to

$$\bar{\mathbf{x}}^a = \bar{\mathbf{x}}^f + \mathbf{K}(\mathbf{y} - \mathbf{H}\bar{\mathbf{x}}^f) \quad (12)$$

177 and

$$\mathbf{X}^a = \mathbf{X}^f \mathbf{T}. \quad (13)$$

178 The vector $\overline{\mathbf{x}}^a$ is the analysis state (the mean of the analysis ensemble), $\overline{\mathbf{x}}^f$ is the mean of the forecast ensemble
 179 and $\mathbf{K} \in \mathbb{R}^{N \times p}$ is an ensemble version of the Kalman gain (as shown in equation (16)). The matrix $\mathbf{T} \in \mathbb{R}^{M \times M}$
 180 updates the perturbations such that the state error covariance calculated by using \mathbf{X}^a in equation (11) matches
 181 that given by the Kalman covariance update, equation (7) (Kalman, 1960). There is not a unique solution
 182 for \mathbf{T} ; here we use an unbiased, symmetric square root formulation known as an ensemble transform Kalman
 183 Filter (ETKF), following the approach of Livings et al. (2008), Livings (2005) and Garcia-Pintado et al. (2013).
 184 In this approach we define a forecast observation ensemble comprising M forecast observation vectors, \mathbf{y}_i^f ,
 185 ($i = 1, 2, \dots, M$) such that

$$\mathbf{y}_i^f = \mathbf{H}(\mathbf{x}_i^f). \quad (14)$$

186 The forecast observation ensemble has a mean, and a perturbation matrix \mathbf{Y}^f , defined in the same way as for
 187 the state ensemble matrix.

188 We define a matrix \mathbf{D} as

$$\mathbf{D} = \mathbf{Y}^f (\mathbf{Y}^f)^T + \mathbf{R}; \quad (15)$$

189 the Kalman gain \mathbf{K} can then be written in terms of the forecast perturbation matrices \mathbf{X}^f and \mathbf{Y}^f ,

$$\mathbf{K} = \mathbf{X}^f (\mathbf{Y}^f)^T \mathbf{D}^{-1}. \quad (16)$$

190 Substituting equation (16) for \mathbf{K} on the right hand side of equation (7), and using equations (13) and (11) on
 191 the left hand side shows that the matrix \mathbf{T} in equation (13) then needs to satisfy

$$\mathbf{T}(\mathbf{T})^T = \mathbf{I} - (\mathbf{Y}^f)^T \mathbf{D}^{-1} (\mathbf{Y}^f). \quad (17)$$

192 Using the Sherman-Woodbury-Morisson identity for the right hand side of equation (17), as in equation (15) of
 193 Tippett et al. (2003), this becomes

$$\mathbf{T}(\mathbf{T})^T = (\mathbf{I} + (\mathbf{Y}^f)^T \mathbf{R}^{-1} \mathbf{Y}^f)^{-1}. \quad (18)$$

194 A scaled forecast observation ensemble perturbation matrix can then be introduced,

$$\widehat{\mathbf{Y}}^f = \mathbf{R}^{-\frac{1}{2}} \mathbf{Y}^f. \quad (19)$$

195 Performing a singular value decomposition (Golub and Van Loan, 1996) of $(\widehat{\mathbf{Y}}^f)^T$ gives a factorisation such
 196 that

$$(\widehat{\mathbf{Y}}^f)^T = \mathbf{U} \Sigma \mathbf{V}^T, \quad (20)$$

197 where \mathbf{U} and \mathbf{V} are orthogonal matrices with dimensions $(M$ by $M)$ and $(p$ by $p)$ respectively. The columns of
 198 \mathbf{U} and \mathbf{V} are the left and right singular vectors of $(\widehat{\mathbf{Y}}^f)^T$ respectively, and the diagonal elements of the $(M$ by
 199 $p)$ matrix Σ are the singular values of $(\widehat{\mathbf{Y}}^f)^T$. Combining equations (18), (19) and (20) gives

$$\mathbf{T}(\mathbf{T})^T = \mathbf{U} (\mathbf{I} + \Sigma \Sigma^T)^{-1} \mathbf{U}^T, \quad (21)$$

200 and a solution for \mathbf{T} is therefore

$$\mathbf{T} = \mathbf{U}(\mathbf{I} + \Sigma\Sigma^T)^{-\frac{1}{2}}\mathbf{U}^T. \quad (22)$$

201 This is the solution used in this work.

202 2.2.2 Joint state-parameter estimation

203 Section 2.2.1 describes how the ETKF can be used to update the water levels in a computational domain, given
 204 observational data. It is also possible to update values of uncertain forecast model parameters as part of the
 205 same process. This is achieved by state augmentation, in which parameters are appended to the state vector
 206 (Smith et al., 2013; Navon, 1998; Evensen et al., 1998; Smith et al., 2009, 2011). The augmented state vector,
 207 \mathbf{x}_{aug} , is then given by

$$\mathbf{x}_{aug} = \begin{bmatrix} \mathbf{x} \\ \mathbf{b} \end{bmatrix}, \quad (23)$$

208 where $\mathbf{b} \in \mathbb{R}^m$ is a vector of m parameters and $\mathbf{x}_{aug} \in \mathbb{R}^{N+m}$. In this work, we are interested in updating just
 209 one parameter, the Manning’s friction coefficient in the river channel, n_{ch} . This means that \mathbf{b} is scalar in this
 210 case.

211 We assume that the value of n_{ch} does not change with time over the course of a particular flood. This means
 212 that the value of n_{ch} is constant during the forecast step and only updates at assimilation times. The forecast
 213 equation for the augmented state vector is then given by

$$\mathbf{x}_{aug}(t_{k+1}) = \begin{bmatrix} \mathfrak{M}(\mathbf{x}(t_k)) \\ \mathbf{b}(t_k) \end{bmatrix}, \quad (24)$$

214 where \mathfrak{M} is the forecast model as in equation (4).

215 The ETKF update equations (12) and (13) can be applied to the augmented state vector in the same way
 216 as described in section 2.2.1. The ensemble assimilation scheme then takes into account covariances between
 217 errors in the state vectors and the parameter(s). These covariances act to correct the parameter value according
 218 to information from observations as part of the same process that corrects water levels in the domain.

219 Estimating parameter values in this way has a number of advantages over a more traditional offline cal-
 220 ibration approach. Firstly, the updating of the parameter values is performed with information from current
 221 observations. Calibrating parameters with data from previous events risks using out of date information which
 222 does not take into account changes to the river bed due to, for example, erosion or sediment transport. Calcu-
 223 lating parameters using data assimilation also allows the value to change on shorter timescales during a flood
 224 event as the value is assumed to be constant during forecast steps, but updates each time new observational
 225 information is available. Additionally, off-line calibration and tuning of parameters can be computationally
 226 costly and needs to be performed ahead of a flooding event which may occur with little warning.

227 In our synthetic experiments we have assumed that the channel friction parameter, n_{ch} is the same value
 228 for the whole channel. In a real setting, it would be necessary to take an approach like that in Garcia-Pintado

229 et al. (2015), where different values of n_{ch} were assumed for different types of channel such as large rivers and
 230 small streams.

231 **2.3 Hydrostatic initialisation shock**

232 The ETKF is a sequential method and this means that each time observations are available an assimilation can
 233 be carried out. In order to perform an assimilation, the forecast model is interrupted. The ensemble states (water
 234 levels) are updated by the ETKF and each ensemble member then restarts running in Clawpack, reinitialised
 235 with the new water levels. In some approaches to data assimilation for inundation modelling, e.g. Lai and
 236 Monnier (2009); Hostache et al. (2010); Ricci et al. (2011), the state vector contains information about water
 237 flow or discharge rates as well as water levels. The flow rates are therefore updated along with water levels as
 238 part of the assimilation process. In contrast, in this study, as in Garcia-Pintado et al. (2015), the state vector
 239 contains only water depth information (plus parameters when considering the joint state-parameter estimation
 240 problem).

241 In Garcia-Pintado et al. (2015), a hydrostatic assumption was made for reinitialisation, i.e. the water was
 242 assumed to have zero momentum at each forecast restart time. The effect of this assumption in our domain can
 243 be seen by interrupting a simulation and restarting without performing any data assimilation, i.e. reinitialising
 244 with identical water levels as before, but with zero momentum everywhere. Comparing the root mean square
 245 error (RMSE) between the water depths predicted by a reinitialised version and continuous version of the
 246 simulation then gives a measure of how the hydrostatic assumption at restart affects the forecast. The RMSEs
 247 are measured over the whole domain and defined as

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (h_i^r - h_i^c)^2}, \quad (25)$$

248 where h_i^r is the forecast water depth after reinitilisation in the i th cell and h_i^c is forecast water depth in the
 249 same cell without reinitialisation. The number of cells in the domain is N , as before.

250 The open circles in figure 1 show RMSEs between the reinitialised forecast and the continuous forecast.
 251 Figure 1 shows that the consequence of using a hydrostatic assumption is that the error between the continuous
 252 and restarted cases is large at times less than approximately four hours in this system. This means that forecast-
 253 ing the behaviour of flood water at these times is problematic. The error becomes negligible by approximately
 254 four hours after the assimilation time.

255 In order to correct for this without adding flow information to the state vector, we assume that the water in
 256 each cell has the same velocity (u and v in the x and y directions respectively) after the assimilation as it did
 257 before the assimilation. This gives a state vector of lower dimension (approximately one third as many entries)
 258 than the approach of Lai and Monnier (2009), Hostache et al. (2010) and Ricci et al. (2011), thus reducing
 259 computational expense, while avoiding problems caused by assuming zero flow rates at the start of each forecast
 260 step as in Garcia-Pintado et al. (2015). Reinitialising with the same flow rate (hu and hv) values in each cell

261 would also be possible, but since the water levels will have changed in some cells due to the assimilation, this
262 is likely to lead to unrealistic behaviour. Reinitialising the water with the pre-analysis velocity values removes
263 the large shock shown in figure 1; the resulting RMSE values are shown in figure 1 with filled circles. The very
264 small RMSE values shown by the filled circles show that the method is effective in removing the initialisation
265 shock.

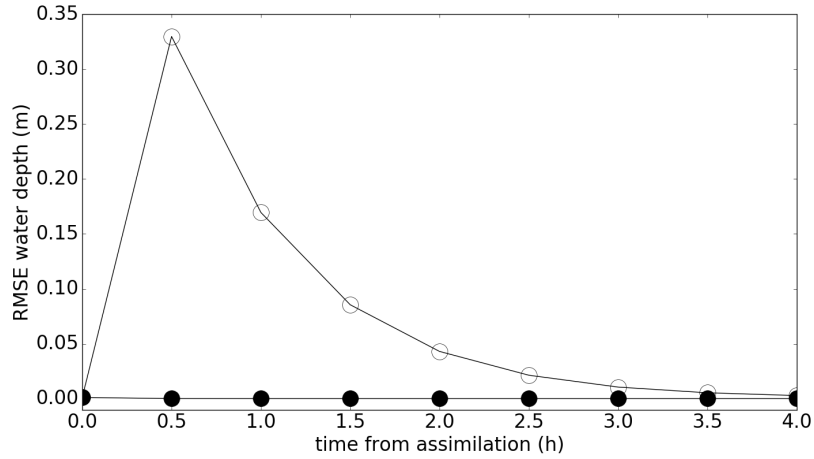


Figure 1: RMSE in water depth over the domain. Open circles show the RMSE between the continuous truth and restarted truth for a hydrostatic assumption. Filled circles show the RMSE when reinitialising with forecast velocities.

266 We performed a simple comparison of the values of hu and hv obtained using our approach ('simple
267 calculation value') with those calculated during an assimilation in which hu and hv were included in the state
268 vector ('analysis value'). We compared values at each assimilation time in an identical twin experiment in
269 which we update both the water levels and the channel friction parameter. Figure 2 shows some typical results
270 (from the assimilation at 28h in the SPL experiment as described in section 3.2).

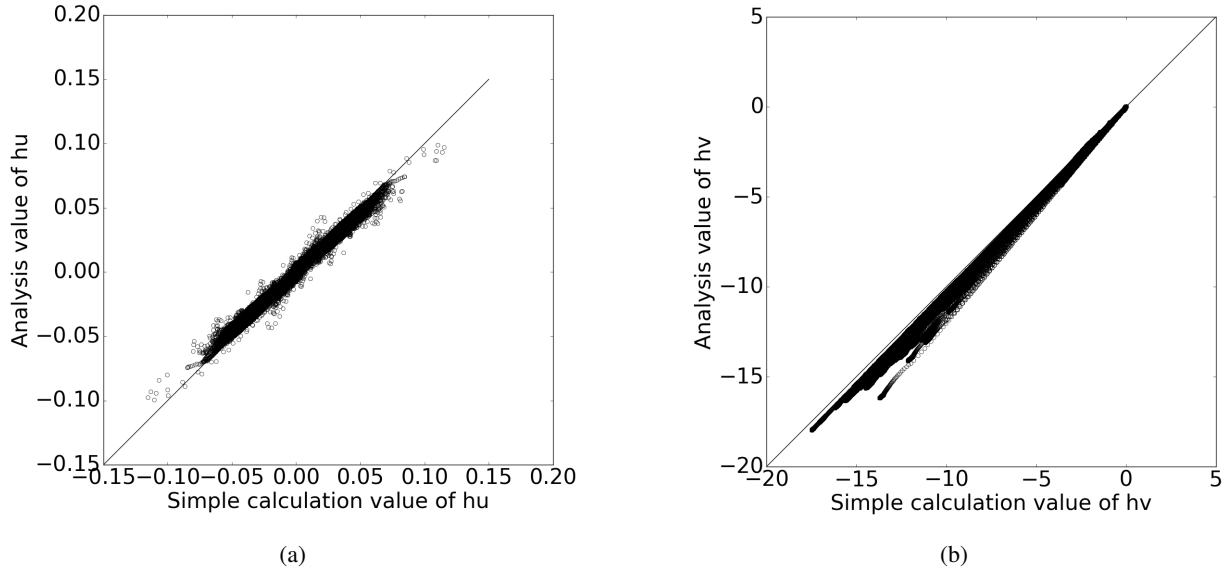


Figure 2: Comparison of (a) hu and (b) hv values at one assimilation time.

271 Figure 2a shows the values of hu obtained using the simple method described here plotted against the values
 272 of hu calculated by including hu and hv in the assimilation state vector; figure 2b shows the same results for
 273 values of hv . The values are close to the identity line and therefore in broad agreement. We found that the
 274 agreement between the methods was better at later assimilation times, when the forecast error is low. This is
 275 because both methods provide values close to the pre-assimilation (forecast) values when the adjustment by
 276 the assimilation is relatively small. The values of n_{ch} obtained when including hu and hv in the state vector
 277 were almost identical (less than 0.001% difference) to the values obtained when the state vector comprises only
 278 water levels. We observed no instabilities in the solution at initialisation times using our technique.

279 3 Experimental design

280 3.1 Model domain

281 All of the experiments referred to in this paper are carried out in domains with a simplified river valley-like
 282 topography. We use two domains in this work, the ‘long’ domain describes an area of 20 km by 250m and is
 283 shown in figure 3. Note that the axes are not to the same scale. The ‘regular’ domain is 5km by 250m, and
 284 is identical to the long domain for $15 \leq y \leq 20km$ and $0 \leq x \leq 250m$. The domains are gently sloping
 285 symmetrical valleys with a 50m wide central river channel as shown in figure 3. The grid cell size for the
 286 computation is 10m by 10m in all cases. The river channel is defined to be the central 5 grid cells in the x
 287 direction for all values of y ; the rest of the domain is defined as the flood plain. The cross section for both
 288 domains is the same. The domain has an upstream-downstream slope of 0.08% and the slope of the floodplain
 289 towards the river is 0.8%.

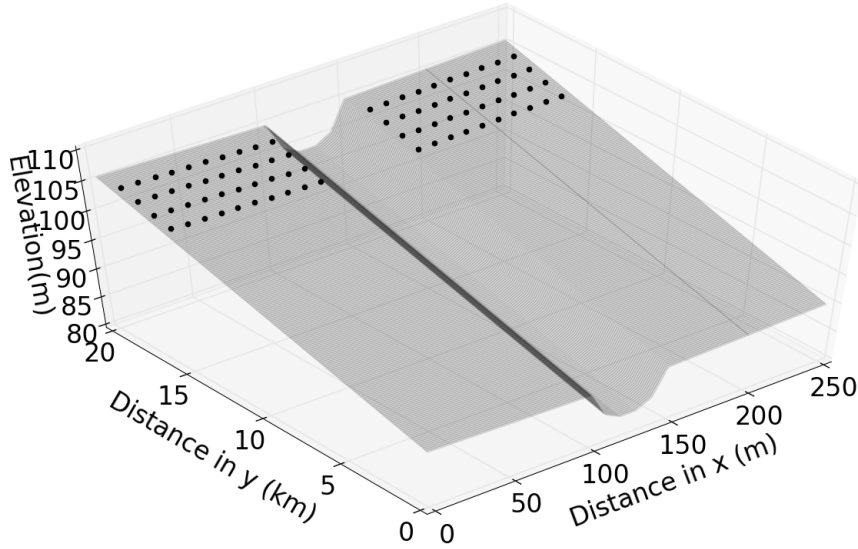


Figure 3: Elevation in metres of the long test domain used for the assimilation experiments. The regular domain is defined by $15 \leq y \leq 20\text{km}$ and $0 \leq x \leq 250\text{m}$. The black circles indicate the positions of water elevation observations used in the data assimilation.

290 3.1.1 Identical Twin Experiments

291 In this study, we use an ETKF in identical twin experiments. Identical twin experiments are commonly carried
 292 out in order to test a data assimilation system as well as to generate information about the model to which data
 293 assimilation is applied, e.g. Evensen (1994). In such experiments, a numerical model is used to generate a
 294 ‘truth’ output for a set of known initial conditions and model parameters. The truth run for these experiments
 295 is a continuous run of our inundation model for 112 hours using a time varying inflow shown by the solid black
 296 circles in figure 4. For the first four hours, the inflow is set to be constant in order to fill the river channel with
 297 water in a spin-up period. The inflow from $t = 4$ hours onwards is based on some real hydrograph data from a
 298 flood of the river Severn near Tewksbury in the summer of 2007. The inflow comprises hourly values and linear
 299 interpolation is used to give flow rates between the hourly points. The truth run uses a value for the channel
 300 Manning’s friction parameter of $n_{ch} = 0.04$, which is the value given for a natural stream by Maidment and
 301 Mays (1988). The Manning’s friction parameter on the flood plain, n_{fp} , is likely to be higher due to vegetation
 302 and here we use a value of $n_{fp} = 0.05$.

303 The inundation model is also used to generate a 100 member ensemble of flood realisations. This ensemble
 304 represents a forecast of the true flood given uncertainty in upstream inflow and the channel friction parameter
 305 values. The number of ensemble members is relatively small compared to the dimension of the state vector,
 306 which contains 125,000 water depths for the short domain and 500,000 for the long domain. However, none
 307 of the problems which indicate undersampling of a system (spurious correlations or ensemble collapse as out-

308 lined by Petrie and Dance (2010)) are seen, suggesting that this number of ensemble members is sufficient to
309 represent the system in this case. It was therefore not necessary to apply any localisation or inflation in these
310 experiments.

311 Each member of the ensemble is driven by a different inflow and has a different friction parameter. The
312 ensemble inflows are generated by adding time correlated random errors to the ‘true’ inflow; the ensemble
313 inflows and true inflow are shown in figure 4. The variance for the inflow distribution is a proportion of the
314 inflow, since the error in measured or predicted flow is likely to be flow-dependent as in Garcia-Pintado et al.
315 (2015). The standard deviation for the generated inflow distribution is $0.15 \times$ inflow, which is the same as the
316 value used by Garcia-Pintado et al. (2015) and fits within the range of errors in measured flow rates (4% to
317 43%) reported in Di Baldassarre and Montanari (2009). No bias was applied to the inflow ensemble so that the
318 mean inflow is very similar to the true inflow. An unbiased inflow removes the effect of an incorrectly specified
319 inflow, since this has already been studied elsewhere. Choosing to use an unbiased inflow allows the effect of
320 the incorrect channel friction parameter value to be studied in isolation; we briefly address the effect of biased
321 inflow at the end of section 4.2.

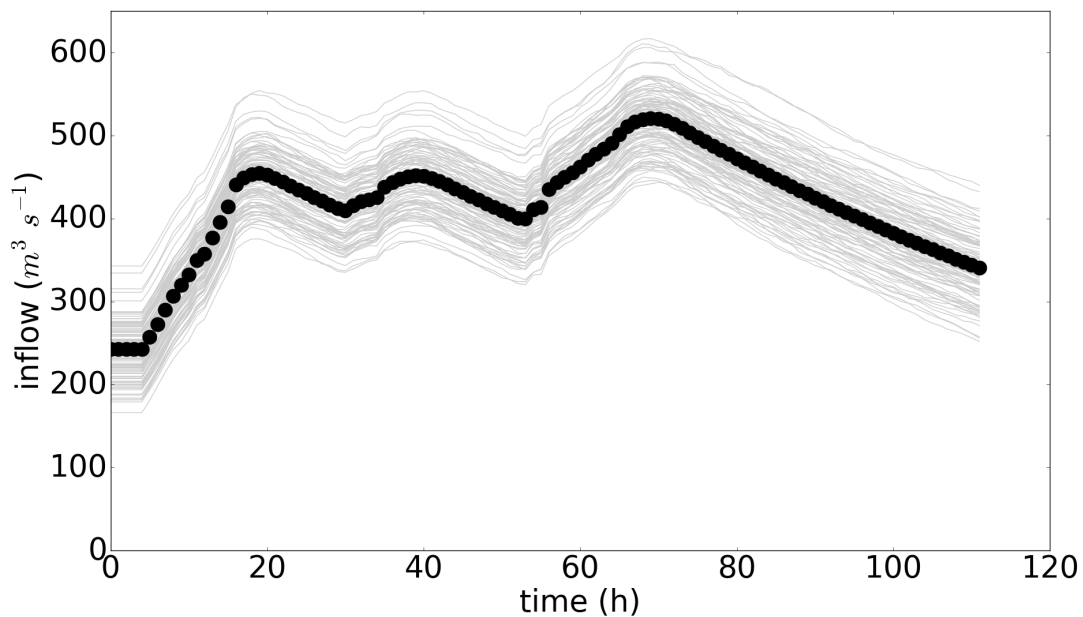


Figure 4: Inflow ensemble with time. Circles show the true inflow values and the grey lines show the ensemble inflows.

322 Ensemble channel friction parameters were generated by selecting from a Gaussian distribution centered on
323 a ‘wrong’ initial value to reflect the fact that this parameter varies between catchments and will not generally
324 be known before the start of a flood event. The channel friction parameter is also not likely to be directly
325 measurable as it relates to the specific way in which Clawpack models friction. Different numerical models
326 with different friction parameterisations have been shown to generate different optimal friction parameters
327 for the same data for this reason (Horritt and Bates, 2002). Centering the channel friction ensemble on an

328 incorrect value also enables us to test whether the data assimilation scheme can retrieve the correct value from
329 an incorrect starting point. The channel friction parameter for each ensemble member was selected from a
330 Gaussian distribution, $\mathcal{N}(0.05, 0.01)$. The true value of $n_{ch} = 0.04$ falls within one standard deviation of the
331 mean of this distribution. The value for the friction parameter on the flood plain was set to the true value for all
332 ensemble members, i.e. $n_{fp} = 0.05$.

333 Data assimilation using an ETKF is carried out on the forecast ensemble, using synthetic observations
334 generated from the truth as described in the next section. Since the ETKF is a sequential method the ensemble
335 is evolved forward in time with Clawpack between observation times, and an assimilation is carried out every
336 12 hours. We also consider the ‘open loop’ case in which a forecast ensemble runs with no assimilation.

337 **3.2 Experimental configurations**

338 Various data assimilation experiments are carried out, each for a total period of 112 hours, including a 4 hour
339 spin-up period with constant inflow to allow the river channel to fill up (as shown in figure 4). Synthetic
340 observations of water depth are taken from the truth at 12 hourly intervals and assimilated with an ETKF.
341 Twelve hourly assimilation intervals were chosen as this represents the smallest likely return time for SAR-
342 equipped satellites at present.

343 Since we are running identical twin experiments, we know the true water levels everywhere in the domain,
344 as well as the water levels forecast by the ensemble. It is theoretically possible to use SAR derived flood extent
345 observations along with a high quality digital terrain model (DTM) to derive water levels in all parts of a real
346 domain. One approach in a synthetic experiment is therefore to directly use water level observations in all parts
347 of the domain as a proxy for SAR derived information. Such an approach is used by, for example, Lai and
348 Monnier (2009). In reality, SAR images can reliably provide information about water elevation only at a few
349 points along the flood extent, as demonstrated in Mason et al. (2012).

350 In this paper, we do not use all the available water levels. Instead we use synthetic observations of water
351 levels taken directly from the truth run in the positions shown by black circles in figure 3. This approach
352 replicates a situation in which four reliable flood delineation positions are available from a SAR image at $y =$
353 16, 17, 18 and 19km. We assume that we have a SAR image covering the domain from $y = 15$ to 20km, and that
354 water elevation at each of the four flood edge positions can be obtained from a DTM; this water level can then
355 be extrapolated perpendicular to the channel to give water elevation in each floodplain cell in the cross sections
356 where we have delineation observations (i.e. $y = 16, 17, 18, 19$ km). Although extrapolating water elevation
357 across a cross section in this way would also give information about the water elevation in the channel, we
358 exclude observations in the channel in this experiment. This is because topography information in the channel
359 is likely to be much less accurate than that for the floodplain, making water depths less certain. Noise was
360 added to the synthetic observations to represent uncertainty due to instrument error, flood extent determination
361 and typical DTM errors. The noise added to the observations is Gaussian with a standard deviation of 0.25m;
362 this is the same value as used in experiments with real data in Garcia-Pintado et al. (2015).

363 We perform a series of experiments using both the regular and long domain. Further details of the individual
364 experiments are as follows:

- 365 • **Case SOR:** State-only estimation in the regular domain, with the ensemble of channel friction parameters
366 distributed about an incorrect ‘first guess’ as described in section 3.1.1.
- 367 • **Case SOL:** State-only estimation in the long domain; all other details as for case SOR.
- 368 • **Case SPR:** State and channel friction parameter estimation in the regular domain with the initial channel
369 friction parameter distributed about an incorrect ‘first guess’ as described in section 3.1.1 .
- 370 • **Case SPL:** State and channel friction parameter estimation in the long domain; all other details as for
371 case SPR.
- 372 • **Case OR:** Open loop ensemble forecast in the regular domain; this is a free running ensemble forecast
373 with the same initial conditions as cases SOR and SPR but without assimilation of observations.
- 374 • **Case OL:** Open loop ensemble forecast for the long domain.

375 The positions of the observations are the same for both the long and regular domains. This corresponds to
376 observations spread throughout the whole of the regular domain, and observations only in the upstream part of
377 the long domain. The observation errors are the same for the four different configurations that use observations.

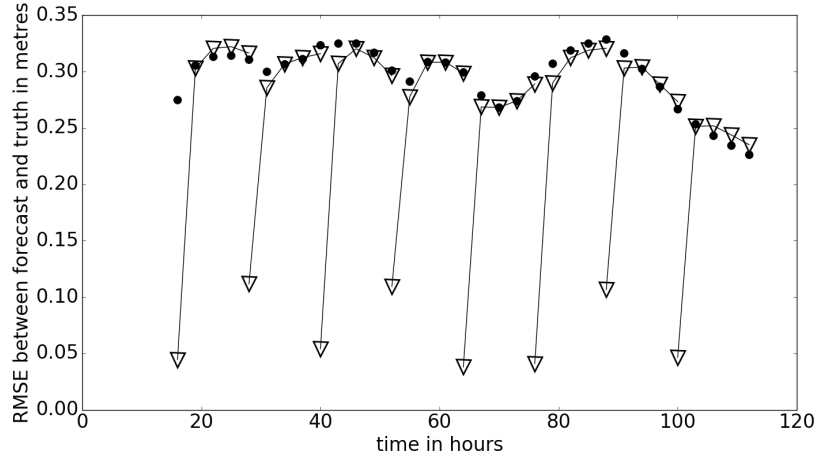
378 **4 Results and discussion of assimilation**

379 **4.1 State only estimation (SOR and SOL)**

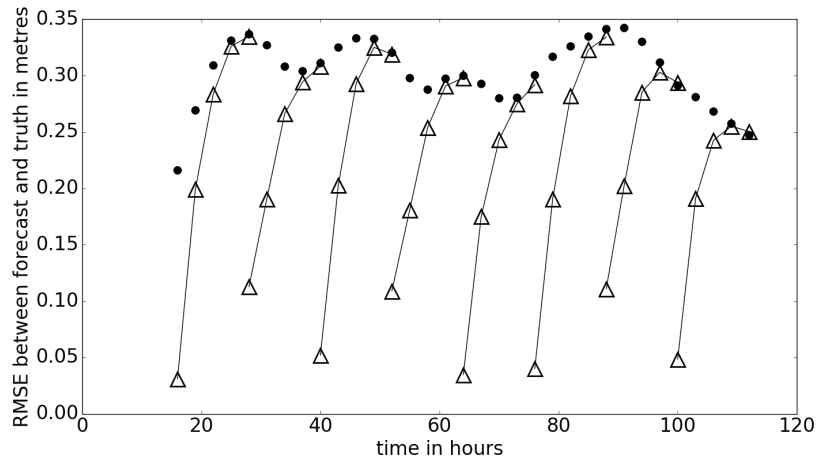
380 Results from state-only assimilation experiments are shown in figure 5. The graphs shows the RMSE over
381 the whole domain between the forecast ensemble mean water depths and the true water depths at three hourly
382 intervals from the time of the first assimilation at 16h. Here, RMSE is defined as

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (\overline{h_i^f} - h_i^t)^2}, \quad (26)$$

383 where $\overline{h_i^f}$ and h_i^t are the forecast ensemble mean and true water depth in cell i respectively. This definition
384 means that the error is averaged over a larger area for the longer domain than for the regular domain. The
385 values of RMSEs, though broadly similar, are therefore not directly comparable between domains.



(a) RMSE between the ensemble forecast mean and the true water depth $(\bar{x}^f - x^t)$ in the regular domain. Triangles show results for state only estimation (SOR), with assimilation carried out at $t=16h, 28h, 40h, 52h, 64h, 76h, 88h$ and $100h$. Circles show the open loop (OR) case for the regular domain (no assimilation).



(b) RMSE between the ensemble forecast mean and the true water depth $(\bar{x}^f - x^t)$ in the long domain. Triangles show results for state only estimation (SOL), with assimilation carried out at $t=16h, 28h, 40h, 52h, 64h, 76h, 88h$ and $100h$. Black circles show the open loop case (OL) for the long domain (no assimilation).

Figure 5: RMSEs for state-only estimation in the regular and long domains.

386 Figure 5a shows the RMSE between the forecast ensemble mean and true water depths with time for the
 387 regular domain (SOR). Figure 5b shows the same results for the longer domain (SOL). In both domains the
 388 ETKF produces a good analysis. The difference between the analysis ensemble mean water levels and the true
 389 water levels is very small at the time of each observation, and a large improvement is seen compared to the
 390 open loop forecast. However, for the regular domain in particular, the forecast skill is quickly lost during each
 391 subsequent forecast step and the RMSE quickly relaxes towards the open loop case. Comparing 5a and 5b
 392 shows that the RMSE at each analysis time is broadly similar for the two different domains. The results also

393 show that the forecast skill persists for longer in the long domain; the forecast takes longer to relax to the open
394 loop case in the longer domain than in the regular domain. This means that the same observations are having a
395 longer-lived impact on the forecast when a longer stretch of river and floodplain is considered.

396 In order to further understand why the observation impact is longer-lived in the long domain, the evolution
397 of the error during the forecast step can be investigated. Figure 6 shows the long domain in plan view with the
398 error between the forecast ensemble mean and the true water levels in each cell. The errors are shown at several
399 times during the forecast after assimilation at $t = 52\text{h}$ and before assimilation at $t = 64\text{h}$. In this particular
400 forecast period the inflow is increasing steadily, but similar patterns are seen for forecast periods in which the
401 inflow is varying in other ways.

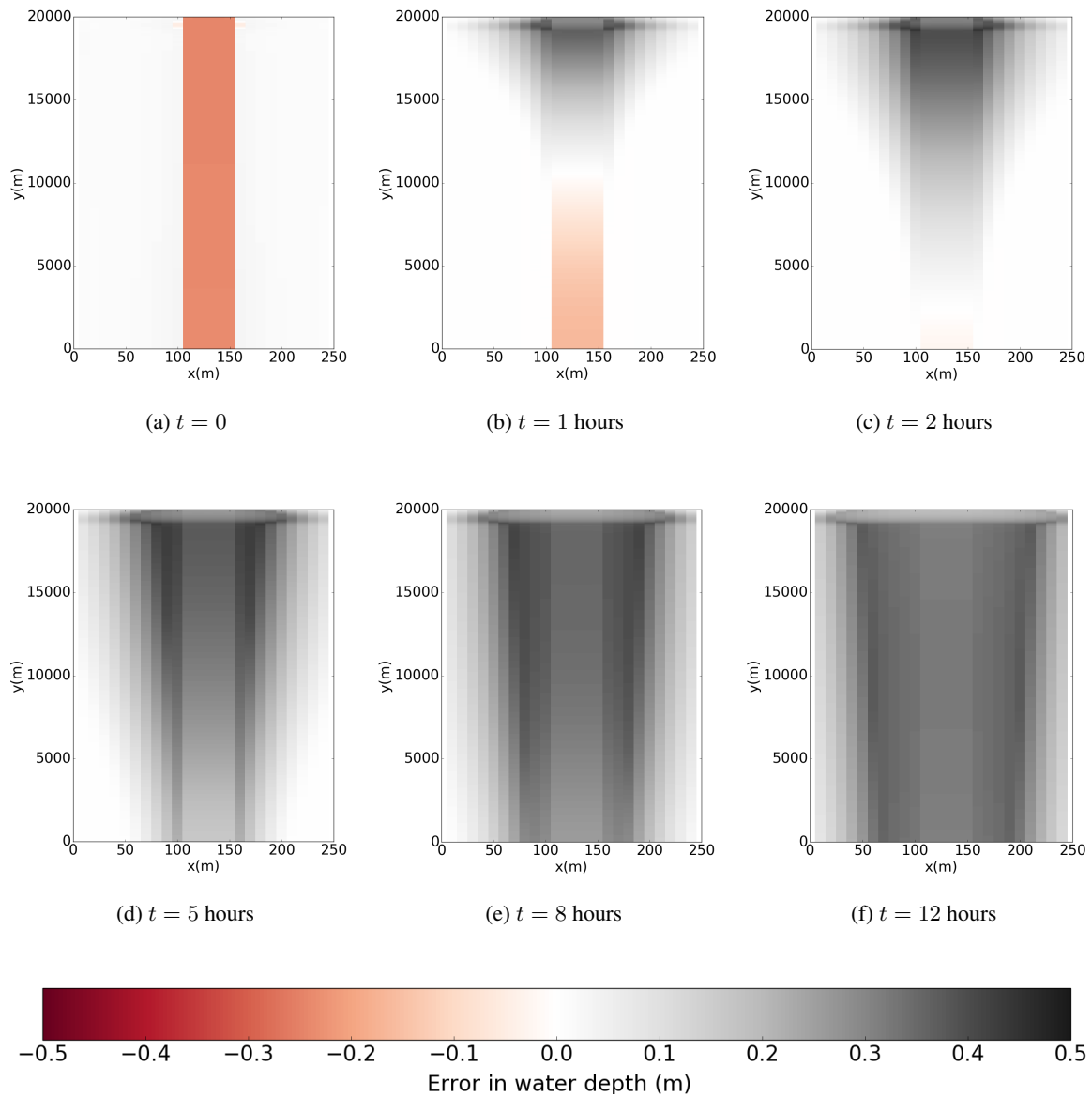


Figure 6: Forecast (ensemble mean) water depth minus true water depth in the long domain, shown in plan view for case SOL. Times are measured from assimilation at $t = 52$ h. For reference, the true water depth on the floodplain varied between 0 and 0.4m during this forecast period. Water depth in the centre of channel varied between 5.9m and 6.4m.

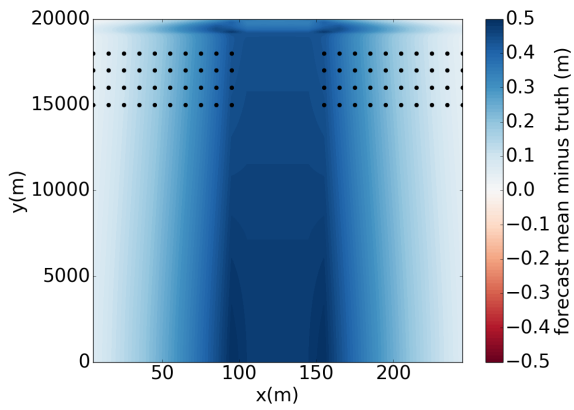
402 Figure 6a shows the difference between the forecast ensemble mean water depths and the true water depths
 403 at the observation/assimilation time. The error between the forecast ensemble mean and true water depths is
 404 small at all points in the domain at this time. The difference between the forecast ensemble mean and the truth
 405 is highest in the channel; this reflects the fact that there are no observations of channel water depth used in
 406 the assimilation. Figure 6b shows the error between the forecast ensemble mean and the truth 1 hour after the
 407 assimilation. The error at the downstream end of the domain remains small, while a large, positive error can
 408 be seen in the upstream part. A positive error here means that the forecast is overestimating the water depth.

409 In figure 6c, the errors at 2 hours after assimilation are shown. The physical area in which the forecast is
410 overestimating water depths has grown in the hour between 6b and 6c, and penetrated further downstream into
411 the domain. This pattern of error growth from upstream to downstream continues over time in figures 6d (5
412 hours after assimilation), 6e (8 hours after assimilation) and 6f (12 hours after assimilation).

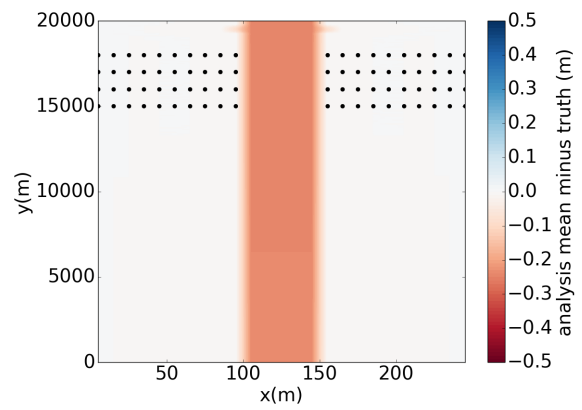
413 The observed pattern of error growth explains why the observations have impact in the longer domain for a
414 longer time. The regular domain is defined by $15 \leq y \leq 20\text{km}$ and $0 \leq x \leq 250\text{m}$ (as shown in figure 3). The
415 errors in water depth in this part of the long domain become very large within a few hours of the assimilation,
416 as can be seen in figure 6c. This means that the error in the whole of the regular domain becomes large very
417 quickly. In contrast, the RMSE for the long domain includes the downstream area where the water levels are
418 still corrected from the assimilation; the RMSE is therefore lower for a longer time as the error takes a longer
419 time to reach the downstream part of the longer domain.

420 During the forecast step, figure 6 shows that the error in the forecast resulting from incorrect specification
421 of the n_{ch} parameter starts at the upstream end of the domain, and propagates downstream with time. This
422 pattern of error growth is the same as that which would be expected from a bias in inflow, as noted in e.g.
423 Andreadis et al. (2007). A biased inflow acting on corrected water levels will clearly degrade the forecast water
424 levels close to the upstream boundary first and this error will propagate downstream with the flow. The results
425 shown in figure 6 therefore indicate that errors due to incorrect inflow specification and those due to incorrect
426 specification of the channel friction parameter may be difficult to separate out in a real flood event.

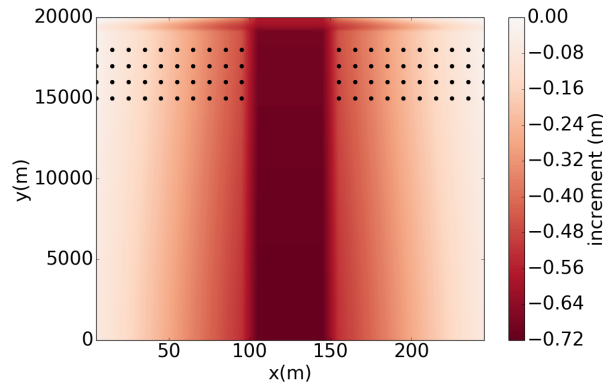
427 The low RMSEs between the analysis and the truth in the long domain highlight the fact that the ETKF is
428 able to correct the water levels in areas for which there are no observations. The state error covariance matrix
429 generated by the ensemble perturbations is such that information from the observations is spread throughout the
430 domain, enabling corrections to be made to the state at the downstream part of the domain when observations
431 are available only at the upstream end. This is further demonstrated in figure 7, which shows the difference
432 between the forecast ensemble mean and the truth pre-assimilation (figure 7a) and post-assimilation (figure 7b),
433 plotted in the long domain at $t = 52\text{h}$. Figure 7c shows the increments applied in the long domain as a result
434 of observations in the upstream part of the domain only. The figure clearly shows that adjustments are made to
435 water levels in the whole domain.



(a) Difference between the forecast ensemble mean and the truth ($\bar{\mathbf{x}}^f - \mathbf{x}^t$) plotted in the long domain (pre assimilation) at $t = 52$ hours.



(b) Difference between the analysis ensemble mean and the truth ($\bar{\mathbf{x}}^a - \mathbf{x}^t$) plotted in the domain (after assimilation) at $t = 52$ hours.



(c) Increments applied to the forecast ensemble mean for the assimilation at $t = 52$ hours

Figure 7: Difference between the forecast ensemble mean and the truth at $t = 52$ hours, (a) pre assimilation and (b) post assimilation; (c) shows the increment applied to the forecast to compute the analysis ($\bar{\mathbf{x}}^a - \bar{\mathbf{x}}^f$). In each plot the black circles show the position of the observations.

436 For a reliable ensemble, the RMSE should be close to the spread of the ensemble, where the spread is
 437 defined as the square root of the average ensemble variance (see e.g. Fortin et al. (2014)). Reliability plots (of
 438 RMSE vs. spread) should therefore produce points which lie close to the identity line. Such plots can be used
 439 to diagnose ensemble collapse, where the spread of an ensemble becomes unrealistically small.

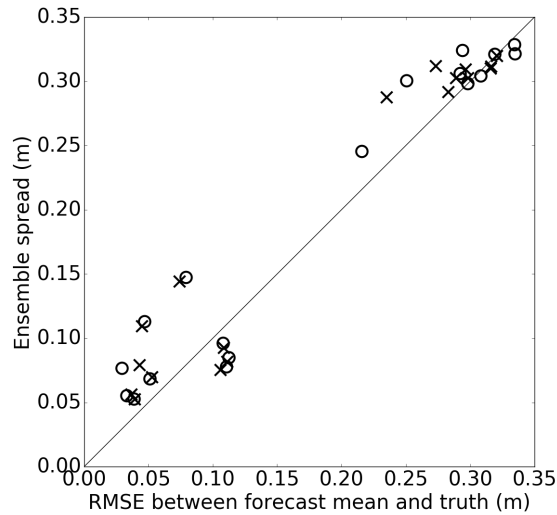


Figure 8: Reliability plot for the SOR and SOL experiments, showing forecast and analysis RMSE vs ensemble spread at each assimilation time. Circles are for the long domain, crosses for the regular domain. For an ideal ensemble, all points would lie on the identity line.

440 Figure 8 is a reliability plot for the SOR and SOL experiments. The points all lie close to the identity line,
 441 indicating that the ensemble spread is adequate to capture the uncertainty in the forecast. There is no indication
 442 of ensemble collapse. The points form two clusters, with large error, large spread values before an assimilation
 443 and low error, small spread values for analysis ensembles.

444 4.2 State and parameter estimation (SPR and SPL)

445 Considering a longer stretch of river in our idealised domain, as in section 4.1, shows an improvement in the
 446 forecast skill of the ETKF, in that the RMSE increases more slowly. By design, much of the error between the
 447 truth and the forecast comes from the incorrect channel friction parameter in these experiments. In this section
 448 we show results from using data assimilation to jointly estimate the state and the channel friction parameter in
 449 both domains.

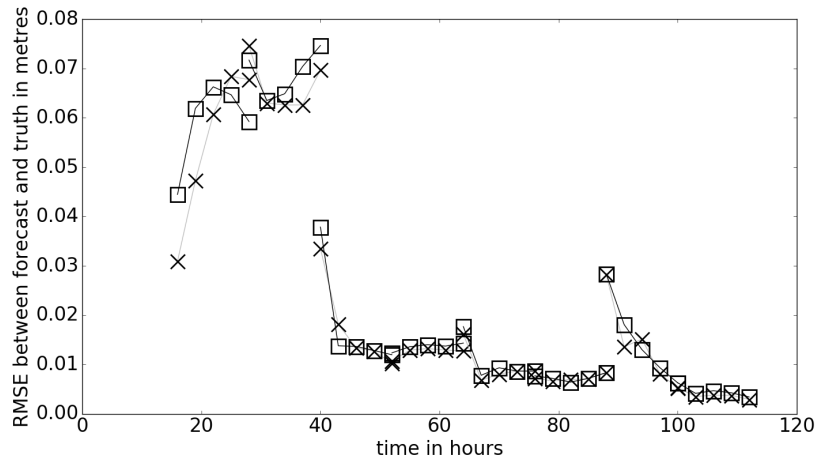


Figure 9: RMSE between the ensemble mean and the truth over the whole domain for joint state-parameter estimation; crosses denote RMSE for the long domain (SPL) and squares denote RMSE for the regular domain (SPR).

450 Figure 9 shows the RMSEs with time for the state-parameter estimation experiments in the regular and
 451 long domain. Comparison of figures 5 and 9 demonstrates a very clear improvement in the forecast for joint
 452 state-parameter estimation over the state only case (note the different scales on the y axes). Joint state-parameter
 453 estimation markedly increases the observation impact for exactly the same observations. The extra computational
 454 cost of estimating the friction parameter along with the state is extremely small, as it adds only a single extra
 455 component to the state vector. Joint state-parameter estimation is therefore a very efficient way of producing a
 456 much better forecast in this situation.

457 The small RMSE between the truth and the forecast for joint state-parameter estimation is of the order of
 458 the observation error. There is no longer any significant difference between the results for the different length
 459 domains and this implies that the error growth must occur at similar rates along the length of the long domain
 460 when the friction parameter is estimated.

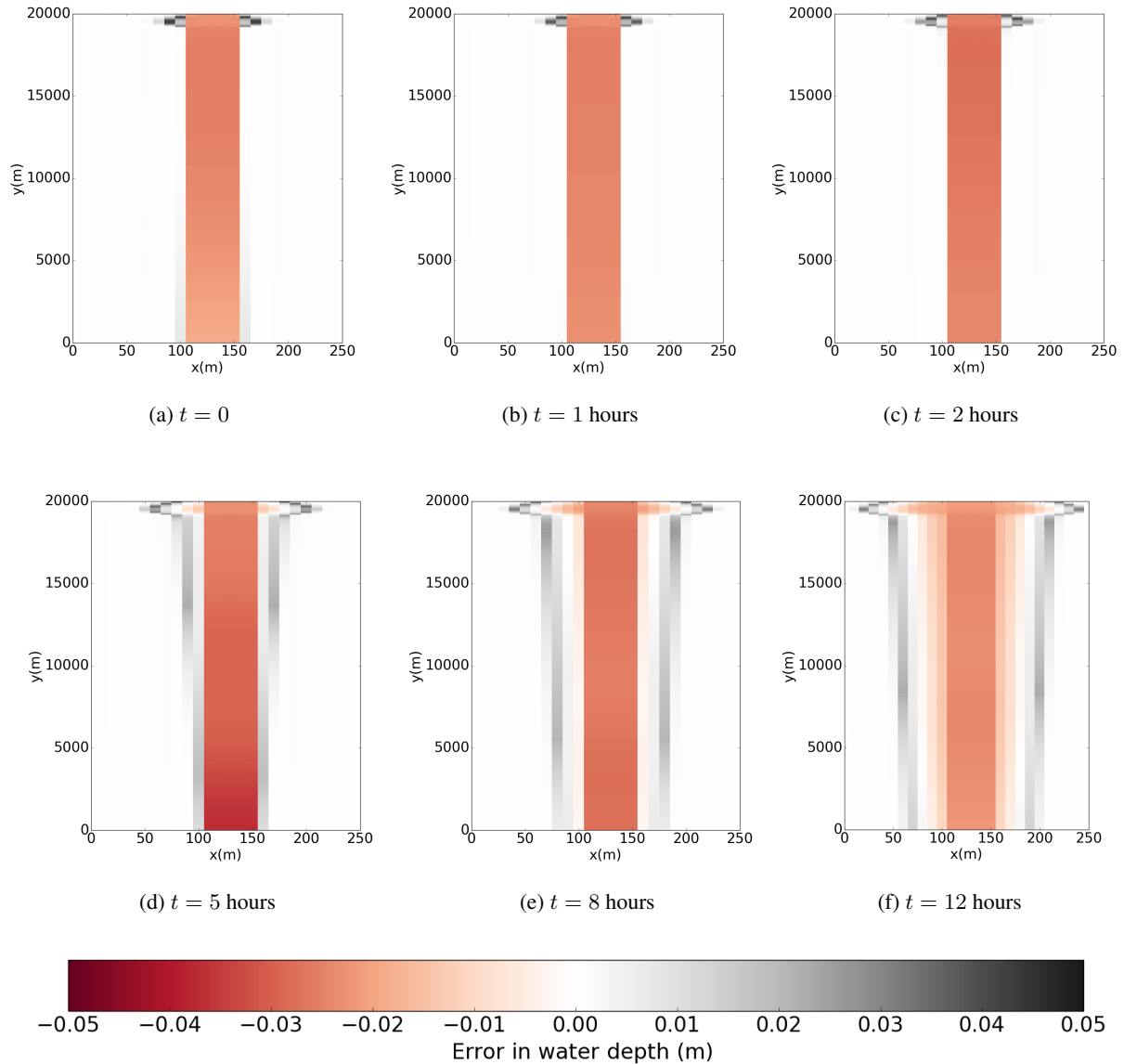


Figure 10: Forecast (ensemble mean) water depth minus true water depth in the long domain, shown in plan view for case SPL. Times are measured from assimilation at $t=52$ h. For reference, the true water depth on the floodplain varied between 0 and 0.4m during this forecast period. Water depth in the centre of channel varied between 5.9m and 6.4m.

461 Figure 10 shows the the difference between the forecast ensemble mean and the true water levels, plotted
 462 in plan view in the long domain, at several times during the forecast step starting at $t = 52$ hours for the SPL
 463 experiment. Note that the scale in figure 10 is ten times smaller than in figure 6. Figure 10a shows the difference
 464 between the forecast ensemble mean water depths and the true water depths at the observation/assimilation time.
 465 As in the SOL experiment, the error between the forecast ensemble mean and true water depths is small at all
 466 points in the domain at this time. Figure 10b shows the error between the forecast and the truth 1 hour after
 467 the assimilation; figures 10c (2 hours after assimilation), 10d (5 hours after assimilation), 10e (8 hours after

468 assimilation) and 10f (12 hours after assimilation) show how the error evolves. Unlike in the SOL experiment,
 469 the error does not propagate from upstream to downstream; instead, the error grows at a similar rate along
 470 the length of the domain. This further suggests that the upstream-downstream error growth seen in the SOL
 471 experiments is due to incorrect friction parameter specification.

472 Figure 10 shows that the mean forecast overestimates water depth on the floodplain but underestimates
 473 water depth in the channel. This reflects the fact that although each ensemble member predicts a physically
 474 realistic water level that is flat in cross section, the ensemble mean forecast is not necessarily flat and therefore
 475 not physically realistic. This is because the forecast mean water depth in each cell is the average value predicted
 476 by the ensemble members. An example of this situation is shown in figure 11.

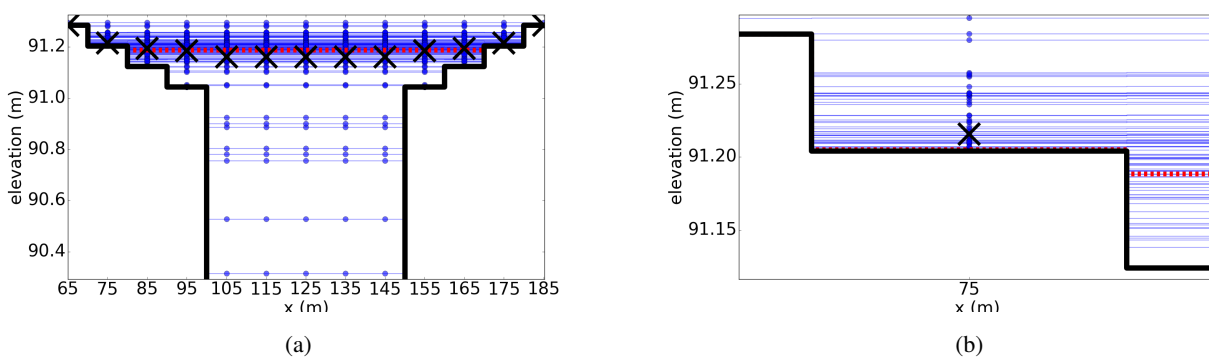


Figure 11: Cross section of the domain showing bathymetry as a solid black line. The true water level is shown as a dashed red line, water levels predicted by each ensemble member are shown as blue circles. The mean forecast in each model cell is shown as a cross. Figure 11a shows the central part of the domain from $65 \leq x \leq 185$ m. Figure 11b shows the forecast water levels and resulting forecast mean in the cell centred at 75m in greater detail.

477 Figure 11 shows the true flood level at one cross section of the domain and the water level predicted by
 478 each ensemble member. The crosses show the mean ensemble water level in each cell in the cross section. In
 479 the channel (e.g. at $x = 125$ m), figure 11a shows the ensemble predictions are such that the ensemble mean
 480 is slightly lower than the true water level. Beyond the edge of the true flood on the flood plain, the true water
 481 depth relative to the topography is zero, and most ensemble members also predict zero water depth. However,
 482 as shown in figure 11b for the cell at $x = 75$ m, there are cells beyond the flood edge in which some ensemble
 483 members predict non-zero water depth and the ensemble mean is therefore a very small positive water depth;
 484 this simply follows from equation 9. It is therefore possible for the ensemble mean to predict water levels
 485 deeper than the truth in cells beyond the true flood edge where there are a number of ensemble members which
 486 predict non-zero depth, even when the water level is under-predicted in the channel. It should be noted that the
 487 errors are very small.

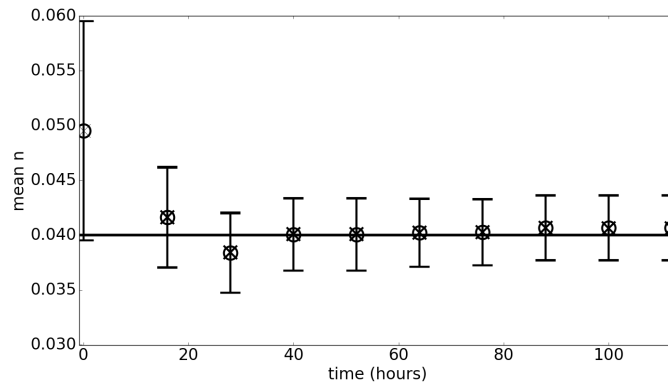


Figure 12: Calculated (analysis) mean channel friction parameter values at each assimilation time. The true value is shown by the horizontal line. Open circles show the values for the long domain, crosses for the regular domain. The error bars show one standard deviation of the analysis parameter distribution for the long domain; values for the regular domain are very similar.

488 Figure 12 shows the analysis ensemble mean value of the channel friction parameter at each assimilation
 489 time. The true value of the channel friction parameter, n_{ch} , indicated by the solid horizontal line, and the
 490 incorrect initial mean value is shown at time zero. The error bars show one standard deviation of the analysis
 491 n_{ch} distribution. The results show that the joint-state parameter data estimation produces a good estimate of
 492 the value of n_{ch} , and that the ensemble mean values are almost identical for both the regular and long domains.
 493 It is notable that the convergence of the estimated channel friction parameter value to the truth is achieved with
 494 water depth observations only taken on the floodplain.

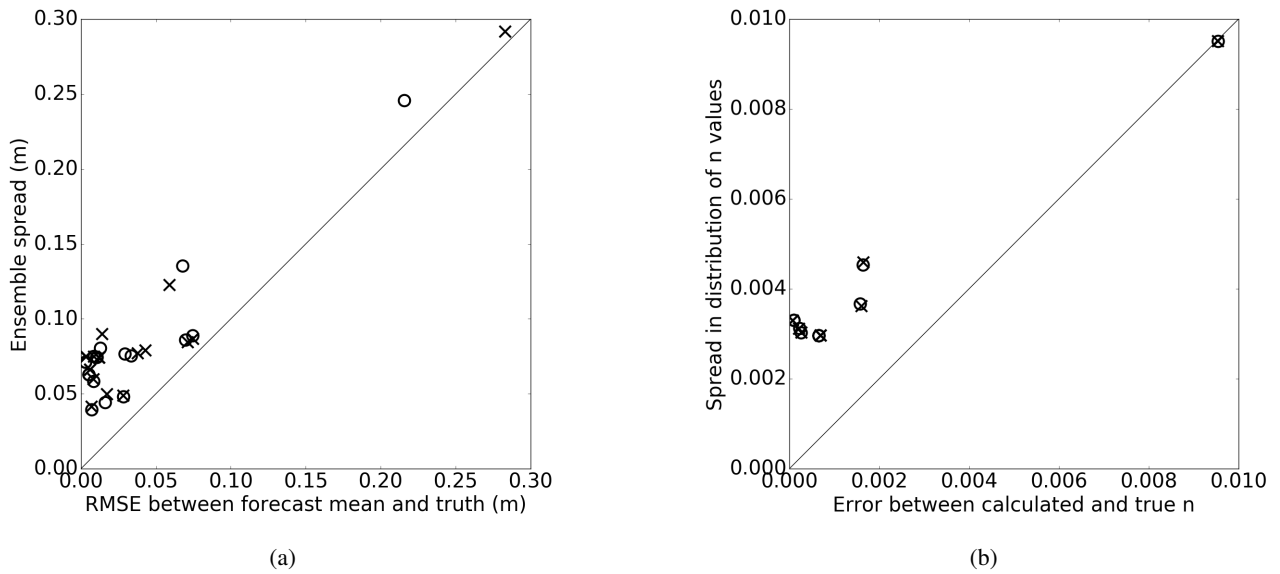


Figure 13: Reliability plot for the SPR and SPL experiments. Circles are for the long domain, crosses for the regular domain. Plots show error vs spread for (a) the ensemble of water levels and (b) the n_{ch} distribution.

495 Reliability plots for the ensemble of state vectors are given in figure 13a and for the calculated parameter
 496 distributions in figure 13b. The plots show no evidence of ensemble collapse, which can be a problem in
 497 ensemble data assimilation schemes. In fact the spread of the state and parameter distributions remains broader
 498 than the size of the error in our experiments, which minimises the risk of overfitting the value of n_{ch} at a
 499 particular time in the simulation. If the spread of either the parameter or the state ensembles became too small
 500 it would be necessary to use inflation techniques (see e.g. Anderson (2007)).

501 These results show a clear advantage in jointly estimating the channel friction parameter alongside the
 502 model state; this contrasts with the findings of Garcia-Pintado et al. (2015), where no clear improvement in
 503 forecast water levels was seen. There are a number of possible reasons for this, one being that in Garcia-
 504 Pintado et al. (2015) convergence of the channel friction parameter value to a steady value was slow compared
 505 to the timescales of the flood event. The difference between our results and those in Garcia-Pintado et al. (2015)
 506 may also be related to the fact that there are more sources of uncertainty in Garcia-Pintado et al. (2015), which
 507 used real data and real topography, rather than the idealised situation in this study. One significant source of
 508 time-varying error not accounted for in the setup used by Garcia-Pintado et al. (2015) and not present in our
 509 experiments is lateral inflows (see Bermudez et al. (2017)). It may also be that the initial parameter value used
 510 in Garcia-Pintado et al. (2015) was already close to the true value, such that the error in the parameter was not a
 511 large source of error, whereas our initial guess was incorrect by design. A better initial guess would also explain
 512 the smaller changes to n_{ch} produced by the data assimilation in Garcia-Pintado et al. (2015). Alternatively, it
 513 may be that the presence of the initialisation shock in Garcia-Pintado et al. (2015) prevented convergence to a
 514 more accurate channel friction parameter.

515 Another possible reason for the contrasting importance to the forecast of updating the channel friction
 516 parameter may be that in Garcia-Pintado et al. (2015) a bias correction was also made to the inflow as part of
 517 the data assimilation. It may be that inflow correction was also indirectly including some of the effects of the
 518 incorrect n_{ch} parameter. This seems likely, since the upstream-downstream error propagation pattern seen in
 519 figure 6 would also be expected for an incorrectly specified inflow. Thus it may be that no added benefit was
 520 gained from including n_{ch} estimation in addition to inflow bias estimation because correcting error in inflow
 521 bias also compensates for any error in n_{ch} . To test the interdependence of inflow error and error in n_{ch} we
 522 conducted some state-parameter estimation experiments exactly as for the SPL experiments but with biased
 523 inflows. No correction was made to the biased inflow, but the value of n_{ch} was updated at each assimilation
 524 time.

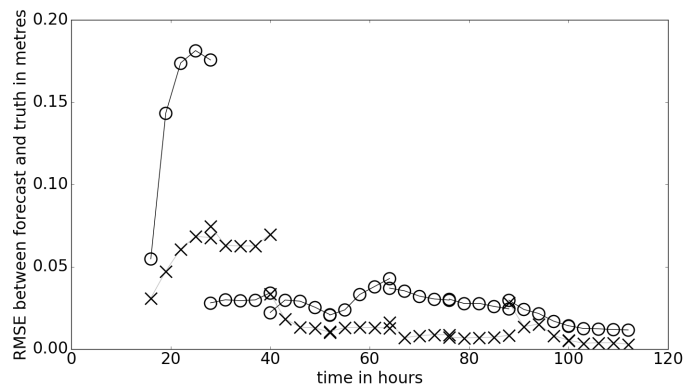


Figure 14: RMSEs between the mean forecast and the truth for positive inflow bias in the long domain shown as open circles. The corresponding RMSEs for the unbiased inflow are shown as crosses for comparison.

525 Figure 14 shows water level RMSEs with time for the long domain with biased and unbiased inflows, and
 526 demonstrates that correction of the channel friction parameter allows the forecast to predict accurate water
 527 levels, even with a biased inflow. The correction to the value of n_{ch} is therefore compensating for inflow bias.

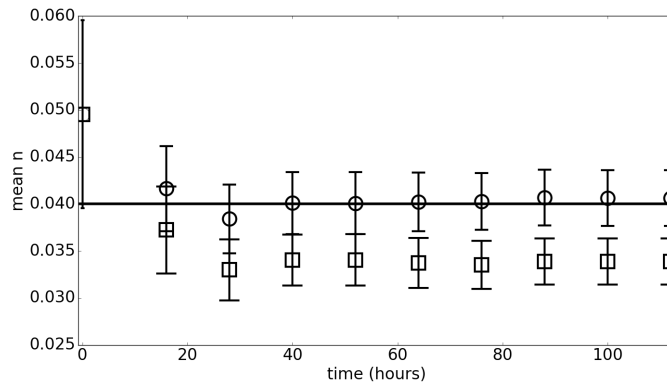


Figure 15: Calculated values of mean n_{ch} for biased inflow in the long domain shown as squares. Circles show the corresponding values for unbiased inflow. The horizontal line shows the true value and the error bars show one standard deviation of the calculated n_{ch} distribution.

528 The updated values of n_{ch} with time for biased inflow are shown in figure 15. When the inflow is biased,
 529 the value of n_{ch} does not converge to the true value, but instead to a value which allows it to compensate
 530 for inflow bias and minimise errors in water levels in the domain. This clearly indicates an interdependence
 531 between errors in channel friction parameter value and inflow.

532 Whatever the reason for the differences to the results in Garcia-Pintado et al. (2015), the work presented
 533 here shows that our inundation forecast model is sensitive to the channel friction parameter, and that the correct
 534 value of the parameter can be retrieved from observations of water depth by using joint state-parameter data
 535 assimilation during a flood event with unbiased inflow information.

536 5 Conclusions

537 In this study, we have investigated the effect of domain length and channel friction parameter estimation in
 538 data assimilation for flood inundation forecasting. We have also demonstrated that assuming water has zero
 539 momentum at the start of each forecast step can cause an initialisation shock. The period of time for which this
 540 shock then causes problems for the forecast is likely to be domain dependent; in this study we found that the
 541 impact of the shock disappeared within a period of approximately 4 hours. We developed a novel method to
 542 reinitialise water velocities in each model grid cell with pre-assimilation values, and showed that this approach
 543 eliminated the initialisation shock.

544 In agreement with Andreadis et al. (2007), Neal et al. (2009), Garcia-Pintado et al. (2013) and Matgen
 545 et al. (2010), we found that assimilating SAR-like water levels in a state-only data assimilation system gives
 546 a time limited improvement in the forecast skill, since such improvement can only persist for as long as the
 547 information is relevant in the domain. We have shown that considering a longer domain extends the time over
 548 which observations have an impact on the forecast, even when no extra observations are used. This is because

549 the ETKF is able to correct water levels downstream of the observations due to strong covariances between the
550 errors in water levels in different parts of the domain. In a domain with more realistic topography, the correla-
551 tions between the errors in water depth in different parts of the domain may not be as strong, and are likely to be
552 more complex. However, work by authors such as Garcia-Pintado et al. (2015) indicates that water level errors
553 in large, real domains are correlated, as depths can be corrected at considerable distances from SAR-derived ob-
554 servations. Additionally, understanding the effects of domain length and friction parameter estimation without
555 the extra complications of topographical features is important in understanding the fundamental sensitivities of
556 such systems.

557 We have shown that in the forecast period following an assimilation, the difference between the forecast
558 and the truth when the channel friction parameter is incorrectly specified and not updated grows faster in
559 the upstream part of the domain, and then propagates downstream. This error propagation is the reason that
560 the forecast ensemble retains skill for a longer time in the long domain; the errors grow more slowly in the
561 downstream areas which are not considered in the regular domain.

562 Jointly estimating the channel friction parameter along with the water levels is shown to produce a signif-
563 icantly better forecast for the same observations at very little extra cost. This was not seen in Garcia-Pintado
564 et al. (2015), in which inflow and parameters were estimated simultaneously. Correcting the channel friction
565 parameter also eliminates the differences in forecast error growth for the two different domain lengths, as errors
566 grow at similar rates in the upstream and downstream parts of the domain. We have shown that it is possible to
567 estimate a good value for the channel friction parameter, even when water level observations are available only
568 on the floodplain.

569 In summary, we have shown that in the case where there is no inflow bias but channel friction is incor-
570 rectly specified, assimilating SAR-like water levels from floodplains provides a time limited improvement in
571 the forecast when only water levels are corrected. The time over which the forecast is improved depends on the
572 length of the domain of interest. Authors such as Andreadis et al. (2007); Matgen et al. (2010); Giustarini et al.
573 (2011); Garcia-Pintado et al. (2015, 2013) have shown that inflow correction can lead to a marked improvement
574 in forecast skill. We have shown that jointly estimating the channel friction parameter along with the water lev-
575 els also provides a clear improvement in the forecast at all times and can retrieve an accurate channel friction
576 parameter value. Our results suggest that it may be difficult to separate out errors due to incorrect specification
577 of inflow and incorrect specification of channel friction when carrying out ensemble data assimilation for inun-
578 dation modelling. This is because the character of the errors in the forecast resulting from these two sources of
579 uncertainty are similar; this interdependence explains our finding that updating the value of the channel friction
580 parameter can compensate for a bias in inflow. Further study is required to see how well each of these conclu-
581 sions are applicable to more complex and realistic topography, and for real satellite derived observations. In
582 this way, the work here may serve to enhance operational flood forecasting potential.

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588 on request, subject to licensing conditions.

589 Appendix A Inflow and friction source terms

590 In order to model fluvial flooding in a stretch of river, the amount of water flowing into that stretch needs to be
591 modelled. Here we describe the implementation of a new inflow source term in Clawpack. Clawpack is able to
592 solve systems of partial differential equations with or without source terms and is designed such that the user
593 can introduce new code to describe additional source terms. Our new inflow source term has been implemented
594 in the code in a similar way to the pre-existing friction source term. The code for the friction source term is
595 outlined in section A.1 and the new inflow source term is described in section A.2.

596 A.1 Pre-existing friction source term

597 Friction between the fluid and the channel in which it is flowing acts as a momentum source in the shallow
598 water equations. This is represented in Clawpack with a source term of the form

$$\mathbf{R}(\mathbf{q})_{friction} = \begin{bmatrix} 0 \\ -\gamma(hu) \\ -\gamma(hv) \end{bmatrix}, \quad (\text{A.1})$$

599 where γ is given by

$$\gamma = \frac{gn^2 \sqrt{(hu)^2 + (hv)^2}}{h^{\frac{7}{3}}}, \quad (\text{A.2})$$

600 h is water depth and u and v are velocities in the x and y directions. Acceleration due to gravity is denoted g
601 and n is Manning's friction coefficient. This coefficient describes the roughness of the channel bed in which
602 the water is flowing and in practical applications its value is usually determined empirically. The value of n is
603 specified by the user in the Clawpack code, and can vary over the domain if specified in the simulation setup.
604 The units of n are $sm^{-1/3}$.

605 In Clawpack, inhomogeneous sets of equations are solved using the method of fractional stepping described
606 in LeVeque (2002) p.380-395. This method splits the equation into two simpler problems; one homogeneous
607 conservation law and one inhomogeneous partial differential equation - which can be solved independently over
608 the same time step. The solutions are then combined in an alternating fashion to give a solution to the whole
609 problem. For a friction source term, the set of problems to be solved are the homogeneous system

$$\frac{\partial \mathbf{q}}{\partial t} + \frac{\partial \mathbf{F}(\mathbf{q})}{\partial x} + \frac{\partial \mathbf{G}(\mathbf{q})}{\partial y} = 0, \quad (\text{A.3})$$

610 and the source term equation

$$\frac{\partial \mathbf{q}}{\partial t} = \mathbf{R}(\mathbf{q})_{friction}, \quad (\text{A.4})$$

611 with $\mathbf{R}(\mathbf{q})_{friction}$ as in A.1 and \mathbf{q} a vector of conserved quantities (see equation (2)). For each time step in the
 612 code, equation (A.3) is advanced from t_i to t_{i+1} to give intermediate values of h_* , hu_* and hv_* in \mathbf{q}_* . The
 613 values in \mathbf{q}_* are then used to solve equation (A.4) over the same time step. This introduces a ‘splitting error’
 614 into the solution of order $\Delta t = t_{i+1} - t_i$, making the whole method only first order accurate. A more accurate
 615 splitting method (‘Strang splitting’) is available for implementation in the code, but the first order accuracy has
 616 been found to be more stable and sufficient in practice for a wide range of applications (LeVeque, 2002, 1997).

617 A.2 Novel inflow source term

618 For inundation simulations, water entering the domain of interest can be modelled as a source term. We have
 619 added a novel inflow source term to the Clawpack code to model river-like flow. In operational situations,
 620 information regarding this source term may be available from an upstream gauge as a mass flow rate, Q ,
 621 measured in $m^3 s^{-1}$. In an ungauged catchment, the same information could be generated using a rainfall run-
 622 off model. Here we use hourly values of Q based on gauge data; linear interpolation is carried out between the
 623 hourly values. A water mass flow rate can be turned into a source term, S expressed in ms^{-1} (c.f. the term
 624 ‘Sce’ in Hervouet (2007) p.31, which has the same units and can include rainfall, infiltration etc) as long as
 625 the area of the domain or ‘footprint’ over which the water is added is known. For water added over an area A ,
 626 $S = Q/A$. The equation for the inflow source term is then given by

$$\frac{\partial \mathbf{q}}{\partial t} = \mathbf{R}(\mathbf{q})_{inflow}, \quad (\text{A.5})$$

627 where

$$\mathbf{R}(\mathbf{q})_{inflow} = \begin{bmatrix} S \\ 0 \\ 0 \end{bmatrix}. \quad (\text{A.6})$$

628 Equations A.5 and A.6 show that for each time step Δt , the change in h due to the incoming water will
 629 depend on the value of the inflow source, S , over the same Δt . The extra water arriving in the domain creates
 630 extra water height, and is assumed here to arrive without any momentum; the water is subject only to hydrostatic
 631 momentum effects. This inflow source term has been implemented in the code in the following way

- 632 • determine in which grid cells the source term will be applied. This is reasonably arbitrary but must be
 633 such that the solution remains stable (we used trial and error in this experiment);

- 634 • calculate the total area that the inflow cells cover in the domain, A ;
- 635 • for a given mass flow rate Q , calculate S for each value of Q by dividing by A ;
- 636 • at the relevant grid points extract depth, h_* , as calculated from equation (A.3);
- 637 • calculate the change to h_* due to incoming water from a discretisation of equation (A.6) using a Crank-
- 638 Nicholson scheme (Crank and Nicolson, 1996)

$$h = h_* + \Delta t \frac{S(t) + S(t + \Delta t)}{2}; \quad (\text{A.7})$$

- 639 • use the new value of h from equation (A.7) to solve for the next time step.

640 **A.3 Combining friction and inflow source terms**

641 The source terms described in this section are applied in a sequential manner in the code. For each time step,
 642 the inflow source term calculates the new water depths in the relevant parts of the domain and then the friction
 643 source term is applied to the new water depths.

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